



Horizon 2020  
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for Research & Innovation

# Stefano Gariazzo

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*CSIC – Universitat de Valencia*

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## Relic neutrinos and the PTOLEMY project

## 1 *Cosmic Neutrino Background*

## 2 *Direct detection of relic neutrinos*

- Some proposed methods
- Neutrino capture

## 3 *Relic neutrino clustering at Earth*

- N-one-body simulations
- Results from the Milky Way
- Systematics and future developments

## 4 *PTOLEMY*

- The experiment
- Simulations
- Perspectives

## 5 *Beyond the standard: light sterile neutrinos*

## 6 *Conclusions*

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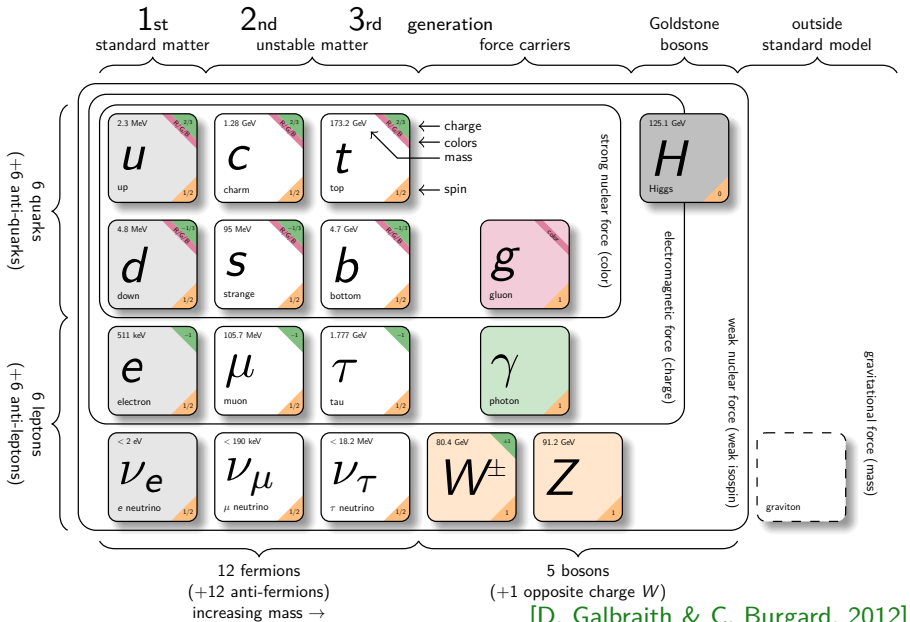
## 4 *PTOLEMY*

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## 5 *Beyond the standard: light sterile neutrinos*

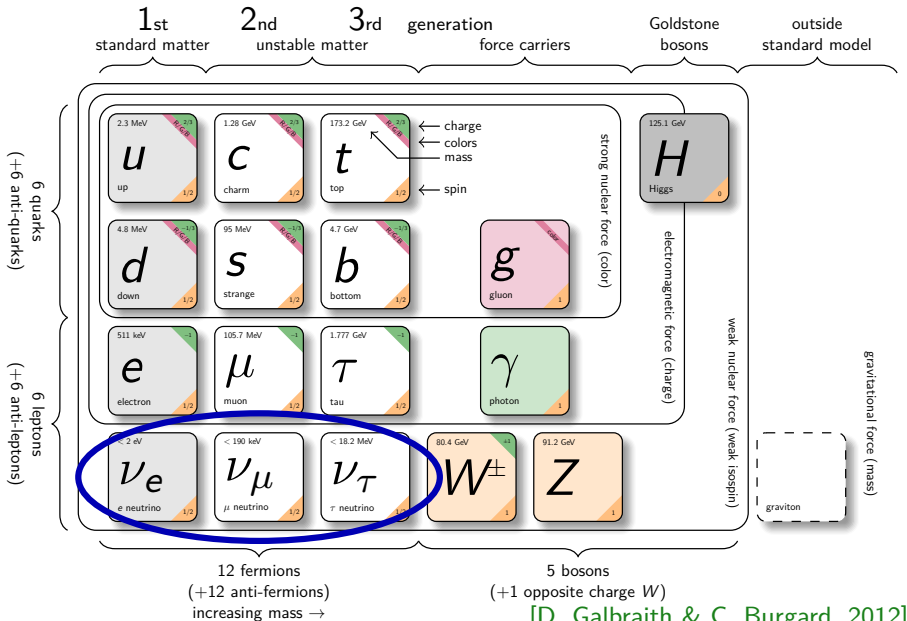
## 6 *Conclusions*

# The Standard Model of Particle Physics



[D. Galbraith & C. Burgard, 2012]

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# Three Neutrino Oscillations

Analogous to CKM mixing for quarks:

[Pontecorvo, 1968]

[Maki, Nakagawa, Sakata, 1962]

$$\nu_\alpha = \sum_{k=1}^3 U_{\alpha k} \nu_k \quad (\alpha = e, \mu, \tau)$$

$\nu_\alpha$  flavour eigenstates,  $U_{\alpha k}$  PMNS mixing matrix,  $\nu_k$  mass eigenstates.

Current knowledge of the 3 active  $\nu$  mixing: [de Salas et al. (2018)]

$\Delta m_{ji}^2 = m_j^2 - m_i^2$ ,  $\theta_{ij}$  mixing angles

**NO**: Normal Ordering,  $m_1 < m_2 < m_3$

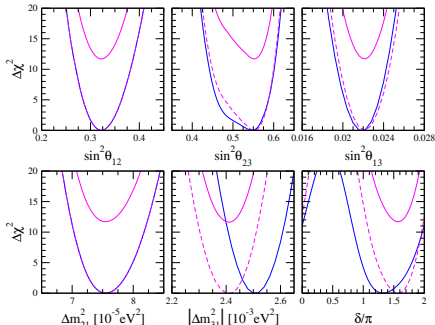
**IO**: Inverted Ordering,  $m_3 < m_1 < m_2$

$$\begin{aligned} \Delta m_{21}^2 &= (7.55^{+0.20}_{-0.16}) \cdot 10^{-5} \text{ eV}^2 \\ |\Delta m_{31}^2| &= (2.50 \pm 0.03) \cdot 10^{-3} \text{ eV}^2 \text{ (NO)} \\ &= (2.42^{+0.03}_{-0.04}) \cdot 10^{-3} \text{ eV}^2 \text{ (IO)} \end{aligned}$$

$$\begin{aligned} \sin^2(\theta_{12}) &= 0.320^{+0.020}_{-0.016} \\ \sin^2(\theta_{13}) &= 0.0216^{+0.008}_{-0.007} \text{ (NO)} \\ &= 0.0222^{+0.007}_{-0.008} \text{ (IO)} \end{aligned}$$

$$\begin{aligned} \sin^2(\theta_{23}) &= 0.547^{+0.020}_{-0.030} \text{ (NO)} \\ &= 0.551^{+0.018}_{-0.030} \text{ (IO)} \end{aligned}$$

First hints for  $\delta_{\text{CP}} \simeq 3/2\pi$



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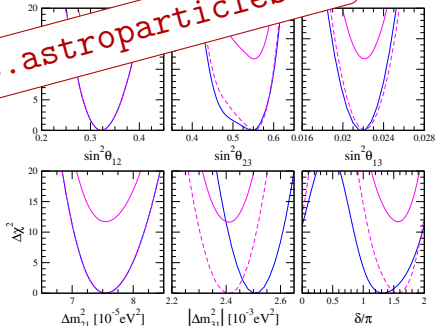
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$$= 0.022^{+0.007}_{-0.008} \text{ (IO)}$$

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see also: <http://globalfit.astroparticles.es>

# Neutrinos and their masses

## Normal ordering (NO)

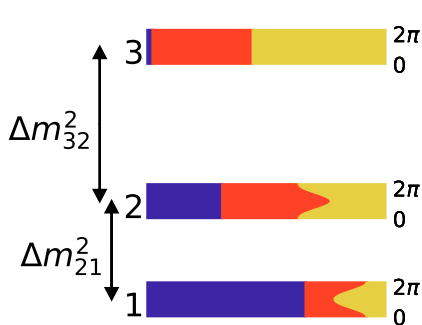
$$m_1 < m_2 < m_3$$

$$\sum m_k \gtrsim 0.06 \text{ eV}$$

  $\nu_e$

  $\nu_\mu$

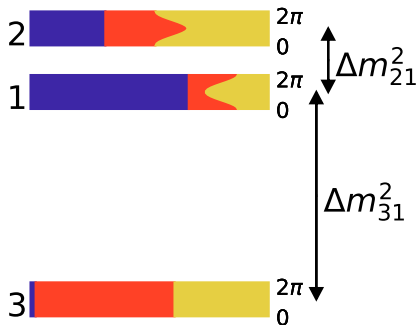
  $\nu_\tau$



## Inverted ordering (IO)

$$m_3 < m_1 < m_2$$

$$\sum m_k \gtrsim 0.1 \text{ eV}$$

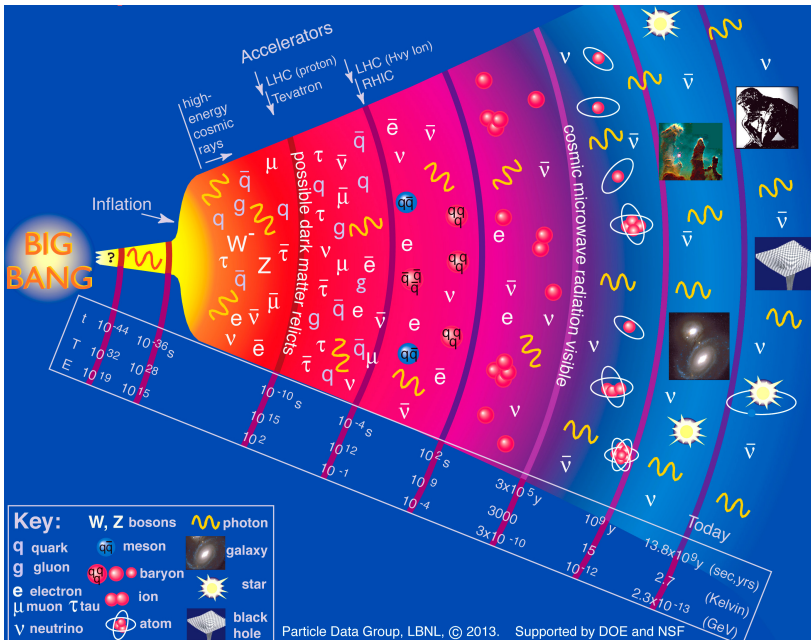


Absolute scale unknown!

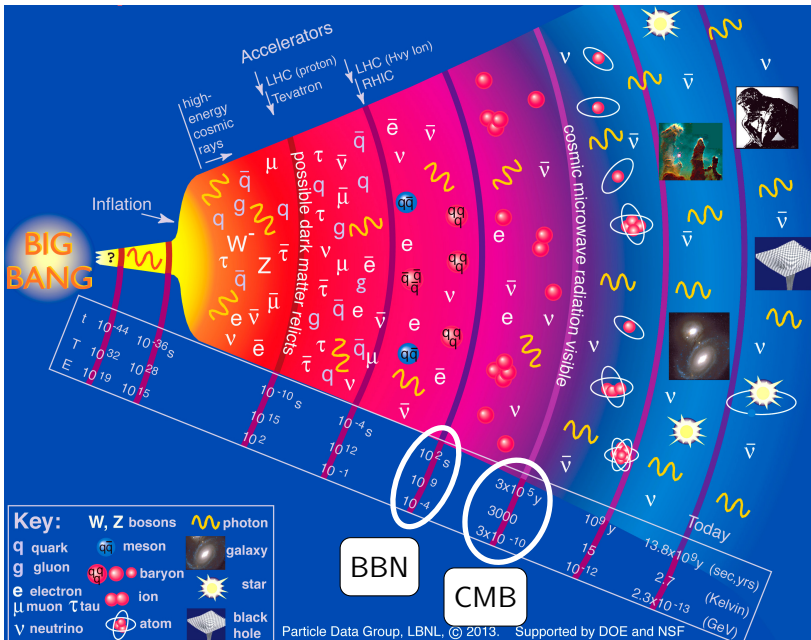
Can we constrain the mass ordering using bounds on  $\sum m_\nu$ ?



