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## Relic neutrinos: clustering and consequences for direct detection

*Featuring “Milky Way” & friends*

EPS-HEP 2019, Ghent (BE), 10–17/07/2019

## 1 Introduction

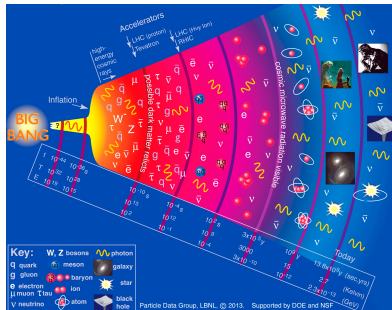
- Neutrinos and early Universe
- Relic neutrino capture

## 2 Neutrino clustering

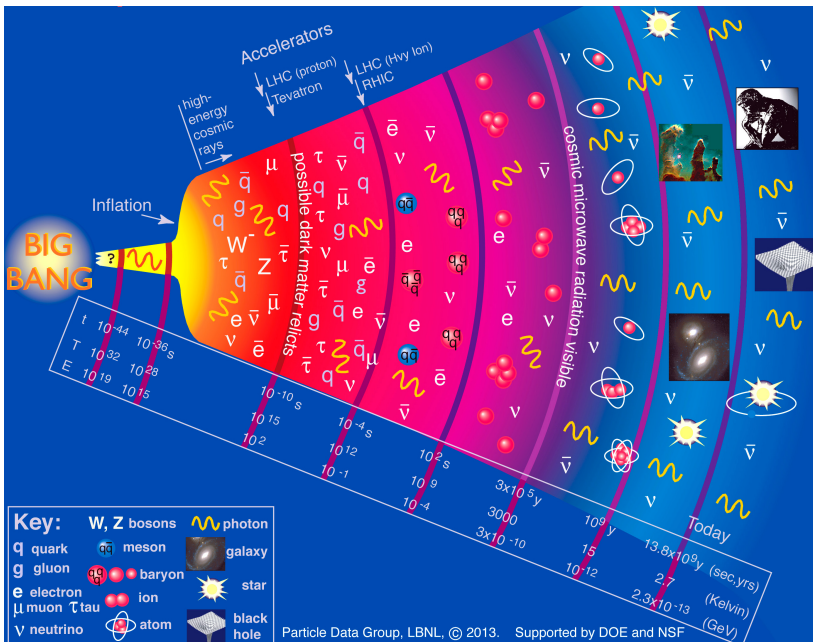
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- Beyond the Milky Way

