



Horizon 2020
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Light sterile neutrinos in the early universe

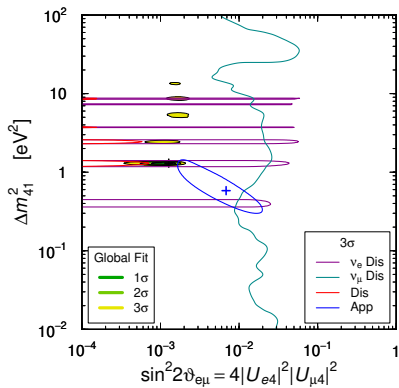
XI CPAN Meeting, Oviedo (ES), 21–23/10/2019

1 Light sterile neutrino

2 Light sterile neutrino and cosmology

3 A new interaction to solve the thermalization problem?

4 Conclusions



Three Neutrino Oscillations

Analogous to CKM mixing for quarks:

[Pontecorvo, 1968]

[Maki, Nakagawa, Sakata, 1962]

$$\nu_\alpha = \sum_{k=1}^3 U_{\alpha k} \nu_k \quad (\alpha = e, \mu, \tau)$$

ν_α flavour eigenstates, $U_{\alpha k}$ PMNS mixing matrix, ν_k mass eigenstates.

Current knowledge of the 3 active ν mixing: [de Salas et al. (2018)]

$\Delta m_{ji}^2 = m_j^2 - m_i^2$, θ_{ij} mixing angles

NO: Normal Ordering, $m_1 < m_2 < m_3$

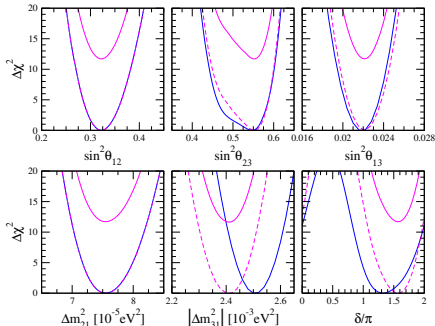
IO: Inverted Ordering, $m_3 < m_1 < m_2$

$$\begin{aligned} \Delta m_{21}^2 &= (7.55^{+0.20}_{-0.16}) \cdot 10^{-5} \text{ eV}^2 \\ |\Delta m_{31}^2| &= (2.50 \pm 0.03) \cdot 10^{-3} \text{ eV}^2 \text{ (NO)} \\ &= (2.42^{+0.03}_{-0.04}) \cdot 10^{-3} \text{ eV}^2 \text{ (IO)} \end{aligned}$$

$$\begin{aligned} \sin^2(\theta_{12}) &= 0.320^{+0.020}_{-0.016} \\ \sin^2(\theta_{13}) &= 0.0216^{+0.008}_{-0.007} \text{ (NO)} \\ &= 0.0222^{+0.007}_{-0.008} \text{ (IO)} \end{aligned}$$

$$\begin{aligned} \sin^2(\theta_{23}) &= 0.547^{+0.020}_{-0.030} \text{ (NO)} \\ &= 0.551^{+0.018}_{-0.030} \text{ (IO)} \end{aligned}$$

First hints for $\delta_{\text{CP}} \simeq 3/2\pi$



Three Neutrino Oscillations

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[Maki, Nakagawa, Sakata, 1962]

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$$\begin{aligned} \Delta m_{21}^2 &= (7.55^{+0.20}_{-0.16}) \cdot 10^{-5} \text{ eV}^2 \\ |\Delta m_{31}^2| &= (2.50^{+0.18}_{-0.16}) \cdot 10^{-3} \text{ eV}^2 \quad (\text{NO}) \\ &= (2.42^{+0.18}_{-0.04}) \cdot 10^{-3} \text{ eV}^2 \quad (\text{IO}) \end{aligned}$$