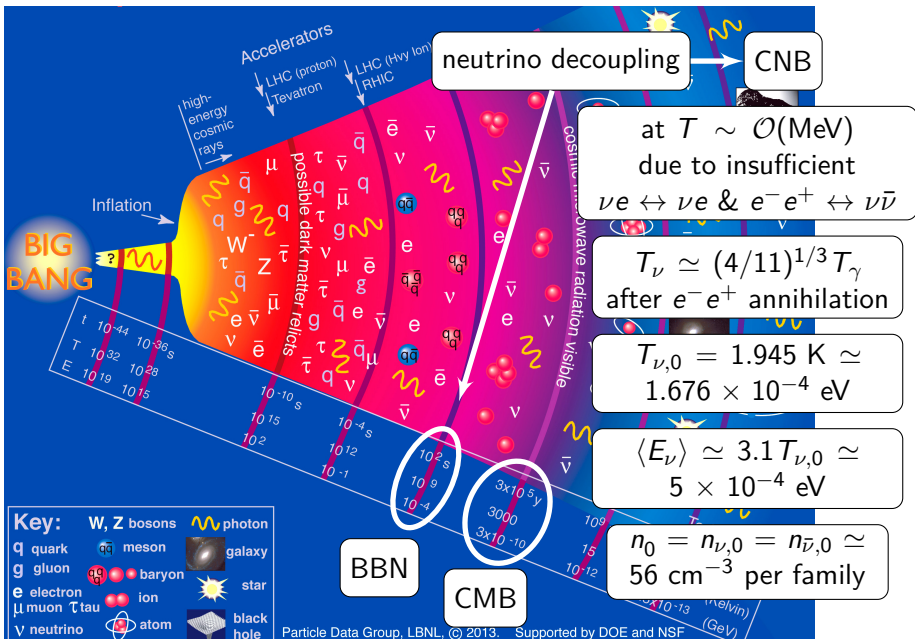
# History of the universe



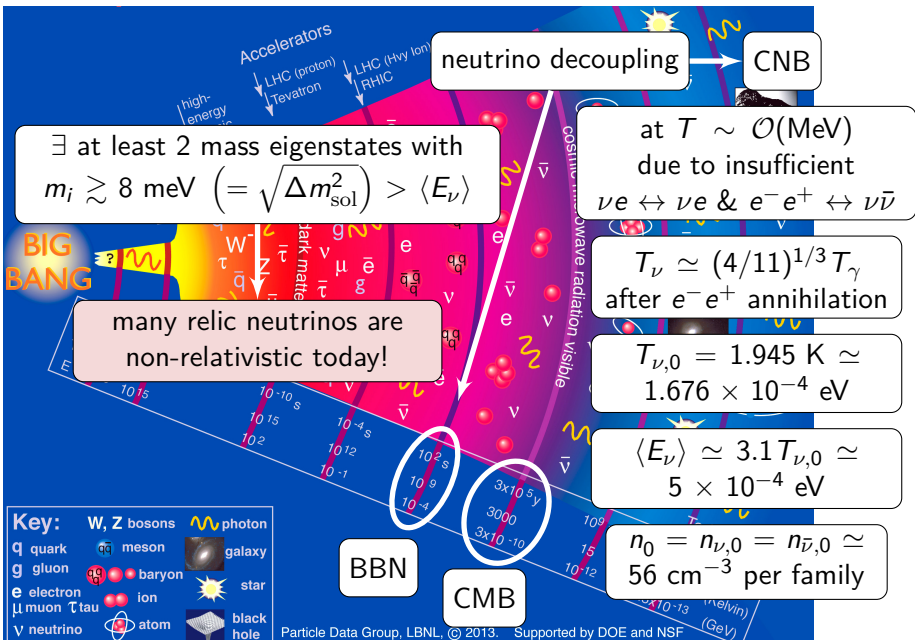
# History of the universe



# History of the universe



# History of the universe



# Relic neutrinos in cosmology: $N_{\text{eff}}$

Radiation energy density  $\rho_r$  in the early Universe:

$$\rho_r = \left[ 1 + \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} N_{\text{eff}} \right] \rho_\gamma = [1 + 0.2271 N_{\text{eff}}] \rho_\gamma$$

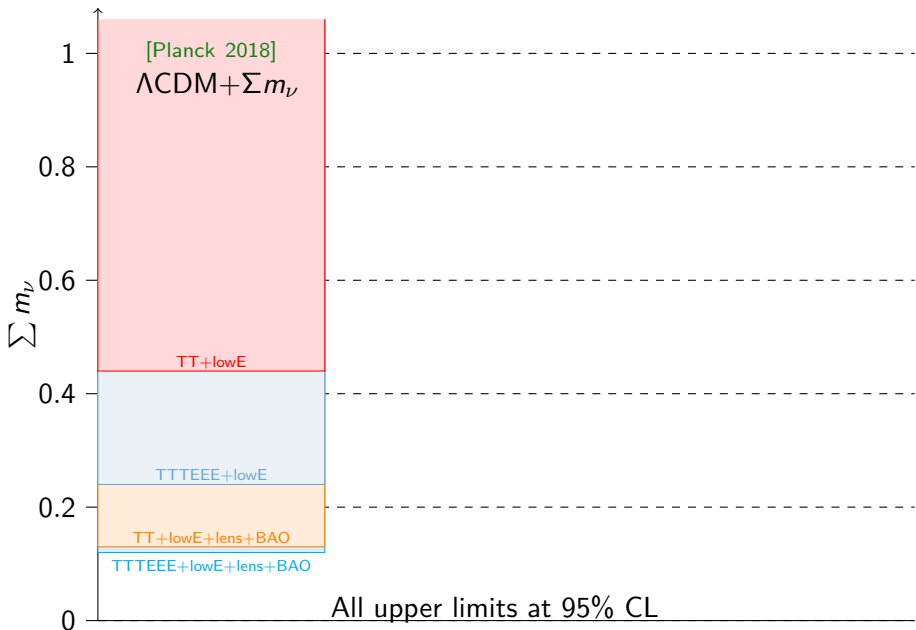
$\rho_\gamma$  photon energy density,  $7/8$  is for fermions,  $(4/11)^{4/3}$  due to photon reheating after neutrino decoupling

- $N_{\text{eff}} \rightarrow$  all the radiation contribution not given by photons
- $N_{\text{eff}} \simeq 1$  correspond to a single family of active neutrino, in equilibrium in the early Universe
- Active neutrinos:  
 $N_{\text{eff}} = 3.046$  [Mangano et al., 2005] (damping factors approximations)  $\sim$   
 $N_{\text{eff}} = 3.045$  [de Salas et al., 2016] (full collision terms)  
due to not instantaneous decoupling for the neutrinos
- + Non Standard Interactions:  $3.040 < N_{\text{eff}} < 3.059$  [de Salas et al., 2016]

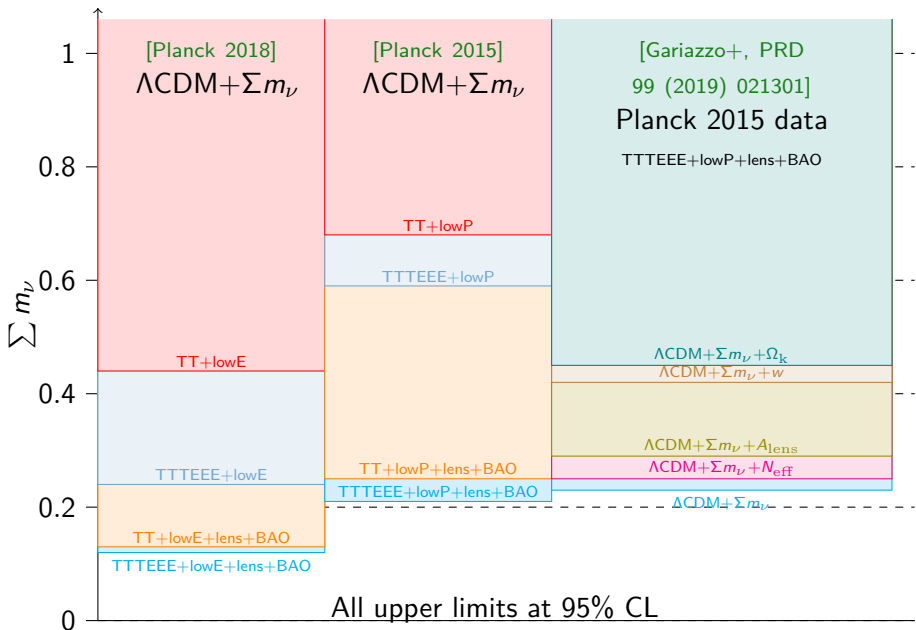
Observations:  $N_{\text{eff}} \simeq 3.0 \pm 0.2$  [Planck 2018]  
Indirect probe of cosmic neutrino background!

$\gg 10\sigma!$

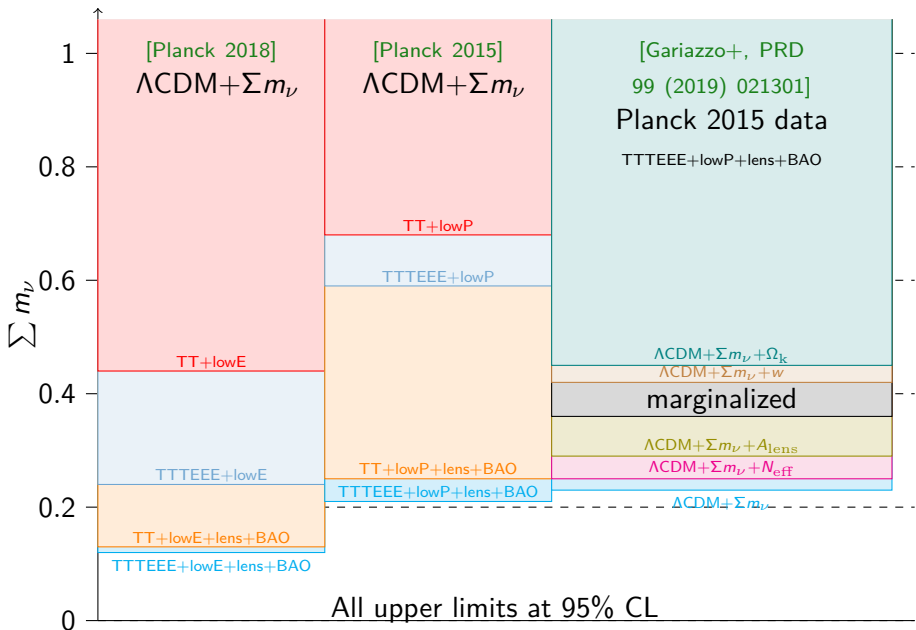
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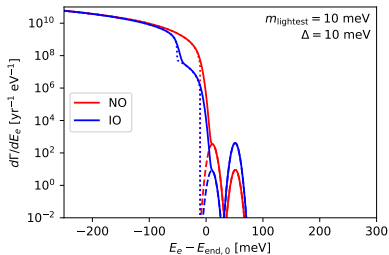
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How to directly detect non-relativistic neutrinos?

Stodolsky effect

[Stodolsky, 1974][Duda et al., 2001]

(only if there is  
lepton asymmetry)

energy splitting of  $e^-$  spin states due to  
coherent scattering with relic neutrinos



torque on  $e^-$  in lab rest frame



use a ferromagnet to build detector



measure torque with a torsion balance

# Direct detection - proposed methods - Stodolsky effect

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expected  $a_\nu \simeq \mathcal{O}(10^{-26}) \text{ cm/s}^2$



$a_{\text{exp}} \simeq \mathcal{O}(10^{-12}) \text{ cm/s}^2$

# Direct detection - proposed methods - at interferometers

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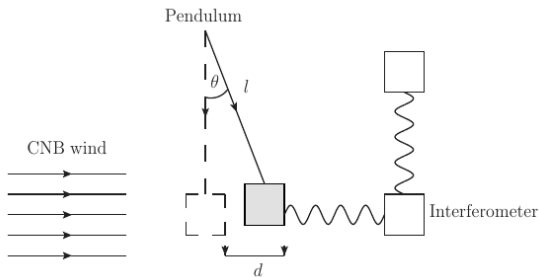
At interferometers

[Domcke et al., 2017]

coherent scattering of relic  $\nu$  on a pendulum



measure oscillations at interferometers



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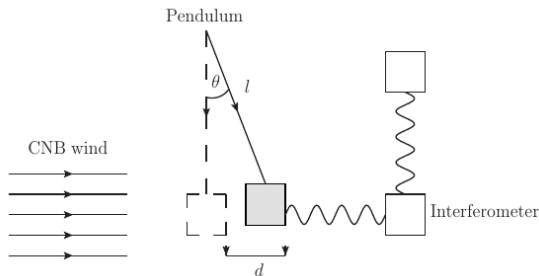
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expected

$$10^{-33} \lesssim a_\nu / (\text{cm/s}^2) \lesssim 10^{-27}$$

$$a_{\text{LIGO/Virgo}} \simeq 10^{-16} \text{ cm/s}^2$$

# Direct detection - proposed methods - Capture (I)

How to directly detect non-relativistic neutrinos?