## 3 Direct detection of relic neutrinos

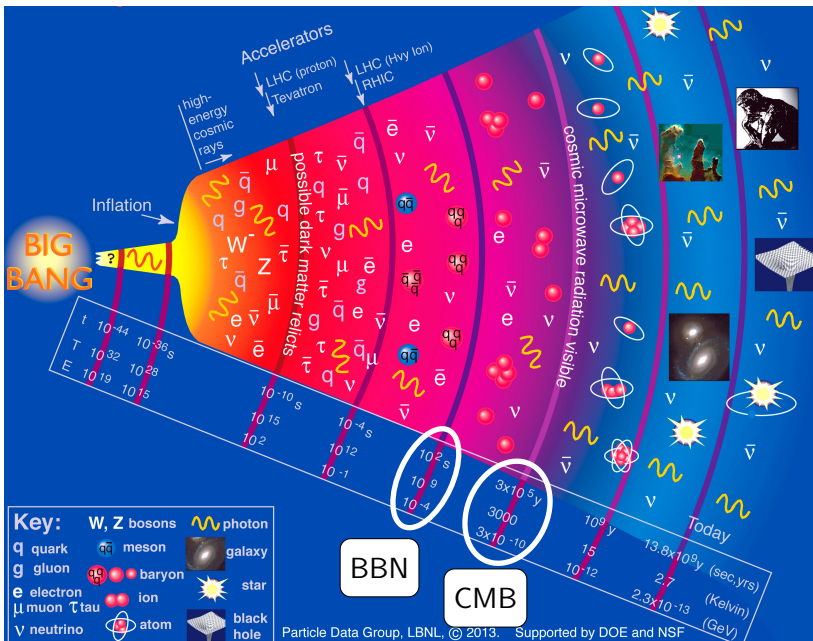
## 4 Conclusions



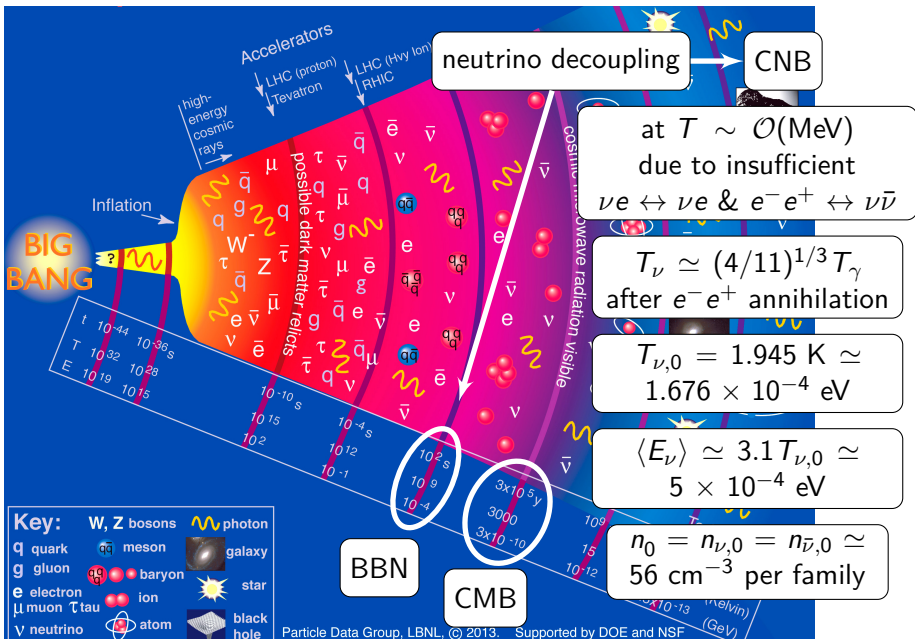
# History of the universe



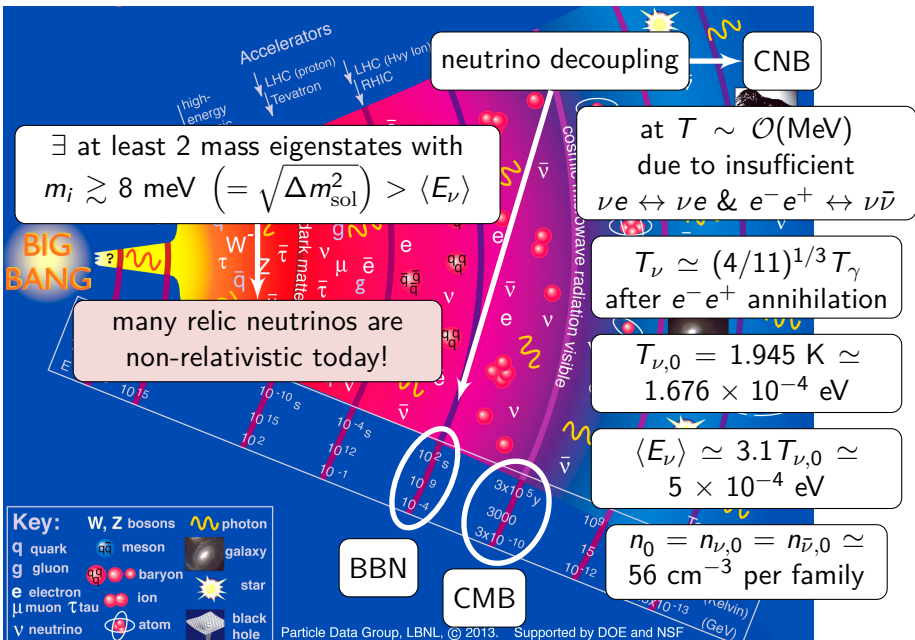
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# History of the universe



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## Relic neutrinos in cosmology: $N_{\text{eff}}$

Radiation energy density  $\rho_r$  in the early Universe:

$$\rho_r = \left[ 1 + \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} N_{\text{eff}} \right] \rho_\gamma = [1 + 0.2271 N_{\text{eff}}] \rho_\gamma$$

$\rho_\gamma$  photon energy density,  $7/8$  is for fermions,  $(4/11)^{4/3}$  due to photon reheating after neutrino decoupling

- $N_{\text{eff}} \rightarrow$  all the radiation contribution not given by photons
- $N_{\text{eff}} \simeq 1$  correspond to a single family of active neutrino, in equilibrium in the early Universe
- Active neutrinos:  
 $N_{\text{eff}} = 3.046$  [Mangano et al., 2005] (damping factors approximations)  $\sim$   
 $N_{\text{eff}} = 3.045$  [de Salas et al., 2016] (full collision terms)  
due to not instantaneous decoupling for the neutrinos
- + Non Standard Interactions:  $3.040 < N_{\text{eff}} < 3.059$  [de Salas et al., 2016]

Observations:  $N_{\text{eff}} \simeq 3.0 \pm 0.2$  [Planck 2018]  
Indirect probe of cosmic neutrino background!