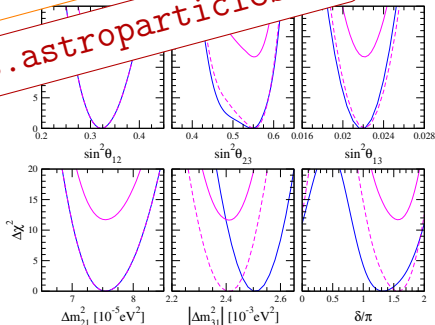
$$\begin{aligned} \sin^2(\theta_{12}) &= 0.307^{+0.008}_{-0.007} \quad (\text{NO}) \\ &= 0.222^{+0.007}_{-0.008} \quad (\text{IO}) \end{aligned}$$

$$\begin{aligned} \sin^2(\theta_{23}) &= 0.547^{+0.020}_{-0.030} \quad (\text{NO}) \\ &= 0.551^{+0.018}_{-0.030} \quad (\text{IO}) \end{aligned}$$

First hints for $\delta_{\text{CP}} \simeq 3/2\pi$

talk by M. Tórtola tomorrow

see also: <http://globalfit.astroparticles.es>



Problem: **anomalies**
in SBL experiments

→ { errors in flux calculations?
deviations from 3- ν description?

A short review:

LSND search for $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$, with $L/E = 0.4 \div 1.5$ m/MeV. Observed a 3.8σ excess of $\bar{\nu}_e$ events [Aguilar et al., 2001]

Reactor re-evaluation of the expected anti-neutrino flux \Rightarrow disappearance of $\bar{\nu}_e$ events compared to predictions ($\sim 3\sigma$) with $L < 100$ m [Mention et al, 2011], [Azabajan et al, 2012]

Gallium calibration of GALLEX and SAGE Gallium solar neutrino experiments give a 2.7σ anomaly (disappearance of ν_e) [Giunti, Laveder, 2011]

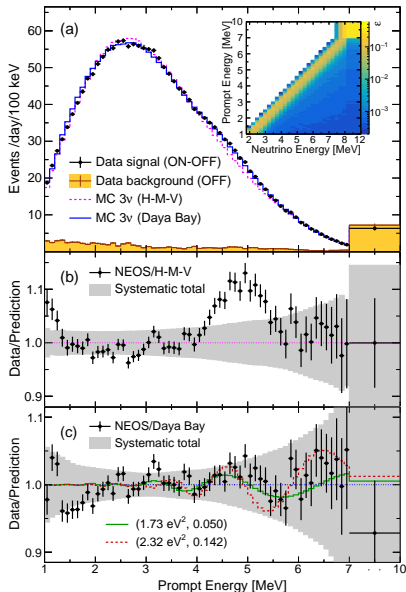
MiniBooNE

See next

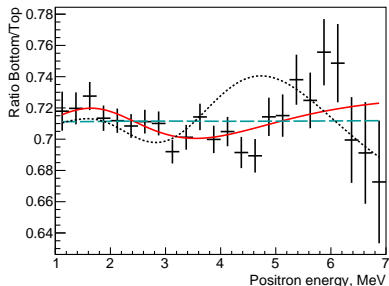
Possible explanation:

Additional squared mass
difference $\Delta m_{\text{SBL}}^2 \simeq 1 \text{ eV}^2$

[NEOS, PRL 118 (2017) 121802]



[DANSS, PLB 787 (2018) 56]

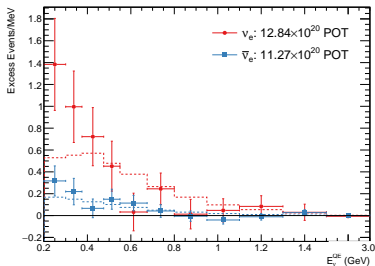
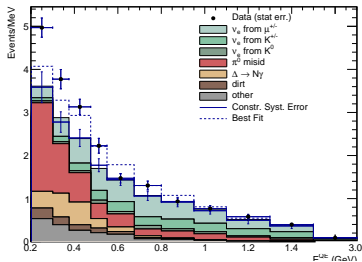


first *model independent* indications in favor of SBL oscillations

DANSS alone gives a $\Delta\chi^2 \simeq 13$ in favor of a light sterile neutrino!