Remember that  
 $\langle E_\nu \rangle \simeq \mathcal{O}(10^{-4})$  eV today

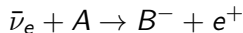


a process without energy  
threshold is necessary

(anti)neutrino capture on  
electron-capture-decaying nuclei

[Cocco et al., 2009]

electron capture (EC):  $e^- + A^+ \rightarrow \nu_e + B^*$   
( $e^-$  from inner level)



must have very specific  $Q$  value  
in order to avoid EC back-  
ground and have no threshold



specific energy conditions required

but

$Q$  value depends on  
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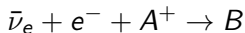
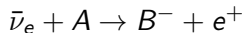


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$Q$  value depends on  
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process useful only “if specific conditions on the  $Q$ -value are met  
or significant improvements on ion storage rings are achieved”

# A viable method - Capture (II)

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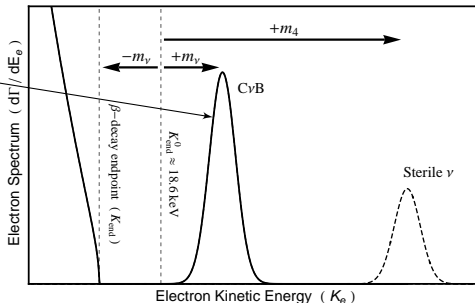
[Weinberg, 1962]: neutrino capture in  $\beta$ -decaying nuclei  $\nu + n \rightarrow p + e^-$

Main background:  $\beta$  decay  $n \rightarrow p + e^- + \bar{\nu}$ !

signal is a peak at  $2m_\nu$   
 above  $\beta$ -decay endpoint

only with a lot of material

need a very good energy resolution





best element has highest  $\sigma_{\text{NCB}}(v_\nu/c) \cdot t_{1/2}$

to minimize contamination from  $\beta$  decay background

Isotope	Decay	$Q_\beta$ (keV)	Half-life (s)	$\sigma_{\text{NCB}}(v_\nu/c)$ ( $10^{-41}$ cm <sup>2</sup> )
<sup>3</sup> H	$\beta^-$	18.591	$3.8878 \times 10^8$	$7.84 \times 10^{-4}$
<sup>63</sup> Ni	$\beta^-$	66.945	$3.1588 \times 10^9$	$1.38 \times 10^{-6}$
<sup>93</sup> Zr	$\beta^-$	60.63	$4.952 \times 10^{13}$	$2.39 \times 10^{-10}$
<sup>106</sup> Ru	$\beta^-$	39.4	$3.2278 \times 10^7$	$5.88 \times 10^{-4}$
<sup>107</sup> Pd	$\beta^-$	33	$2.0512 \times 10^{14}$	$2.58 \times 10^{-10}$
<sup>187</sup> Re	$\beta^-$	2.64	$1.3727 \times 10^{18}$	$4.32 \times 10^{-11}$
<sup>11</sup> C	$\beta^+$	960.2	$1.226 \times 10^3$	$4.66 \times 10^{-3}$
<sup>13</sup> N	$\beta^+$	1198.5	$5.99 \times 10^2$	$5.3 \times 10^{-3}$
<sup>15</sup> O	$\beta^+$	1732	$1.224 \times 10^2$	$9.75 \times 10^{-3}$
<sup>18</sup> F	$\beta^+$	633.5	$6.809 \times 10^3$	$2.63 \times 10^{-3}$
<sup>22</sup> Na	$\beta^+$	545.6	$9.07 \times 10^7$	$3.04 \times 10^{-7}$
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<sup>3</sup>H better because the cross section ( $\rightarrow$  event rate) is higher

$$\frac{d\tilde{\Gamma}_{\text{CNB}}}{dE_e}(E_e) = \frac{1}{\sqrt{2\pi}\sigma} \sum_{i=1}^{N_\nu} \bar{\sigma} N_T |U_{ei}|^2 n_i \times e^{-\frac{[E_e - (E_{\text{end}} + m_j + m_{\text{lightest}})]^2}{2\sigma^2}}$$

$$\frac{d\Gamma_\beta}{dE_e} = \frac{\bar{\sigma}}{\pi^2} N_T \sum_{i=1}^{N_\nu} |U_{ei}|^2 H(E_e, m_j)$$

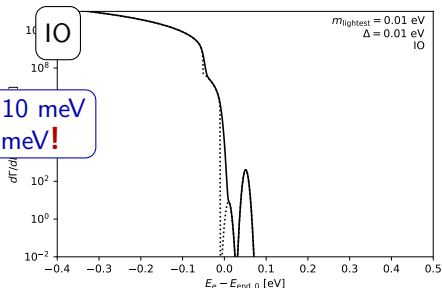
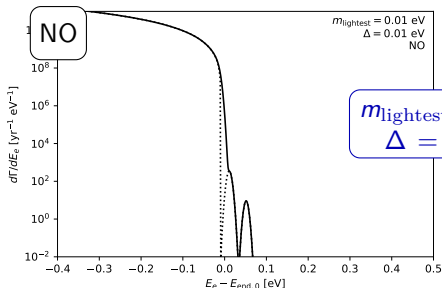
$$\frac{d\tilde{\Gamma}_\beta}{dE_e}(E_e) = \frac{1}{\sqrt{2\pi}\sigma} \int_{-\infty}^{+\infty} dx \frac{d\Gamma_\beta}{dE_e}(x) \exp\left[-\frac{(E_e - x)^2}{2\sigma^2}\right]$$

$\bar{\sigma}$  cross section,  $N_T$  number of tritium atoms in the source (PTOLEMY: 100 g),  $E_{\text{end}}$  endpoint,  $\sigma = \Delta/\sqrt{8 \ln 2}$  standard deviation

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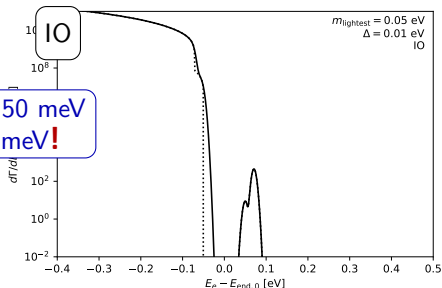
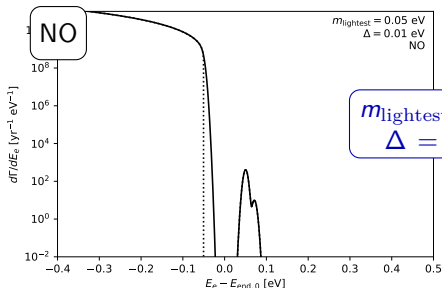
$m_{\text{lightest}} = 10 \text{ meV}$   
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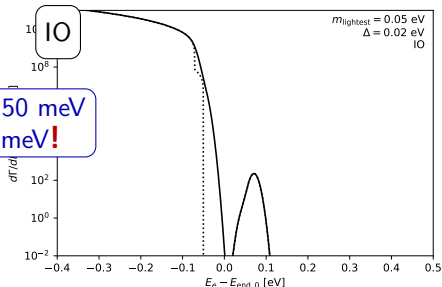
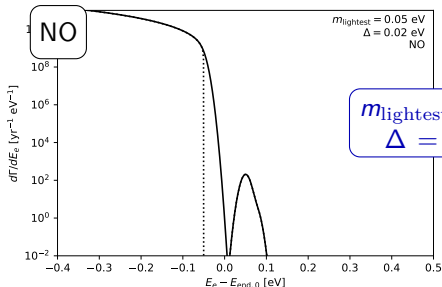
$m_{\text{lightest}} = 50 \text{ meV}$   
 $\Delta = 10 \text{ meV!}$

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$$\frac{d\tilde{\Gamma}_\beta}{dE_e}(E_e) = \frac{1}{\sqrt{2\pi}\sigma} \int_{-\infty}^{+\infty} dx \frac{d\Gamma_\beta}{dE_e}(x) \exp\left[-\frac{(E_e - x)^2}{2\sigma^2}\right]$$



$m_{\text{lightest}} = 50 \text{ meV}$   
 $\Delta = 20 \text{ meV!}$

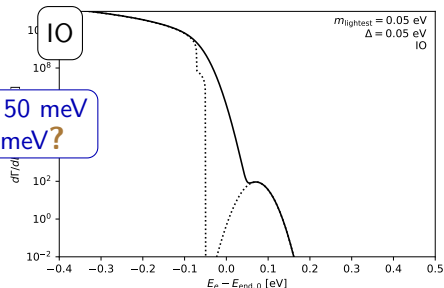
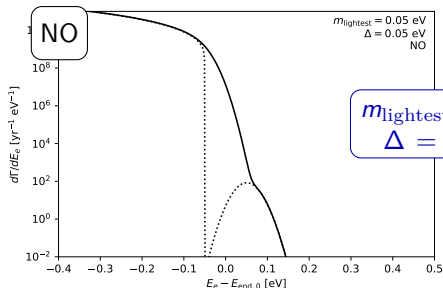
$\bar{\sigma}$  cross section,  $N_T$  number of tritium atoms in the source (PTOLEMY: 100 g),  $E_{\text{end}}$  endpoint,  $\sigma = \Delta/\sqrt{8 \ln 2}$  standard deviation

# $\beta$ and Neutrino Capture spectra

$$\frac{d\tilde{\Gamma}_{\text{CNB}}}{dE_e}(E_e) = \frac{1}{\sqrt{2\pi}\sigma} \sum_{i=1}^{N_\nu} \bar{\sigma} N_T |U_{ei}|^2 n_i \times e^{-\frac{[E_e - (E_{\text{end}} + m_j + m_{\text{lightest}})]^2}{2\sigma^2}}$$

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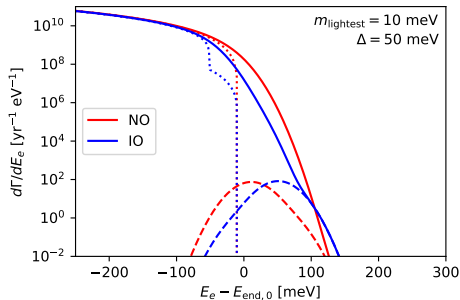
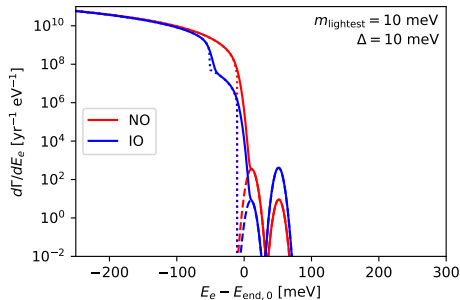
$\bar{\sigma}$  cross section,  $N_T$  number of tritium atoms in the source (PTOLEMY: 100 g),  $E_{\text{end}}$  endpoint,  $\sigma = \Delta/\sqrt{8 \ln 2}$  standard deviation



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PonTecorvo Observatory for Light, Early-universe, Massive-neutrino Yield (PTOLEMY)

expected resolution  $\Delta \simeq 0.1 \text{ eV?}$   
 $0.05 \text{ eV?}$

can probe  $m_\nu \simeq 1.4\Delta \simeq 0.1 \text{ eV}$

built mainly for CNB

$M_T = 100 \text{ g}$  of atomic  ${}^3\text{H}$

$$\Gamma_{\text{CNB}} = \sum_{i=1}^3 |U_{ei}|^2 [n_i(\nu_{h_R}) + n_i(\nu_{h_L})] N_T \bar{\sigma} \sim \mathcal{O}(10) \text{ yr}^{-1}$$

$N_T$  number of  ${}^3\text{H}$  nuclei in a sample of mass  $M_T$      $\bar{\sigma} \simeq 3.834 \times 10^{-45} \text{ cm}^2$      $n_i$  number density of neutrino  $i$

(without clustering)

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$M_T = 100 \text{ g}$  of atomic  ${}^3\text{H}$

enhancement from  
other effects?

enhancement from  
 $\nu$  clustering in the galaxy?

$$\Gamma_{\text{CNB}} = \sum_{i=1}^3 |U_{ei}|^2 [n_i(\nu_{h_R}) + n_i(\nu_{h_L})] N_T \bar{\sigma} \sim \mathcal{O}(10) \text{ yr}^{-1}$$