$\gg 10\sigma!$

How to directly detect non-relativistic neutrinos?

Remember that  
 $\langle E_\nu \rangle \simeq \mathcal{O}(10^{-4})$  eV today



a process without energy  
 threshold is necessary

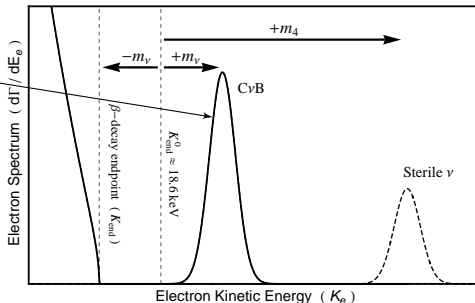
[Weinberg, 1962]: neutrino capture in  $\beta$ -decaying nuclei  $\nu + n \rightarrow p + e^-$

Main background:  $\beta$  decay  $n \rightarrow p + e^- + \bar{\nu}$ !

signal is a peak at  $2m_\nu$   
 above  $\beta$ -decay endpoint

only with a lot of material

need a very good energy resolution





PonTecorvo Observatory for Light, Early-universe, Massive-neutrino Yield (PTOLEMY)

expected resolution  $\Delta \simeq 0.1 \text{ eV?}$   
 $0.05 \text{ eV?}$

can probe  $m_\nu \simeq 1.4\Delta \simeq 0.1 \text{ eV}$

built mainly for CNB

$M_T = 100 \text{ g}$  of atomic  $^3\text{H}$

$$\Gamma_{\text{CNB}} = \sum_{i=1}^3 |U_{ei}|^2 [n_i(\nu_{h_R}) + n_i(\nu_{h_L})] N_T \bar{\sigma} \sim \mathcal{O}(10) \text{ yr}^{-1}$$

$N_T$  number of  $^3\text{H}$  nuclei in a sample of mass  $M_T$      $\bar{\sigma} \simeq 3.834 \times 10^{-45} \text{ cm}^2$      $n_i$  number density of neutrino  $i$

(without clustering)

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enhancement from  
 $\nu$  clustering in the galaxy?

enhancement from  
other effects?

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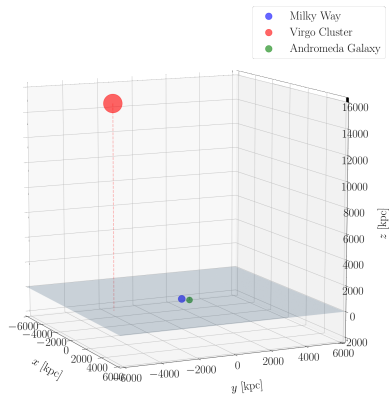
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## 4 *Conclusions*



# $\nu$ clustering with N-one-body simulations

Milky Way (MW) matter attracts neutrinos!

clustering →

$$\Gamma_{\text{CNB}} = \sum_{i=1}^3 |U_{ei}|^2 f_c(m_i) [n_{i,0}(\nu_{h_R}) + n_{i,0}(\nu_{h_L})] N_T \bar{\sigma}$$

$f_c(m_i) = n_i/n_{i,0}$  clustering factor → How to compute it?

Idea from [Ringwald & Wong, 2004] → **N-one-body** = N × single  $\nu$  simulations

→ each  $\nu$  evolved from initial conditions at  $z = 3$

→ spherical symmetry, coordinates  $(r, \theta, p_r, l)$

→ need  $\rho_{\text{matter}}(z) = \rho_{\text{DM}}(z) + \rho_{\text{baryon}}(z)$

Assumptions:

$\nu$ s are independent

only gravitational interactions

$\nu$ s do not influence matter evolution

$(\rho_\nu \ll \rho_{\text{DM}})$

how many  $\nu$ s is "N"?