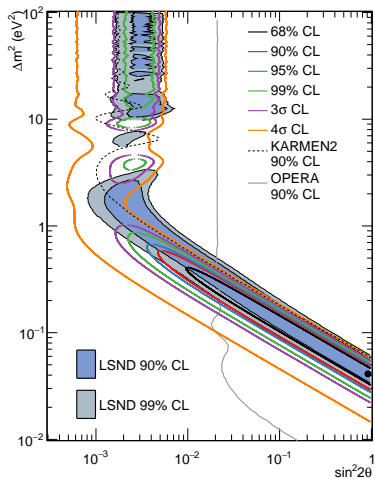
Recent results...

[MiniBooNE, PRL
121 (2018) 221801]



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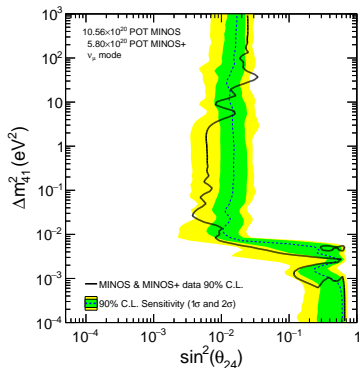
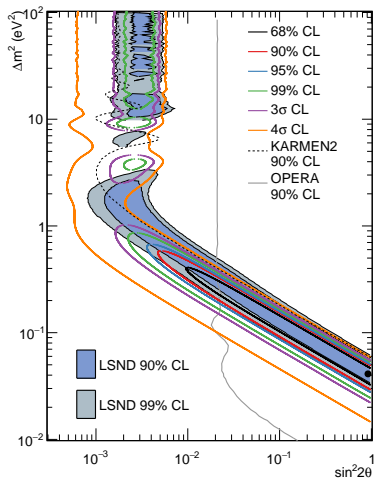
[MiniBooNE, PRL
121 (2018) 221801]



Recent results...

[MiniBooNE, PRL
121 (2018) 221801]

[MINOS+, PRL
122 (2019) 091803]



MiniBooNE is incompatible
with MINOS+ when combined
with NEOS&DANSS

3+1 Neutrino Model

new $\Delta m_{\text{SBL}}^2 \Rightarrow 4$ neutrinos!

ν_4 with $m_4 \simeq 1$ eV,
no weak interactions

light sterile neutrino (LS ν)

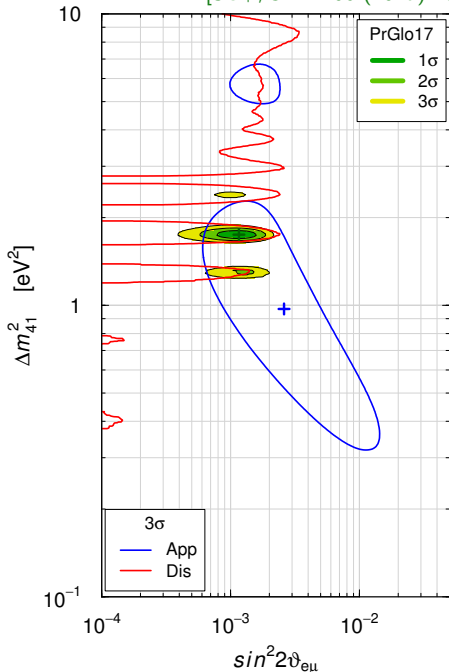
3 (active) + 1 (sterile) mixing:

$$\nu_\alpha = \sum_{k=1}^{3+1} U_{\alpha k} \nu_k \quad (\alpha = e, \mu, \tau, s)$$

ν_s is mainly ν_4 :

$$m_s \simeq m_4 \simeq \sqrt{\Delta m_{41}^2} \simeq \sqrt{\Delta m_{\text{SBL}}^2}$$

assuming $m_4 \gg m_i$ ($i = 1, 2, 3$)