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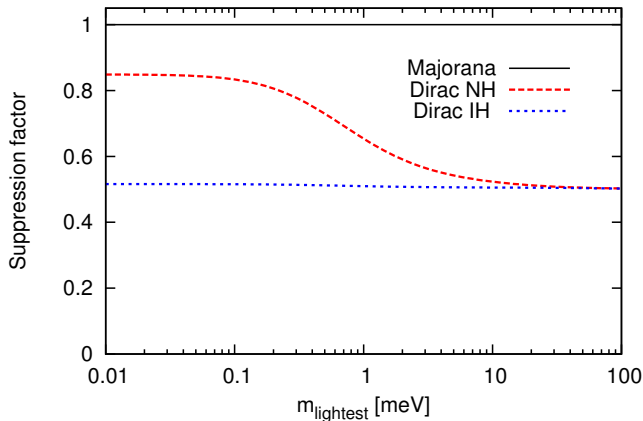
(without clustering)

direct detection through  $\nu_e + {}^3\text{H} \rightarrow e^- + {}^3\text{He}$

only neutrinos with correct chirality can be detected!

non-relativistic **Majorana** case:  $\nu$  and  $\bar{\nu}$  cannot be distinguished!

expect **more events** for the **Majorana** than for **Dirac** case



Dirac **normal**  
or **inverted**  
ordering differ  
because lighter  
 $\nu_1$  and  $\nu_2$  in **NH**  
are **relativistic**  
↓  
almost  
indistinguishable  
from **Majorana**

## 1 Cosmic Neutrino Background

## 2 Direct detection of relic neutrinos

- Some proposed methods
- Neutrino capture

## 3 Relic neutrino clustering at Earth

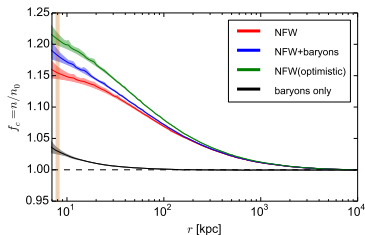
- N-one-body simulations
- Results from the Milky Way
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## 4 PTOLEMY

- The experiment
- Simulations
- Perspectives

## 5 Beyond the standard: light sterile neutrinos

## 6 Conclusions



# $\nu$ clustering with N-one-body simulations

Milky Way (MW) matter attracts neutrinos!

clustering  $\rightarrow$

$$\Gamma_{\text{CNB}} = \sum_{i=1}^3 |U_{ei}|^2 f_c(m_i) [n_{i,0}(\nu_{h_R}) + n_{i,0}(\nu_{h_L})] N_T \bar{\sigma}$$

$f_c(m_i) = n_i/n_{i,0}$  clustering factor  $\rightarrow$  How to compute it?

Idea from [Ringwald & Wong, 2004]  $\rightarrow$  **N-one-body** =  $N \times$  single  $\nu$  simulations

$\rightarrow$  each  $\nu$  evolved from initial conditions at  $z = 3$

$\rightarrow$  spherical symmetry, coordinates  $(r, \theta, p_r, l)$

$\rightarrow$  need  $\rho_{\text{matter}}(z) = \rho_{\text{DM}}(z) + \rho_{\text{baryon}}(z)$

Assumptions:

$\nu$ s are independent

only gravitational interactions

$\nu$ s do not influence matter evolution

$(\rho_\nu \ll \rho_{\text{DM}})$

how many  $\nu$ s is "N"?

$\rightarrow$  must sample all possible  $r, p_r, l$

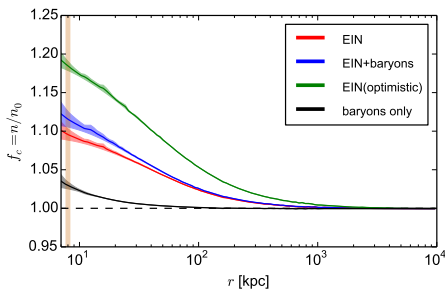
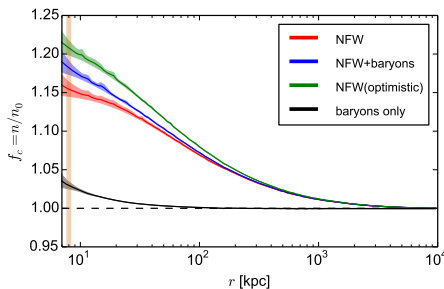
$\rightarrow$  must include all possible  $\nu$ s that reach the MW

(fastest ones may come from  
several (up to  $\mathcal{O}(100)$ ) Mpc!)

given  $N \nu$ :

$\rightarrow$  weigh each neutrinos

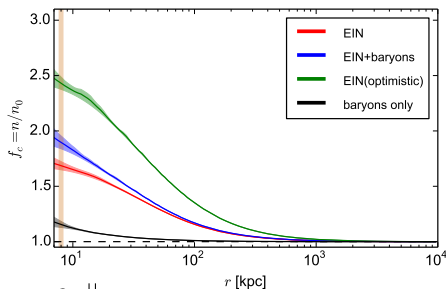
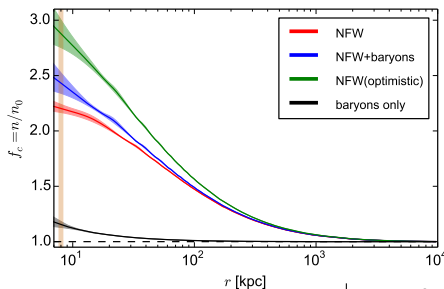
$\rightarrow$  reconstruct final density profile with kernel method from [Merritt&Tremblay, 1994]



masses	ordering	matter halo	overdensity $f_c$		$\Gamma_{\text{tot}} \text{ (yr}^{-1}\text{)}$
			$f_1 \simeq f_2$	$f_3$	
any	any	any	no clustering		4.06
$m_3 = 60 \text{ meV}$	NO	NFW(+bar)	$\sim 1$	1.15 (1.18)	4.07 (4.08)
		NFW optimistic		1.21	4.08
		EIN(+bar)		1.09 (1.12)	4.07 (4.07)
		EIN optimistic		1.18	4.08
$m_1 \simeq m_2 = 60 \text{ meV}$	IO	NFW(+bar)	1.15 (1.18)	$\sim 1$	4.66 (4.78)
		NFW optimistic	1.21		4.89
		EIN(+bar)	1.09 (1.12)		4.42 (4.54)
		EIN optimistic	1.18		4.78

ordering dependence from  $\Gamma_{\text{CNB}} = \sum_{i=1}^3 |U_{ei}|^2 f_i [n_i(\nu_{hR}) + n_i(\nu_{hL})] N_T \bar{\sigma}$

$\Rightarrow$  minimal mass detectable by PTOLEMY if  $\Delta \simeq 100\text{--}150$  meV



matter halo	overdensity $f_c$ $f_1 \simeq f_2 \simeq f_3$	$\Gamma_{\text{tot}}$ ( $\text{yr}^{-1}$ )
any	no clustering	4.06
NFW(+bar)	2.18 (2.44)	8.8 (9.9)
NFW optimistic	2.88	11.7
EIN(+bar)	1.68 (1.87)	6.8 (7.6)
EIN optimistic	2.43	9.9

no ordering dependence:  $m_1 \simeq m_2 \simeq m_3 \Rightarrow f_1 \simeq f_2 \simeq f_3$



# Additional clustering due to other galaxies

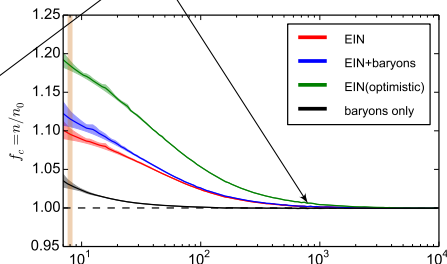
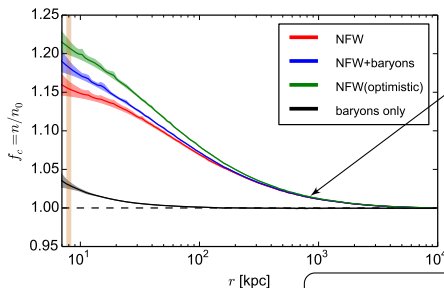
nearest galaxies: various MW satellites

with  $M_{\text{sat}} \ll M_{\text{MW}} \longrightarrow$  negligibly small  $\nu$  halo

nearest big galaxy:

Andromeda

$$M_{\text{Andromeda}} = M_{\text{MW}} \times \mathcal{O}(1) \quad - \quad d_{\text{Andromeda}} \simeq 800 \text{ kpc}$$



$m_{\text{heaviest}} \simeq 60 \text{ meV}$

$f_c$  increased of  $\lesssim 0.03$

# Additional clustering due to other galaxies

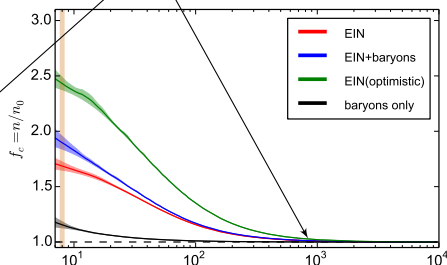
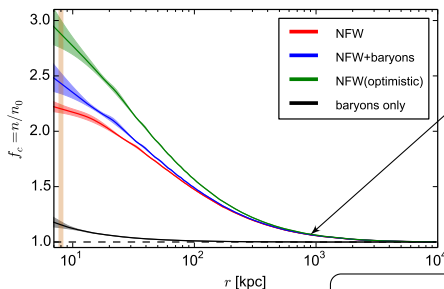
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$$M_{\text{Andromeda}} = M_{\text{MW}} \times \mathcal{O}(1) \quad - \quad d_{\text{Andromeda}} \simeq 800 \text{ kpc}$$



$m_\nu \simeq 150 \text{ meV}$

$f_c$  increased of  $\lesssim 0.1$

(halo is less diffuse for higher  $\nu$  masses)

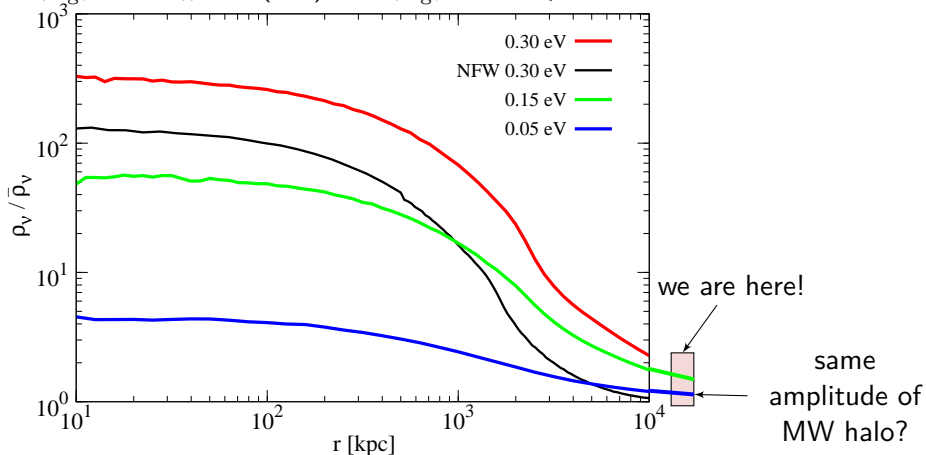
# Additional clustering due to Virgo cluster

nearest galaxy cluster:

Virgo cluster

very wide  $\nu$  halo, may reach Earth

$$M_{\text{Virgo}} = M_{\text{MW}} \times \mathcal{O}(10^3) \quad - \quad d_{\text{Virgo}} \simeq 16 \text{ Mpc}$$



[Villaescusa-Navarro et al., JCAP 1106 (2011) 027]

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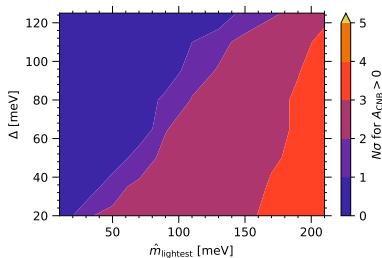
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## 4 **PTOLEMY**

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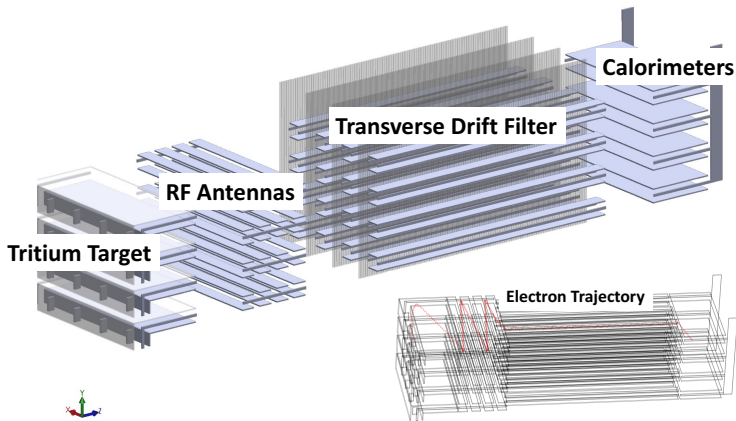
## 6 *Conclusions*



# PTOLEMY pipeline

scope of PTOLEMY:

measure electron spectrum near  ${}^3\text{H}$   $\beta$ -decay endpoint  
(same as neutrino mass experiments, e.g. KATRIN)



[PTOLEMY, arxiv:1810.06703]



## The source - graphene

source of  $^3\text{H}$  in **gas form** (KATRIN-like) has column density  $\sim 1 \mu\text{g cm}^{-2}$   
source tube is 10 m, for  $\sim \mathcal{O}(100) \mu\text{g}$  of  $^3\text{H}$

not practical solution for required 100 g of  $^3\text{H}$ !