→ must sample all possible  $r, p_r, l$

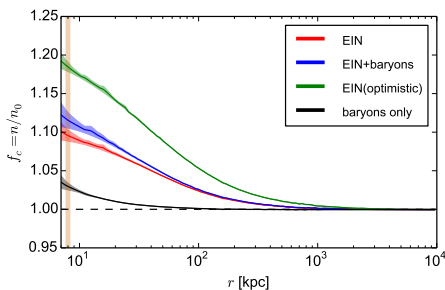
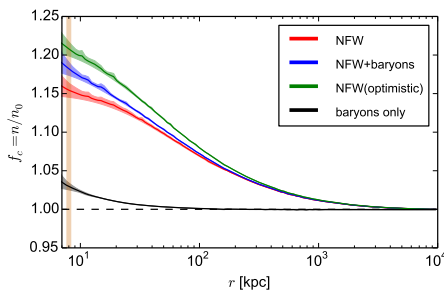
→ must include all possible  $\nu$ s that reach the MW

(fastest ones may come from  
several (up to  $\mathcal{O}(100)$ ) Mpc!)

given N  $\nu$ :

→ weigh each neutrinos

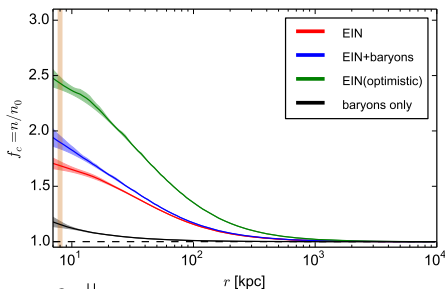
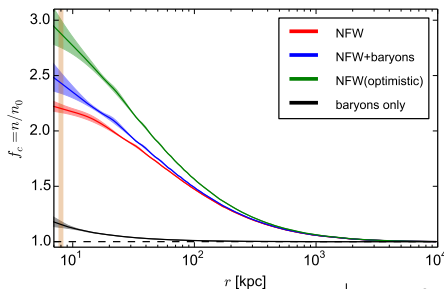
→ reconstruct final density profile with kernel method from [Merritt&Tremblay, 1994]



masses	ordering	matter halo	overdensity $f_c$		$\Gamma_{\text{tot}} \text{ (yr}^{-1}\text{)}$
			$f_1 \simeq f_2$	$f_3$	
any	any	any	no clustering		4.06
$m_3 = 60 \text{ meV}$	NO	NFW(+bar)	$\sim 1$	1.15 (1.18)	4.07 (4.08)
		NFW optimistic		1.21	4.08
		EIN(+bar)		1.09 (1.12)	4.07 (4.07)
		EIN optimistic		1.18	4.08
$m_1 \simeq m_2 = 60 \text{ meV}$	IO	NFW(+bar)	1.15 (1.18)	$\sim 1$	4.66 (4.78)
		NFW optimistic	1.21		4.89
		EIN(+bar)	1.09 (1.12)		4.42 (4.54)
		EIN optimistic	1.18		4.78

ordering dependence from  $\Gamma_{\text{CNB}} = \sum_{i=1}^3 |U_{ei}|^2 f_i [n_i(\nu_{hR}) + n_i(\nu_{hL})] N_T \bar{\sigma}$

$\Rightarrow$  minimal mass detectable by PTOLEMY if  $\Delta \simeq 100$ –150 meV

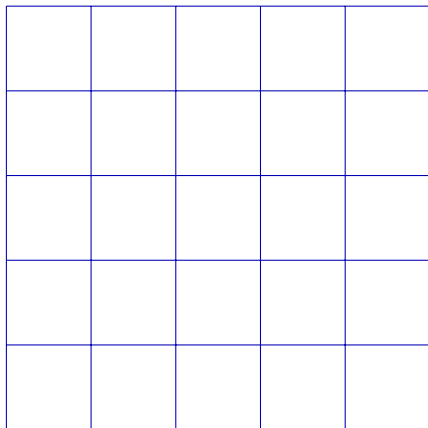
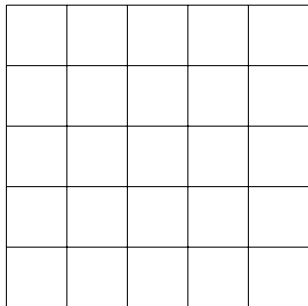


matter halo	overdensity $f_c$ $f_1 \simeq f_2 \simeq f_3$	$\Gamma_{\text{tot}}$ ( $\text{yr}^{-1}$ )
any	no clustering	4.06
NFW(+bar)	2.18 (2.44)	8.8 (9.9)
NFW optimistic	2.88	11.7
EIN(+bar)	1.68 (1.87)	6.8 (7.6)
EIN optimistic	2.43	9.9

no ordering dependence:  $m_1 \simeq m_2 \simeq m_3 \Rightarrow f_1 \simeq f_2 \simeq f_3$