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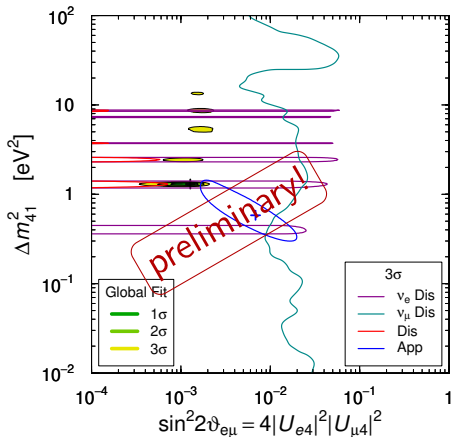
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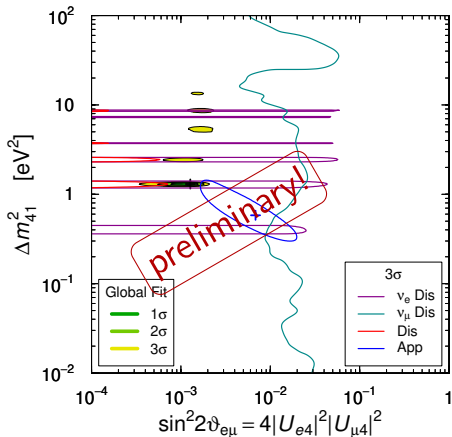
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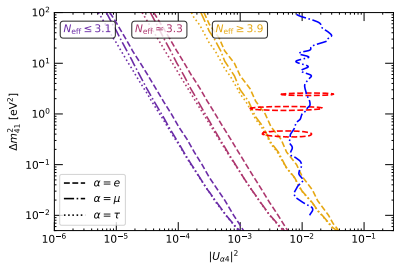
can ν_4 thermalize in the early
Universe through oscillations?

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ν oscillations in the early universe

comoving coordinates: $a = 1/T$ $x \equiv m_e a$ $y \equiv p a$ $z \equiv T_\gamma a$ $w \equiv T_\nu a$

$$\text{density matrix: } \varrho(x, y) = \begin{pmatrix} \varrho_{ee} \equiv f_{\nu_e} & \varrho_{e\mu} & \varrho_{e\tau} & \varrho_{es} \\ \varrho_{\mu e} & \varrho_{\mu\mu} \equiv f_{\nu_\mu} & \varrho_{\mu\tau} & \varrho_{\mu s} \\ \varrho_{\tau e} & \varrho_{\tau\mu} & \varrho_{\tau\tau} \equiv f_{\nu_\tau} & \varrho_{\tau s} \\ \varrho_{se} & \varrho_{s\mu} & \varrho_{s\tau} & \varrho_{ss} \equiv f_{\nu_s} \end{pmatrix}$$

$$\frac{d\varrho(y, x)}{dx} = \sqrt{\frac{3m_{\text{Pl}}^2}{8\pi\rho_T}} \left\{ -i \frac{x^2}{m_e^3} \left[\frac{M_F}{2y} - \frac{8\sqrt{2}G_F y m_e^6}{3x^6} \left(\frac{\mathbb{E}_\ell}{m_W^2} + \frac{\mathbb{E}_\nu}{m_Z^2} \right), \varrho \right] + \frac{m_e^3 G_F^2}{(2\pi)^3 x^4 y^2} \mathcal{I}(\varrho) \right\}$$

m_{Pl} Planck mass – ρ_T total energy density – $m_{W,Z}$ mass of the W, Z bosons – G_F Fermi constant – $[\cdot, \cdot]$ commutator

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$$\mathbb{M}_F = U M U^\dagger$$

$$M = \text{diag}(m_1^2, \dots, m_N^2)$$

$$U = R^{34} R^{24} R^{14} R^{23} R^{13} R^{12} \quad \text{e.g. } R^{14} = \begin{pmatrix} \cos \theta_{14} & 0 & 0 & \sin \theta_{14} \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ -\sin \theta_{14} & 0 & 0 & \cos \theta_{14} \end{pmatrix}$$

$$|U|^2 = \begin{pmatrix} \dots & \dots & \dots & \sin^2 \theta_{14} \\ \dots & \dots & \dots & \cos^2 \theta_{14} \sin^2 \theta_{24} \\ \dots & \dots & \dots & \cos^2 \theta_{14} \cos^2 \theta_{24} \sin^2 \theta_{34} \\ \dots & \dots & \dots & \cos^2 \theta_{14} \cos^2 \theta_{24} \cos^2 \theta_{34} \end{pmatrix}$$