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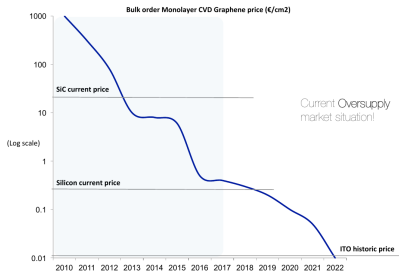
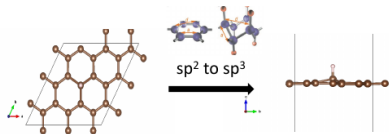
not practical solution for required 100 g of  $^3\text{H}$ !

partially existing technology: hydrogenated graphene

layers

Graphene layers are cheap  
(commercial use in displays)

hydrogenation under study  
at Princeton



[courtesy A.Zurutuza (Graphenea)]





# MAC-E filter

Background flux is too high for microcalorimeter. Must be reduced!

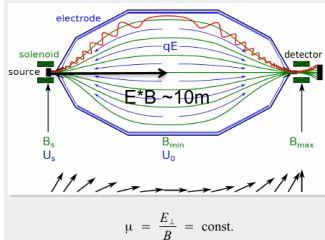
Magnetic Adiabatic Collimation with Electrostatic filter

[KATRIN]

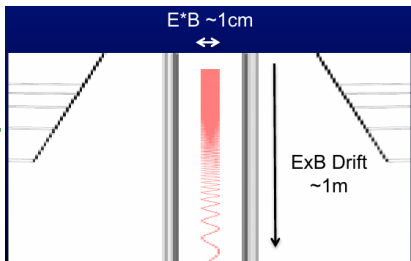
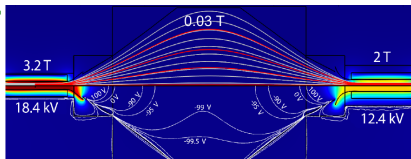


MAC-E filter technique

Magnetic Adiabatic Collimation with Electrostatic filter  
Picard et al., NIM B63 (1992) 345



[PTOLEMY]:  $E \times B$  filter  
(must enter in GS labs)



see also [PTOLEMY, arxiv:1810.06703]

[courtesy C. Tully]

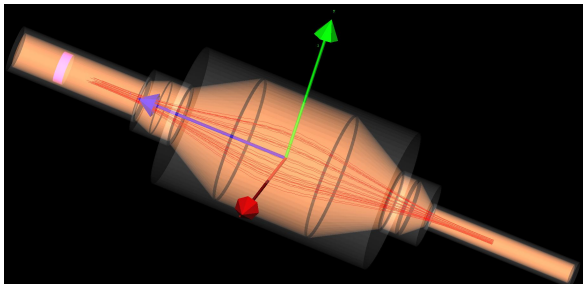
## RF tracking

first energy determination with

RadioFrequency trigger, using  
Cyclotron Radiation Emission Spectroscopy (CRES)

see also [Project 8, JPG 44 (2017) 054004]

can RF antenna be integrated in the MAC-E filter?



## Final energy determination with TES

Final energy determination needs  $\sigma_E \simeq 0.1$  eV or less!

Microcalorimetry with **T**ransition-**E**dge **S**ensors

TES: “A microcalorimeter  
made by a superconducting film  
operated in the temperature region  
between the normal and the superconducting state”

↙  
difficult readout

↘  
difficult temperature control

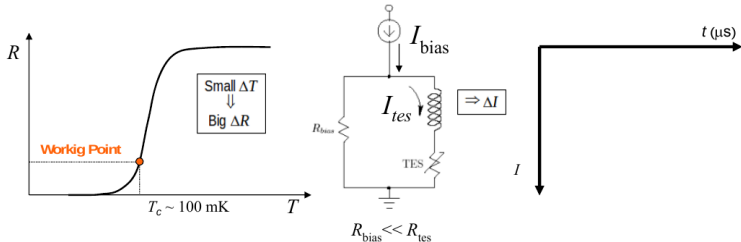
Same technology as in HOLMES experiment ( $\nu$  masses)

# Final energy determination with TES

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Microcalorimetry with **T**ransition-**E**dge **S**ensors

[courtesy M.Ratjeri]

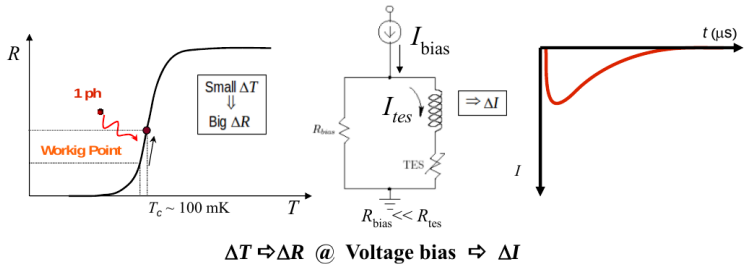


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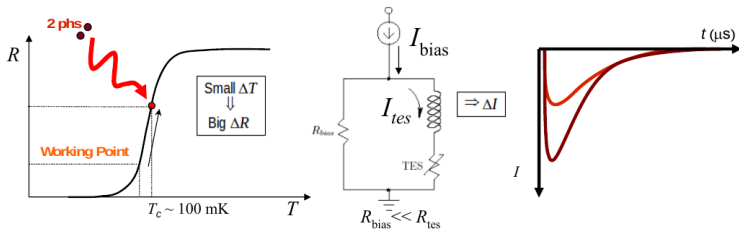


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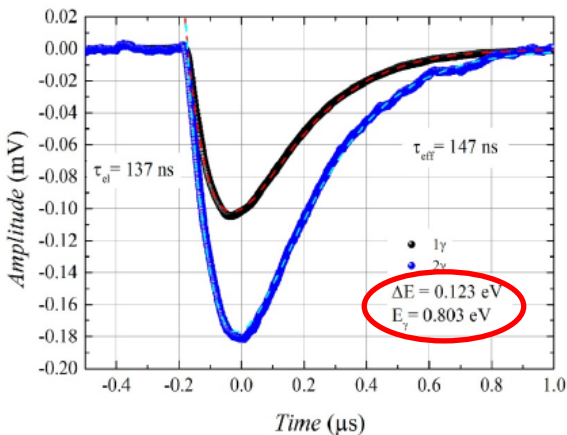
$$\Delta T \Leftrightarrow \Delta R \text{ @ Voltage bias } \Leftrightarrow \Delta I$$

# Final energy determination with TES

Final energy determination needs  $\sigma_E \simeq 0.1$  eV or less!

Microcalorimetry with **T**ransition-**E**dge **S**ensors

[courtesy M.Ratjeri]



Events in **bin**  $i$ , centered at  $E_i$ :

$$N_{\beta}^i = T \int_{E_i - \Delta/2}^{E_i + \Delta/2} \frac{d\tilde{\Gamma}_{\beta}}{dE_e} dE_e$$

$$N_{\text{CNB}}^i = T \int_{E_i - \Delta/2}^{E_i + \Delta/2} \frac{d\tilde{\Gamma}_{\text{CNB}}}{dE_e} dE_e$$

**fiducial** number of events:  $\hat{N}^i = N_{\beta}^i(\hat{E}_{\text{end}}, \hat{m}_i, \hat{U}) + N_{\text{CNB}}^i(\hat{E}_{\text{end}}, \hat{m}_i, \hat{U})$

add **background**  $\hat{N}_b = \hat{\Gamma}_b T$   
with  $\hat{\Gamma}_b \simeq 10^{-5}$  Hz

$$\longrightarrow \boxed{N_t^i = \hat{N}^i + \hat{N}_b}$$

$T$  exposure time –  $(\hat{E}_{\text{end}}, \hat{m}_i, \hat{U})$  fiducial endpoint energy, masses, mixing matrix –  $\theta = (A_{\beta}, N_b, \Delta E_{\text{end}}, A_{\text{CNB}}, m_i, U)$



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simulated **experimental** spectrum:

$$N_{\text{exp}}^i(\hat{E}_{\text{end}}, \hat{m}_i, \hat{U}) = N_t^i \pm \sqrt{N_t^i}$$

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$$\longrightarrow N_t^i = \hat{N}^i + \hat{N}_b$$

simulated **experimental** spectrum:

$$N_{\text{exp}}^i(\hat{E}_{\text{end}}, \hat{m}_i, \hat{U}) = N_t^i \pm \sqrt{N_t^i}$$

repeat for **theory** spectrum, free **amplitudes** and **endpoint position**:

$$N_{\text{th}}^i(\theta) = \mathbf{A}_{\beta} N_{\beta}^i(\hat{E}_{\text{end}} + \Delta \mathbf{E}_{\text{end}}, m_i, U) + \mathbf{A}_{\text{CNB}} N_{\text{CNB}}^i(\hat{E}_{\text{end}} + \Delta \mathbf{E}_{\text{end}}, m_i, U) + N_b$$

$T$  exposure time –  $(\hat{E}_{\text{end}}, \hat{m}_i, \hat{U})$  fiducial endpoint energy, masses, mixing matrix –  $\theta = (A_{\beta}, N_b, \Delta \mathbf{E}_{\text{end}}, A_{\text{CNB}}, m_i, U)$

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$$N_{\text{exp}}^i(\hat{E}_{\text{end}}, \hat{m}_i, \hat{U}) = N_t^i \pm \sqrt{N_t^i}$$

repeat for **theory** spectrum, free **amplitudes** and **endpoint position**:

$$N_{\text{th}}^i(\theta) = \mathbf{A}_{\beta} N_{\beta}^i(\hat{E}_{\text{end}} + \Delta \mathbf{E}_{\text{end}}, m_i, U) + \mathbf{A}_{\text{CNB}} N_{\text{CNB}}^i(\hat{E}_{\text{end}} + \Delta \mathbf{E}_{\text{end}}, m_i, U) + N_b$$

fit  $\longrightarrow$

$$\chi^2(\theta) = \sum_i \left( \frac{N_{\text{exp}}^i(\hat{E}_{\text{end}}, \hat{m}_i, \hat{U}) - N_{\text{th}}^i(\theta)}{\sqrt{N_t^i}} \right)^2$$

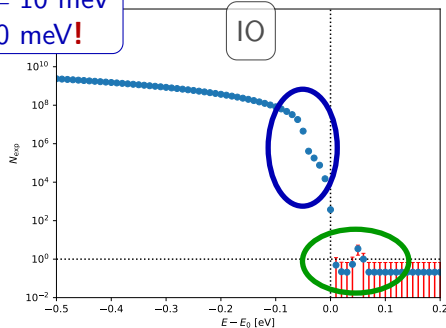
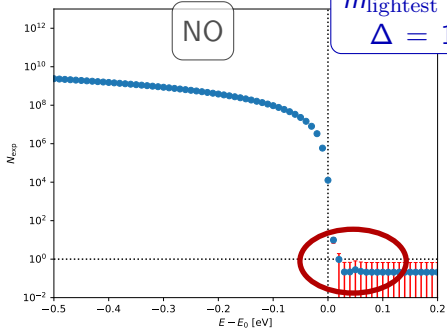
or  $\log \mathcal{L} = -\frac{\chi^2}{2}$

$T$  exposure time –  $(\hat{E}_{\text{end}}, \hat{m}_i, \hat{U})$  fiducial endpoint energy, masses, mixing matrix –  $\theta = (A_{\beta}, N_b, \Delta \mathbf{E}_{\text{end}}, A_{\text{CNB}}, m_i, U)$

# Simulations - II

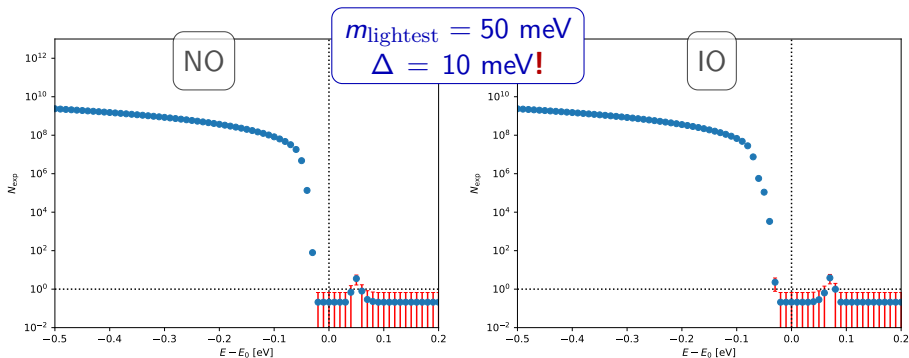
no random noise?