## Forward-tracking and back-tracking

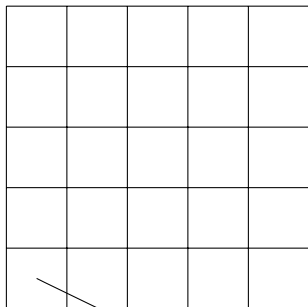
initial phase space,  $z = 4$   $\longrightarrow$  homogeneous Fermi-Dirac distribution



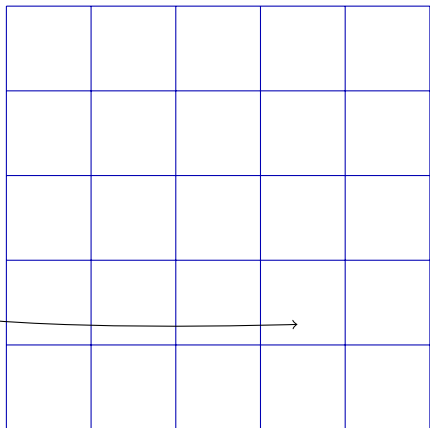
final phase space,  $z = 0$

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compute final position of each particle

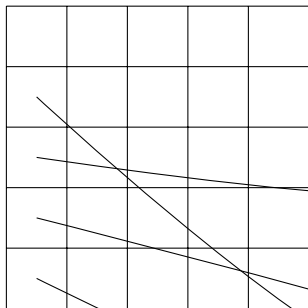


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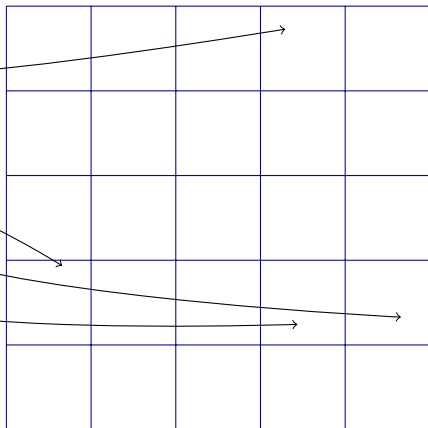


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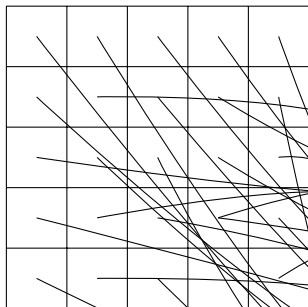
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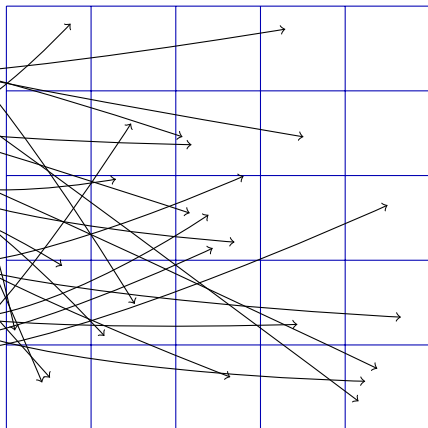
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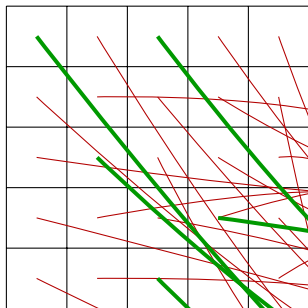
use positions to find neutrino distribution today



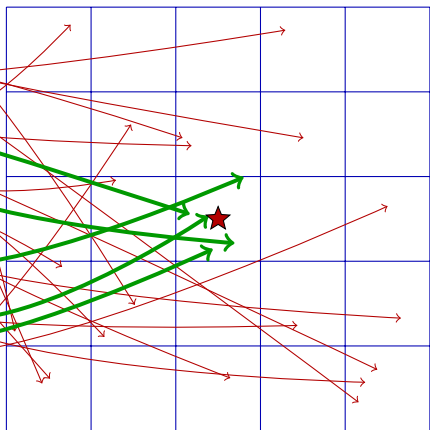
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only interested in overdensity at Earth? ★

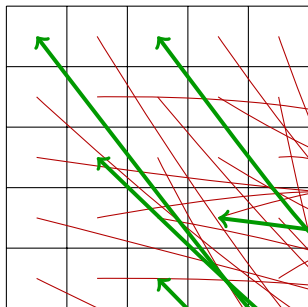


a lot of time is wasted!