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lepton densities

neutrino densities

(only for active neutrinos)

take into account matter effects in oscillations

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$\mathcal{I}(\varrho)$ collision integrals

take into account neutrino-electron scattering and pair annihilation

2D integrals over the momentum, take most of the computation time

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from continuity
equation
 $\dot{\rho} = -3H(\rho + P)$

$$\frac{dz}{dx} = \frac{\sum_{\ell=e,\mu} \left[\frac{r_\ell^2}{r} J(r_\ell) \right] + G_1(r) - \frac{1}{2\pi^2 z^3} \int_0^\infty dy y^3 \sum_{\alpha=e} \frac{d\varrho_{\alpha\alpha}}{dx}}{\sum_{\ell=e,\mu} \left[r_\ell^2 J(r_\ell) + Y(r_\ell) \right] + G_2(r) + \frac{2\pi^2}{15}}$$

$r = x/z$, $r_\ell = m_\ell/m_e r$ $J(r)$, $Y(r)$ from non-relativistic transition of e^\pm , μ^\pm
 $G_1(r)$ and $G_2(r)$ from electromagnetic corrections

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neutrino temperature w : same equation as z , but electrons always relativistic

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neutrino temperature w : same equation as z , but electrons always relativistic

initial conditions: $\varrho_{\alpha\alpha} = \text{Fermi-Dirac at } x_{\text{in}} \simeq 0.001$, with $w = z \simeq 1$

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comoving coordinates: $a = 1/T$ $x \equiv m_e a$ $y \equiv p a$ $z \equiv T_\gamma a$ $w \equiv T_\nu a$

$$\text{density matrix: } \varrho(x, y) = \begin{pmatrix} \varrho_{ee} \equiv f_{\nu_e} & \varrho_{e\mu} & \varrho_{e\tau} & \varrho_{es} \\ \varrho_{\mu e} & \varrho_{\mu\mu} \equiv f_{\nu_\mu} & \varrho_{\mu\tau} & \varrho_{\mu s} \\ \varrho_{\tau e} & \varrho_{\tau\mu} & \varrho_{\tau\tau} \equiv f_{\nu_\tau} & \varrho_{\tau s} \\ \varrho_{se} & \varrho_{s\mu} & \varrho_{s\tau} & \varrho_{ss} \equiv f_{\nu_s} \end{pmatrix}$$

$$\frac{d\varrho(y, x)}{dx} = \sqrt{\frac{3m_{\text{Pl}}^2}{8\pi\rho_T}} \left\{ -i \frac{x^2}{m_e^3} \left[\frac{M_F}{2y} - \frac{8\sqrt{2}G_F y m_e^6}{3x^6} \left(\frac{E_\ell}{m_W^2} + \frac{E_\nu}{m_Z^2} \right), \varrho \right] + \frac{m_e^3 G_F^2}{(2\pi)^3 x^4 y^2} \mathcal{I}(\varrho) \right\}$$

FORTRAN-EVOLVED PRIMORDIAL NEUTRINO OSCILLATIONS (FORTEPIANO)