$m_{\text{lightest}} = 10 \text{ meV}$   
 $\Delta = 10 \text{ meV!}$



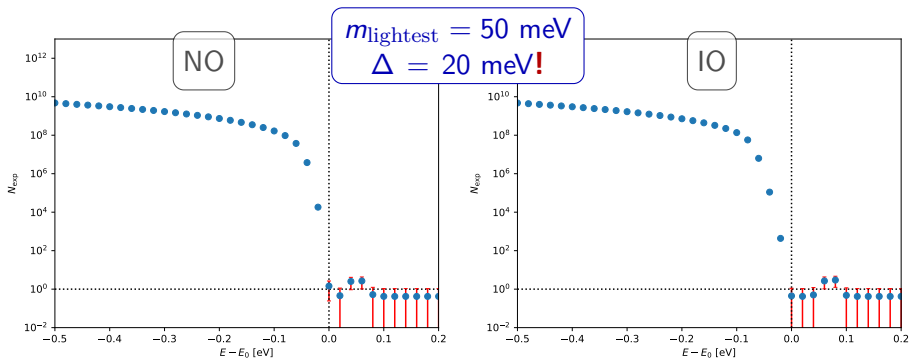
1 year of observation with 100 g of T source

no random noise?



1 year of observation with 100 g of T source

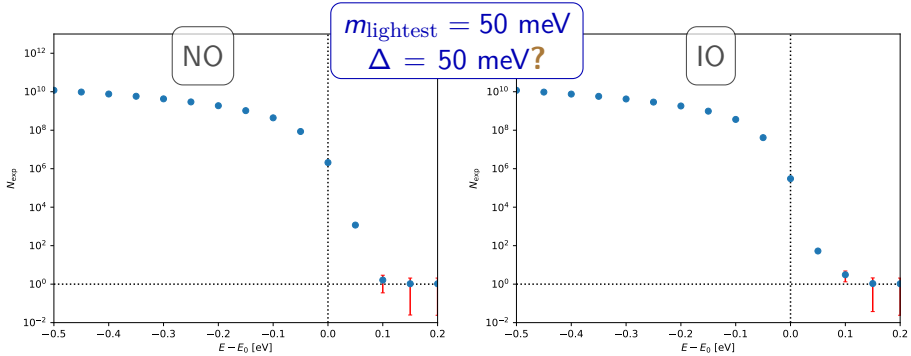
no random noise?



1 year of observation with 100 g of T source

# Simulations - II

no random noise?

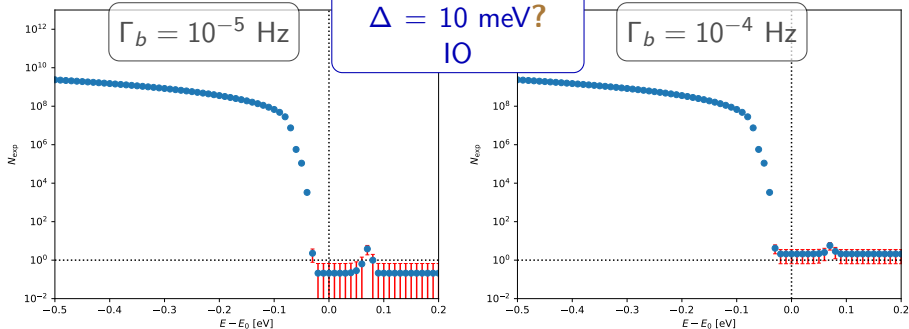


1 year of observation with 100 g of T source

# Simulations - II

no random noise?

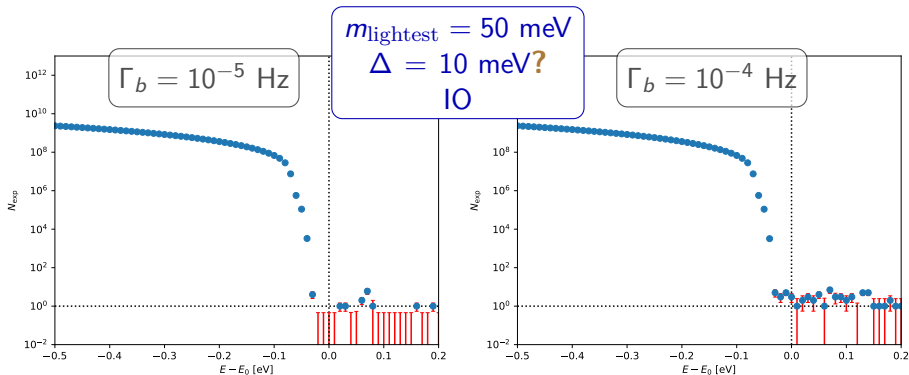
$m_{\text{lightest}} = 50 \text{ meV}$   
 $\Delta = 10 \text{ meV?}$   
IO



1 year of observation with 100 g of T source



with random noise!



things are more complicated in this way...low background needed!

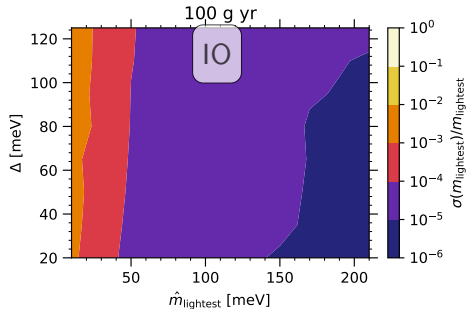
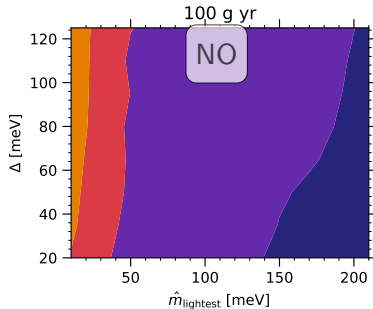
1 year of observation with 100 g of T source

statistical only!

relative error on  $m_{\text{lightest}}$   
as a function of  $\hat{m}_{\text{lightest}}$ ,  $\Delta$

statistical only!

relative error on  $m_{\text{lightest}}$   
as a function of  $\hat{m}_{\text{lightest}}$ ,  $\Delta$

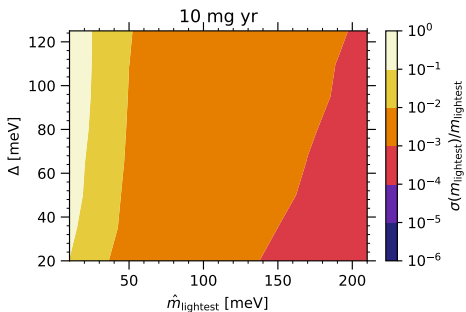
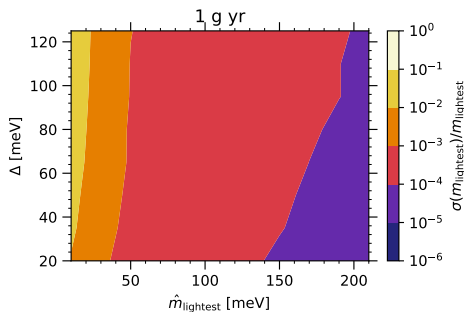


wonderful precision in determining the neutrino mass

(well, yes, with 100 g of tritium...)

statistical only!

relative error on  $m_{\text{lightest}}$   
as a function of  $\hat{m}_{\text{lightest}}$ ,  $\Delta$

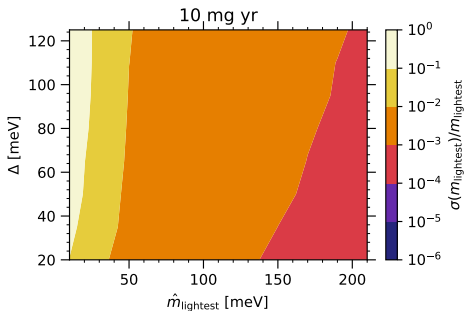
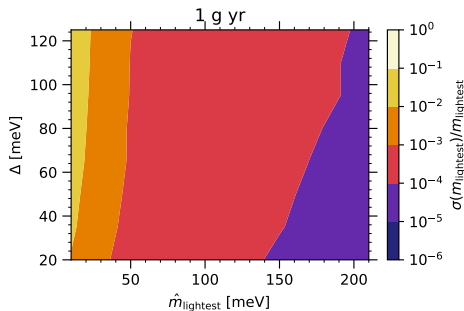


wonderful precision in determining the neutrino mass

(mass detection already with 10 mg of tritium!)

statistical only!

relative error on  $m_{\text{lightest}}$   
as a function of  $\hat{m}_{\text{lightest}}$ ,  $\Delta$



wonderful precision in determining the neutrino mass

(mass detection already with 10 mg of tritium!)

$\Delta$  has almost no impact

Bayesian method:

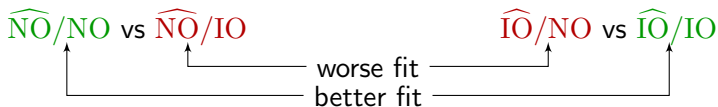
Fit fiducial ordering ( $\widehat{NO}$  or  $\widehat{IO}$ ) using both **correct** and **wrong** ordering

$\widehat{NO}/NO$  vs  $\widehat{NO}/IO$

$\widehat{IO}/NO$  vs  $\widehat{IO}/IO$

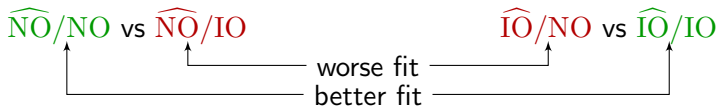
Bayesian method:

Fit fiducial ordering ( $\widehat{NO}$  or  $\widehat{IO}$ ) using both **correct** and **wrong** ordering



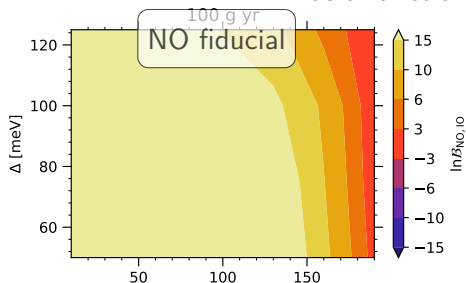
Bayesian method:

Fit fiducial ordering ( $\widehat{NO}$  or  $\widehat{IO}$ ) using both **correct** and **wrong** ordering



statistical only!

(Bayesian) preference on  $m_{\text{lightest}}$   
as a function of  $\hat{m}_{\text{lightest}}, \Delta$



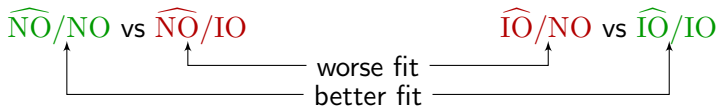
IO fiducial

always strong significance



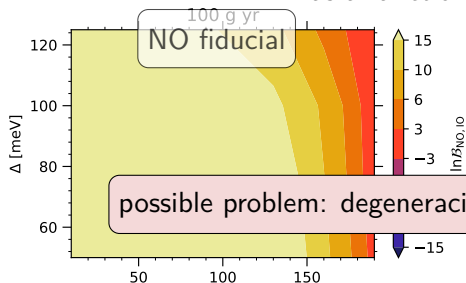
Bayesian method:

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statistical only!