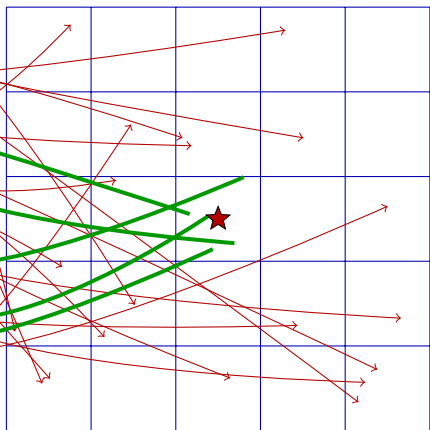
final phase space,  $z = 0$

# Forward-tracking and back-tracking

initial phase space,  $z = 4$   $\longrightarrow$  homogeneous Fermi-Dirac distribution



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a lot of time is wasted!

smarter way: track backwards  
only interesting particles!

final phase space,  $z = 0$

## Advantages of tracking back

First advantage is in computational terms: much less points to compute

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Second advantage: no need to use spherical symmetry!

Forward-tracking

initial conditions need to sample  
1D for position + 2D for momentum  
when using spherical symmetry

with full grid would re-  
quire 3+3 dimensions!

Impossible to relax  
spherical symmetry!

Back-tracking

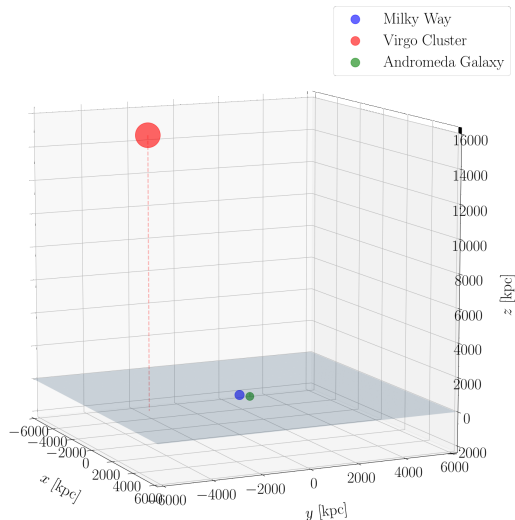
“Initial” conditions only described  
by 3D in momentum  
(position is fixed, apart for checks)

can do the calculation with  
any astrophysical setup

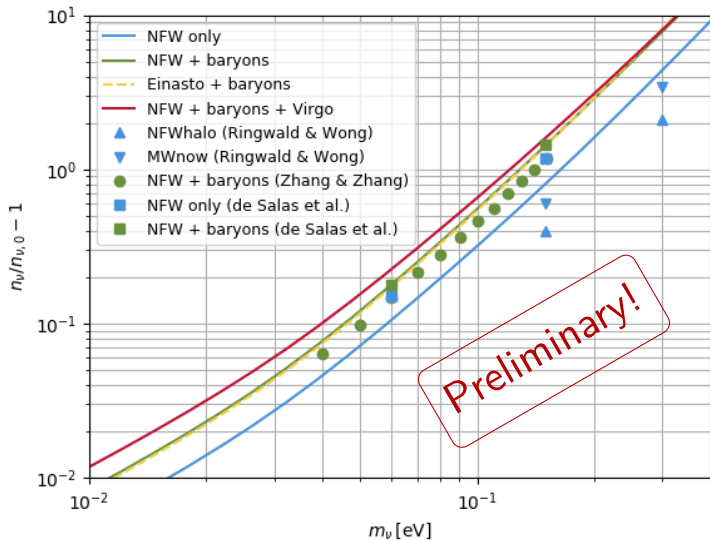
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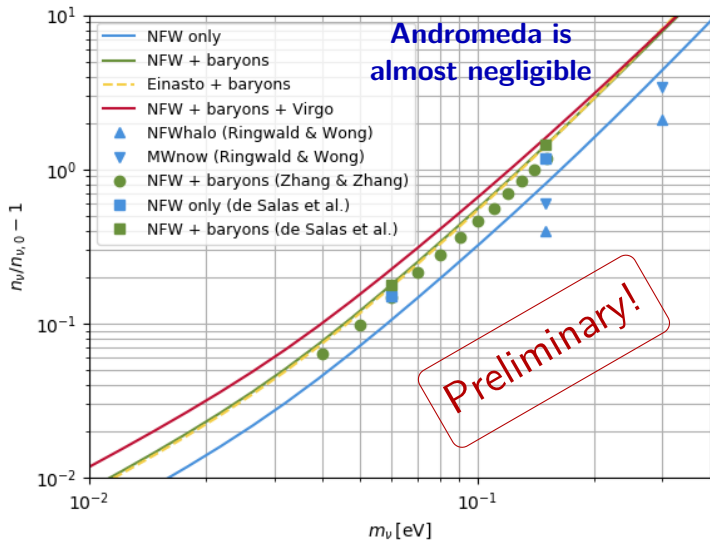


In comparison with previous results:

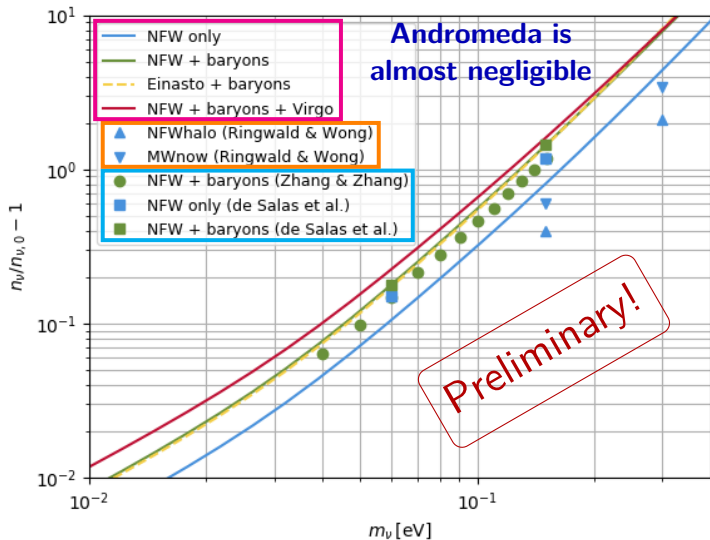




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**Warning:** NFW is not the same for all the cases!

[de Salas+, 2017]

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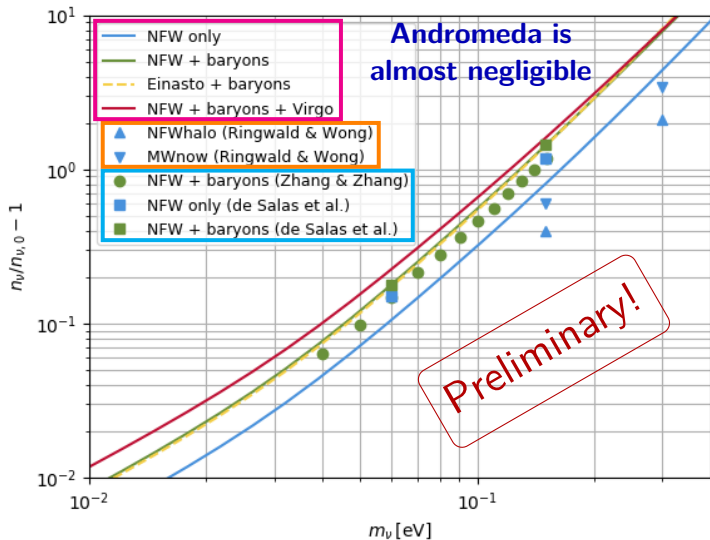
use  $\gamma \neq 1$ ,  
now we have

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[Ringwald&Wong,

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**parameters**

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many checks are missing: distance of Virgo, Sun position, more on DM, ...

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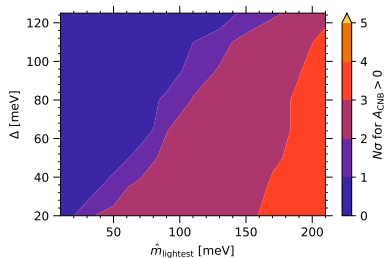
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$$\frac{d\tilde{\Gamma}_{\text{CNB}}}{dE_e}(E_e) = \frac{1}{\sqrt{2\pi}\sigma} \sum_{i=1}^{N_\nu} \bar{\sigma} N_T |U_{ei}|^2 n_0 f_c(m_i) \times e^{-\frac{[E_e - (E_{\text{end}} + m_i + m_{\text{lightest}})]^2}{2\sigma^2}}$$

$$\frac{d\Gamma_\beta}{dE_e} = \frac{\bar{\sigma}}{\pi^2} N_T \sum_{i=1}^{N_\nu} |U_{ei}|^2 H(E_e, m_i)$$