(Bayesian) preference on  $m_{\text{lightest}}$   
as a function of  $\hat{m}_{\text{lightest}}, \Delta$



always strong significance

possible problem: degeneracies between  $m_{\text{lightest}}$  and  $\Delta m_{31}^2$

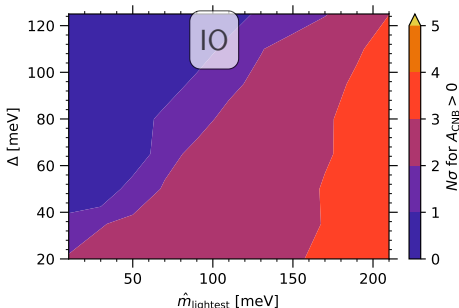
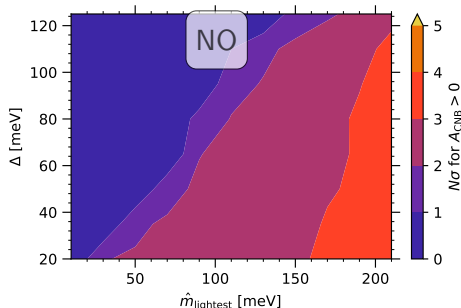
using the definition:

$$N_{\text{th}}^i(\theta) = A_{\beta} N_{\beta}^i(\hat{E}_{\text{end}} + \Delta E_{\text{end}}, m_i, U) + \mathbf{A}_{\text{CNB}} N_{\text{CNB}}^i(\hat{E}_{\text{end}} + \Delta E_{\text{end}}, m_i, U) + N_b$$

if  $\mathbf{A}_{\text{CNB}} > 0$  at  $N\sigma$ , direct detection of CNB accomplished at  $N\sigma$

statistical only!

significance on  $A_{\text{CNB}} > 0$   
as a function of  $\hat{m}_{\text{lightest}}, \Delta$



# Requirements for PTOLEMY discoveries

What do we need to discover...

	low $\Gamma_b$	extreme $\Delta$	a lot of ${}^3\text{H}$
... $\nu$ masses?	✗	✗	?
... $\nu$ mass ordering?	✗	?	?
... CNB direct detection?	✓	✓	✓

✓: strongly required

?: not so strongly required

✗: loosely required

## 1 *Cosmic Neutrino Background*

## 2 *Direct detection of relic neutrinos*

- Some proposed methods
- Neutrino capture

## 3 *Relic neutrino clustering at Earth*

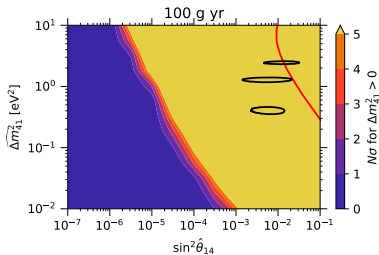
- N-one-body simulations
- Results from the Milky Way
- Systematics and future developments

## 4 *PTOLEMY*

- The experiment
- Simulations
- Perspectives

## 5 *Beyond the standard: light sterile neutrinos*

## 6 *Conclusions*



Problem: **anomalies**  
in SBL experiments

→ { errors in flux calculations?  
deviations from 3- $\nu$  description?

A short review:

**LSND** search for  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ , with  $L/E = 0.4 \div 1.5$  m/MeV. Observed a  $3.8\sigma$  excess of  $\bar{\nu}_e$  events [Aguilar et al., 2001]

**Reactor** re-evaluation of the expected anti-neutrino flux  $\Rightarrow$  disappearance of  $\bar{\nu}_e$  events compared to predictions ( $\sim 3\sigma$ ) with  $L < 100$  m [Mention et al, 2011], [Azabajan et al, 2012]

**Gallium** calibration of GALLEX and SAGE Gallium solar neutrino experiments give a  $2.7\sigma$  anomaly (disappearance of  $\nu_e$ ) [Giunti, Laveder, 2011]

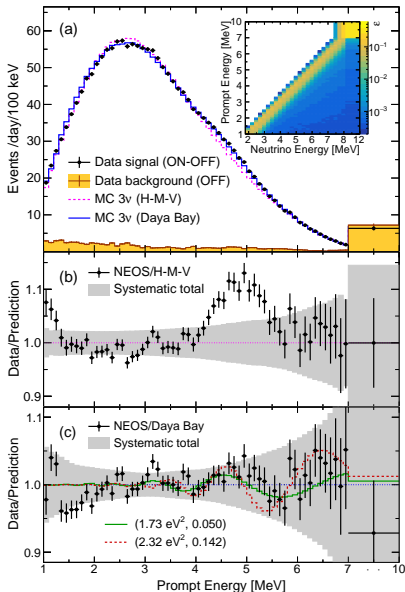
MiniBooNE

See next

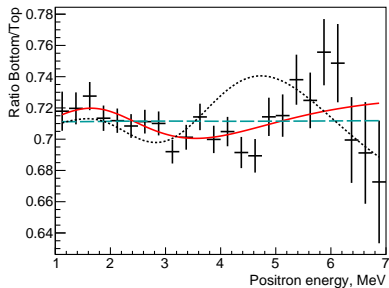
Possible explanation:

Additional squared mass  
difference  $\Delta m_{\text{SBL}}^2 \simeq 1 \text{ eV}^2$

[NEOS, PRL 118 (2017) 121802]



[DANSS, PLB 787 (2018) 56]

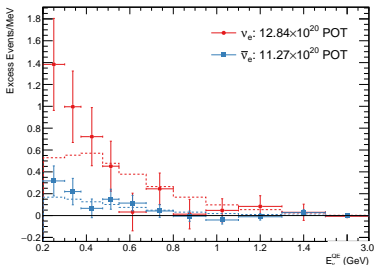
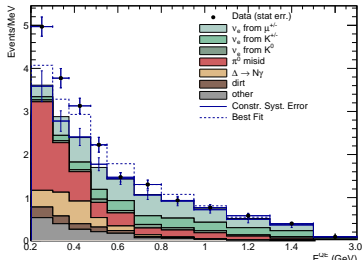


first *model independent* indications in favor of SBL oscillations

DANSS alone gives a  $\Delta\chi^2 \simeq 13$  in favor of a light sterile neutrino!

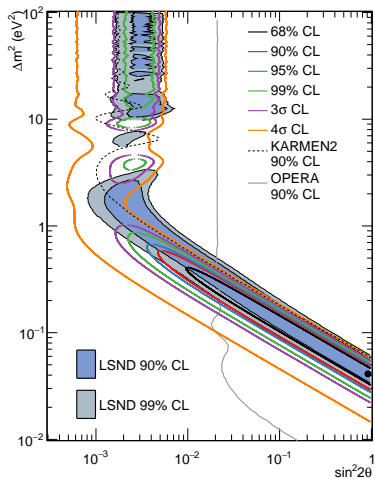
# Recent results...

[MiniBooNE, PRL  
121 (2018) 221801]



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121 (2018) 221801]

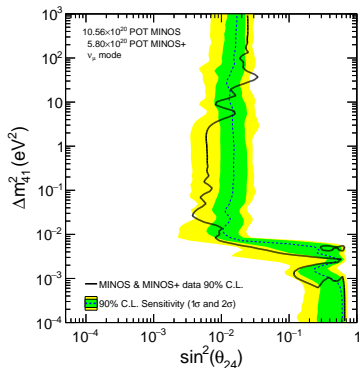
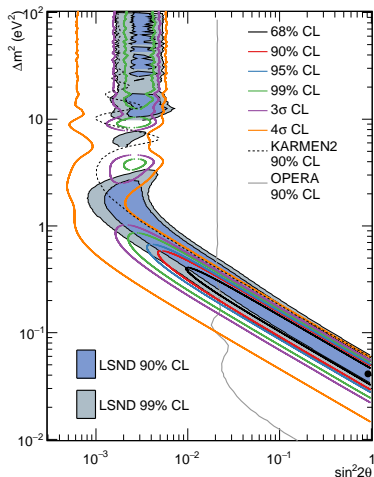




# Recent results...

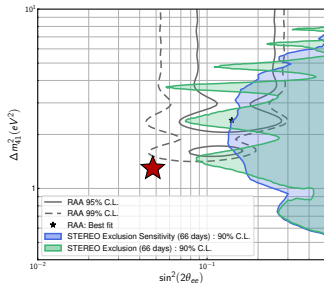
[MiniBooNE, PRL  
121 (2018) 221801]

[MINOS+, PRL  
122 (2019) 091803]

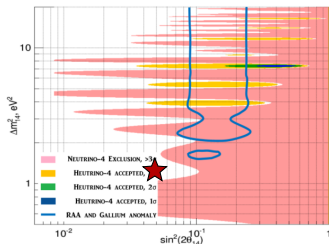


# More to come...

[STEREO, PRL 121 (2018) 161801]

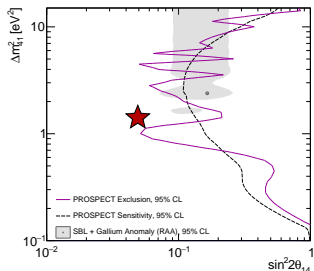


[Neutrino-4, arxiv:1809.10561]

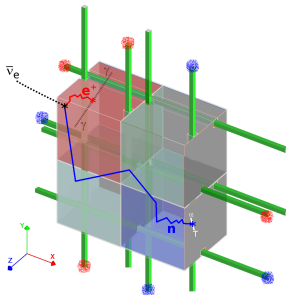


★ = current DANSS+NEOS best fit  
 [SG et al., PLB 782 (2018) 13]

[PROSPECT, PRL 121 (2018) 251802]



[SoLiD, JINST 13 (2018) P09005]



# 3+1 Neutrino Model

new  $\Delta m_{\text{SBL}}^2 \Rightarrow 4$  neutrinos!

$\nu_4$  with  $m_4 \simeq 1$  eV,  
no weak interactions

light sterile neutrino (LS $\nu$ )

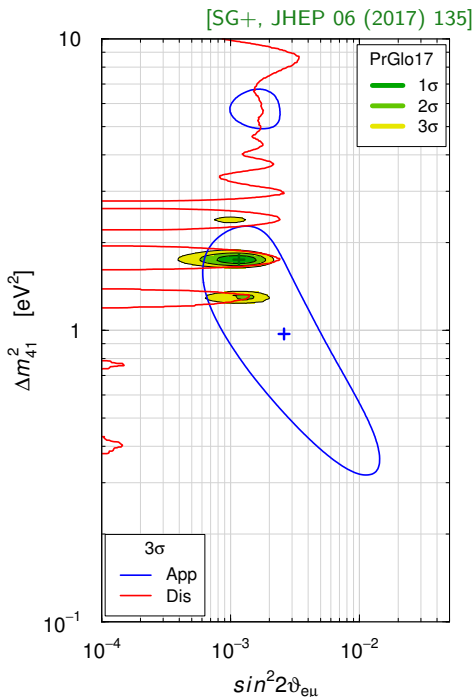
3 (active) + 1 (sterile) mixing:

$$\nu_\alpha = \sum_{k=1}^{3+1} U_{\alpha k} \nu_k \quad (\alpha = e, \mu, \tau, s)$$

$\nu_s$  is mainly  $\nu_4$ :

$$m_s \simeq m_4 \simeq \sqrt{\Delta m_{41}^2} \simeq \sqrt{\Delta m_{\text{SBL}}^2}$$

assuming  $m_4 \gg m_i$  ( $i = 1, 2, 3$ )



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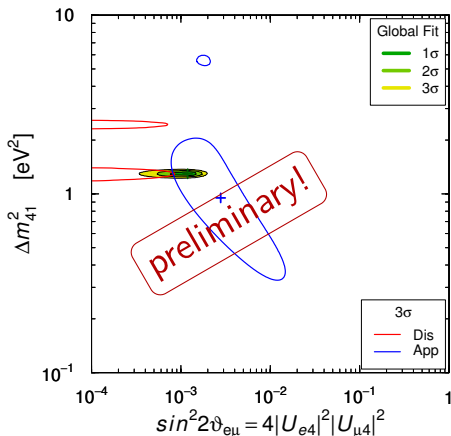
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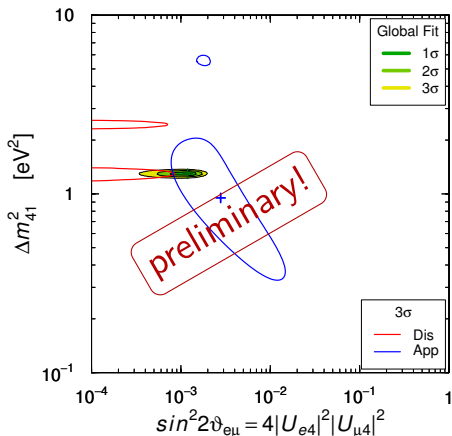
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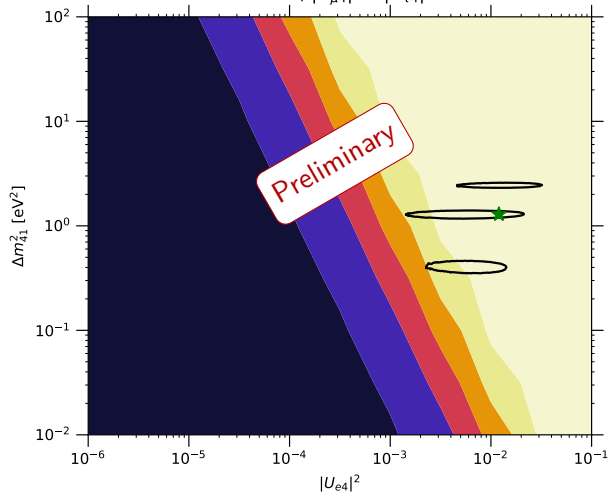
can  $\nu_4$  thermalize in the early  
Universe through oscillations?