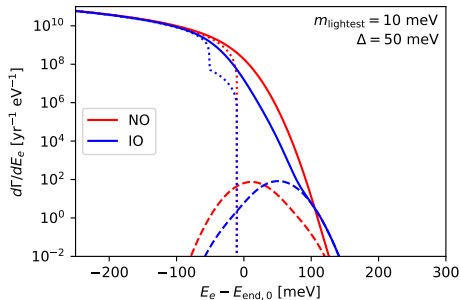
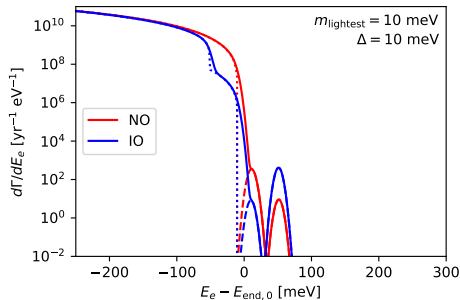
$$\frac{d\tilde{\Gamma}_\beta}{dE_e}(E_e) = \frac{1}{\sqrt{2\pi}\sigma} \int_{-\infty}^{+\infty} dx \frac{d\Gamma_\beta}{dE_e}(x) \exp\left[-\frac{(E_e - x)^2}{2\sigma^2}\right]$$

$\bar{\sigma}$  cross section,  $N_T$  number of tritium atoms in the source (PTOLEMY: 100 g),  $E_{\text{end}}$  endpoint,  $\sigma = \Delta/\sqrt{8 \ln 2}$  standard deviation

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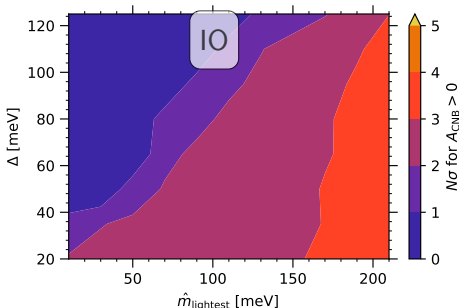
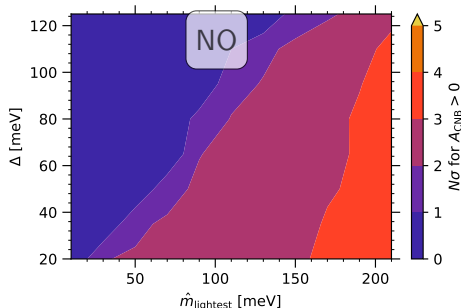
using the definition:

$$N_{\text{th}}^i(\theta) = A_{\beta} N_{\beta}^i(\hat{E}_{\text{end}} + \Delta E_{\text{end}}, m_i, U) + \mathbf{A}_{\text{CNB}} N_{\text{CNB}}^i(\hat{E}_{\text{end}} + \Delta E_{\text{end}}, m_i, U) + N_b$$

if  $\mathbf{A}_{\text{CNB}} > 0$  at  $N\sigma$ , direct detection of CNB accomplished at  $N\sigma$

statistical only!

significance on  $A_{\text{CNB}} > 0$   
as a function of  $\hat{m}_{\text{lightest}}, \Delta$



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# Conclusions

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amazing (neutrino) science  
with **direct detection**  
of relic neutrinos (e.g. PTOLEMY)

[non-relativistic regime, masses, ordering?, MW structure?, Dirac/Majorana?, ...]

2

But it will be a **technological challenge!**  
( $^3\text{H}$  amount, low background, energy resolution, ...)

3

possible event rate **enhancement**  
due to clustering in the Milky Way,  
and also **nearby galaxies/clusters!**

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Clustering **cannot increase detection chances**,  
but we could **constrain** the composition of the  
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Thank you for the attention!

# Baryons: the complexity of a structure

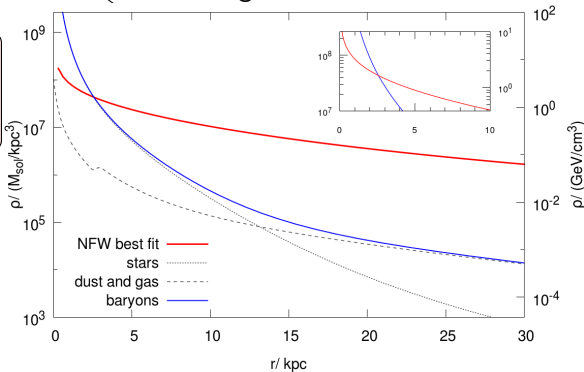
Complex problem: how to model baryon content of a galaxy?

e.g. [Pato et al., 2015]:  
70 different baryonic models

7 models for the bulge  
×  
5 for the disc  
×  
2 for the gas

[Misiriotis et al., 2006]:  
5 independent  
components

warm dust  
cold dust  
stars  
atomic  $H$  gas  
molecular  $H$  gas



our case: [Misiriotis et al., 2006], spherically symmetrized