# LS $\nu$ thermalization

Compute oscillations in early universe,  
varying  $\Delta m_{41}^2$ ,  $|U_{e4}|^2$ , here fix  $|U_{\mu 4}|^2 = |U_{\tau 4}|^2 = 0$ :

[SG+, in preparation]

active NO,  $|U_{\mu 4}|^2 = |U_{\tau 4}|^2 = 0$



**black line, green**

star:  $3\sigma$  region  
and best fit from  
DANSS+NEOS

[Gariazzo+, 2018]

Note:

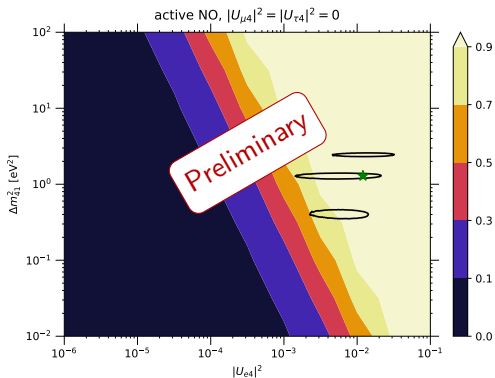
the three  $|U_{\alpha 4}|^2$   
are **NOT** equivalent  
in the thermalization  
process!

# LS $\nu$ thermalization

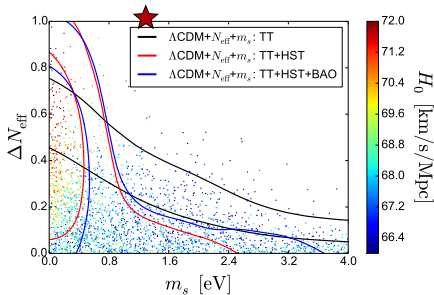
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[SG+, in preparation]

[Archidiacono+, JCAP 08 (2016) 067]



but cosmological fits give:

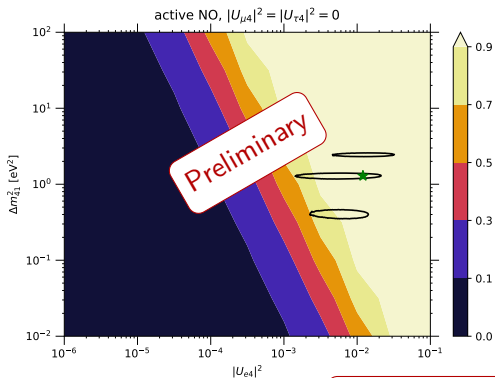


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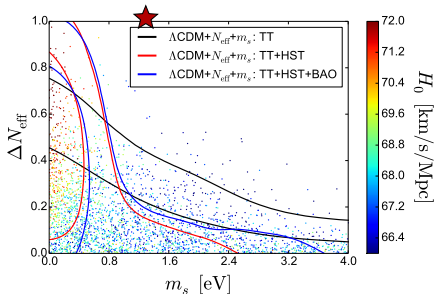
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[SG+, in preparation]

[Archidiacono+, JCAP 08 (2016) 067]



but cosmological fits give:



$\Delta N_{\text{eff}} = 1$  disfavoured!

if LS $\nu$  confirmed, we need new physics to reduce  $N_{\text{eff}}$



# Assumptions and useful equations

We assume possible  
incomplete thermalization

(due to some  
unknown new physics)

$$f_4(p) = \frac{\Delta N_{\text{eff}}}{e^{p/T_\nu} + 1} = \Delta N_{\text{eff}} f_{\text{active}}(p)$$

$$\Delta N_{\text{eff}} = \left[ \frac{1}{\pi^2} \int dp p^3 f_4(p) \right] / \left[ \frac{7}{8} \frac{\pi^2}{15} T_\nu^4 \right]$$

$$\bar{n}_4 = \frac{g_4}{(2\pi)^3} \int f_4(p) p^2 dp = n_0 \Delta N_{\text{eff}}$$

$$n_4 = n_0 \Delta N_{\text{eff}} f_c(m_4)$$

( $f_c(m_4)$  is independent of  $\Delta N_{\text{eff}}$ )

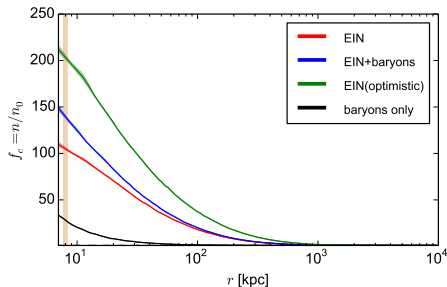
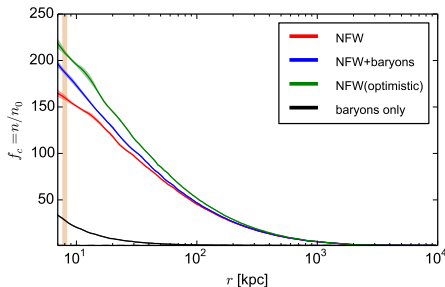
$$\Gamma_4 \simeq |U_{e4}|^2 \Delta N_{\text{eff}} f_c(m_4) \Gamma_{C\nu B}$$

(from global fit [SG et al., 2017]:  $m_4 \simeq 1.3$  eV,  $|U_{e4}|^2 \simeq 0.02$ )

# Overdensity of a sterile neutrino

$$\Gamma_4 \simeq \Delta N_{\text{eff}} |U_{e4}|^2 f_c(m_4) \Gamma_{C\nu B}$$

$$m_4 \simeq 1.3 \text{ eV}, |U_{e4}|^2 \simeq 0.02$$



matter halo	overdensity $f_4$	$\Delta N_{\text{eff}}$	$\Gamma_{\text{tot}}$ ( $\text{yr}^{-1}$ )
NFW(+bar)	159.9 (187.3)	0.2	2.6 (3.0)
		1.0	13.0 (15.2)
NFW optimistic	208.6	0.2	3.4
		1.0	16.9
EIN(+bar)	105.1 (139.5)	0.2	1.7 (2.3)
		1.0	8.5 (11.3)
EIN optimistic	203.5	0.2	3.3
		1.0	16.5

$$\Gamma_{C\nu B} = \mathcal{O}(10)/\text{yr}$$

$$\Gamma_4 \simeq \Delta N_{\text{eff}} |U_{e4}|^2 f_c(m_4) \Gamma_{\text{CNB}}$$

[SG+, PLB 782 (2018)]

$$\Delta N_{\text{eff}} = ??$$

[de Salas+, 2017]

$$f_c(m_4) = \mathcal{O}(10^2)$$

$$m_4 \simeq 1.15 \text{ eV}$$

$$|U_{e4}|^2 \simeq 0.01$$

$\Gamma_4$  depends probably on new physics!

$$\Gamma_{C\nu B} = \mathcal{O}(10)/\text{yr}$$

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[SG+, PLB 782 (2018)]

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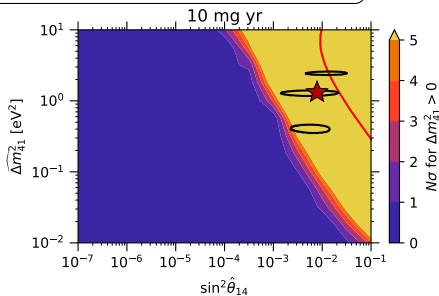
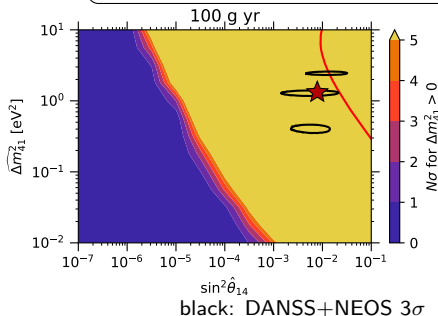
$$f_c(m_4) = \mathcal{O}(10^2)$$

$$m_4 \simeq 1.15 \text{ eV}$$

$$|U_{e4}|^2 \simeq 0.01$$

$\Gamma_4$  depends probably on new physics!

Still possible to measure mass/mixing through  $\beta$  spectrum



red: KATRIN 90% forecast

## 1 *Cosmic Neutrino Background*

## 2 *Direct detection of relic neutrinos*

- Some proposed methods
- Neutrino capture

## 3 *Relic neutrino clustering at Earth*

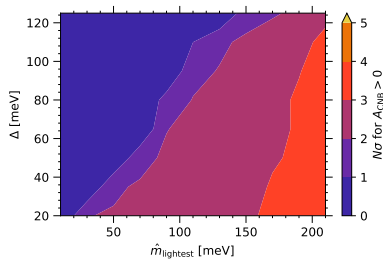
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## 4 *PTOLEMY*

- The experiment
- Simulations
- Perspectives

## 5 *Beyond the standard: light sterile neutrinos*

## 6 *Conclusions*



# Conclusions

1

amazing (neutrino) science  
with **direct detection**  
of relic neutrinos (e.g. PTOLEMY)

[non-relativistic regime, masses, ordering?, MW structure?, Dirac/Majorana?, ...]

2

But it will be a **technological challenge!**  
( $^3\text{H}$  amount, low background, energy resolution, ...)

3

possible event rate **enhancement**  
due to clustering in the Milky Way:  
should also include **nearby galaxies/clusters!**

# Conclusions

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But it will be a **technological challenge!**  
( $^3\text{H}$  amount, low background, energy resolution, ...)

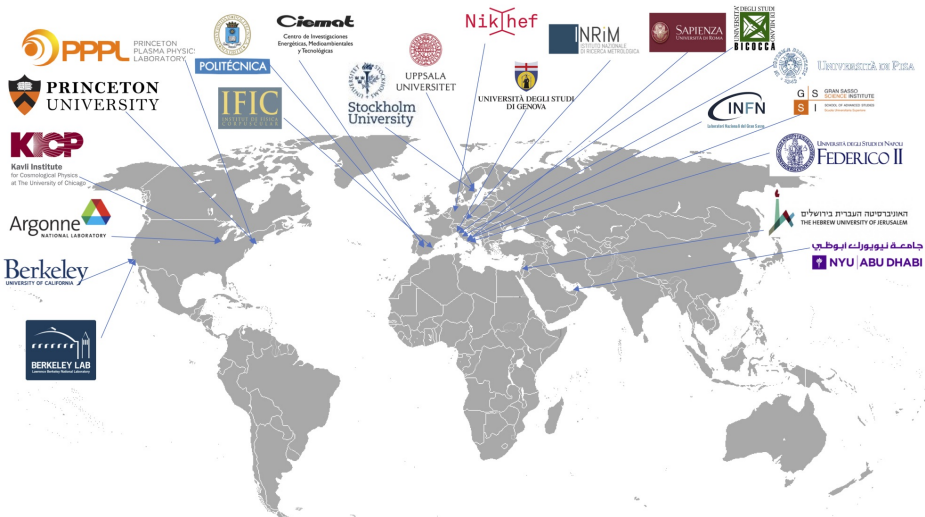
3

possible event rate **enhancement**  
due to clustering in the Milky Way:  
should also include **nearby galaxies/clusters!**

+1

**light sterile neutrino** ( $m_4 \simeq 1.15 \text{ eV}$ ) ??  
**possible detection** thanks to  $\beta$  decay spectrum

# PTOLEMY collaboration



Thank you for the attention!