https://bitbucket.org/ahep_cosmo/fortepiano

from continuity equation

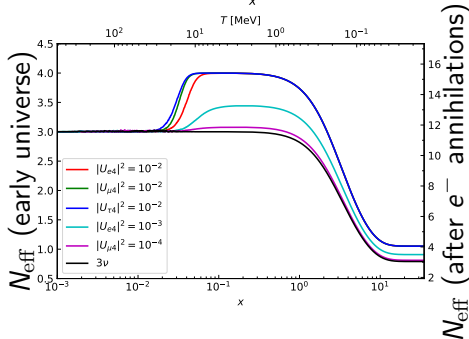
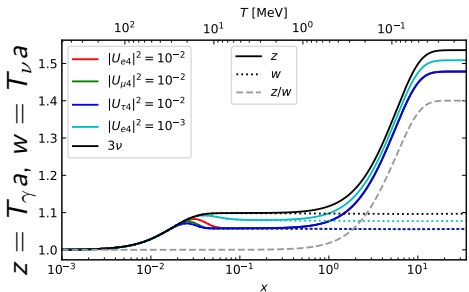
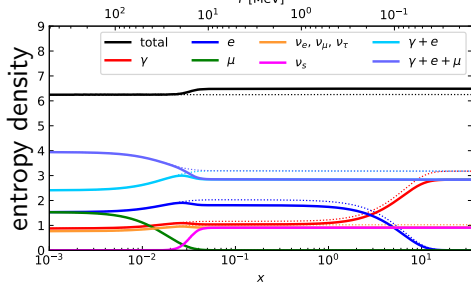
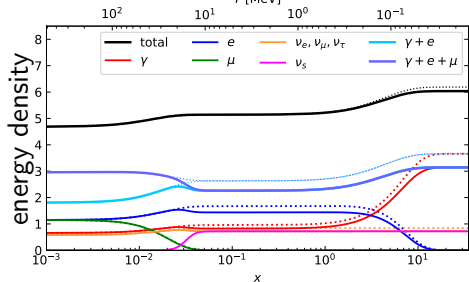
$$\dot{\rho} = -3H(\rho + P)$$

will be public soon

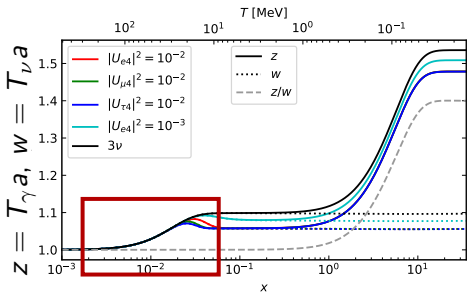
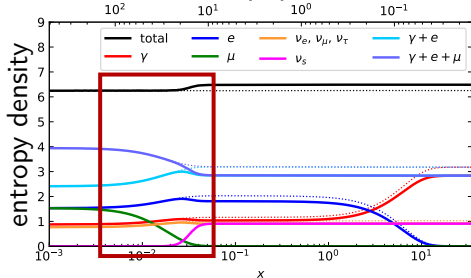
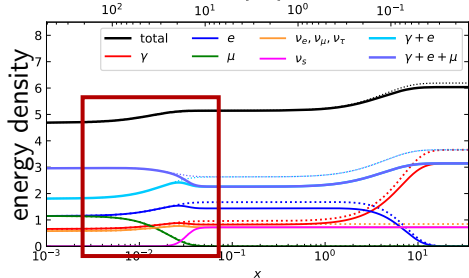
$$\frac{dz}{dx} = \frac{\sum_{\ell=e,\mu} \left[r_\ell^2 J(r_\ell) + Y(r_\ell) \right] + G_2(r) + \frac{2\pi^2}{15}}{2\pi^2 z^3 \int_0^\infty dy y^3 \sum_{\alpha=e} \frac{d\varrho_{\alpha\alpha}}{dx}}$$

neutrino temperature w : same equation as z , but electrons always relativistic
initial conditions: $\varrho_{\alpha\alpha} = \text{Fermi-Dirac at } x_{\text{in}} \simeq 0.001$, with $w = z \simeq 1$

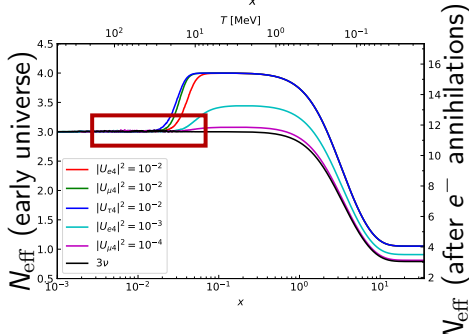
dashed: 3ν , solid: $|U_{e4}|^2 = 10^{-2}$, $|U_{\mu 4}|^2 = |U_{\tau 4}|^2 = 0$. $\Delta m_{41}^2 = 1.29 \text{ eV}^2$ always



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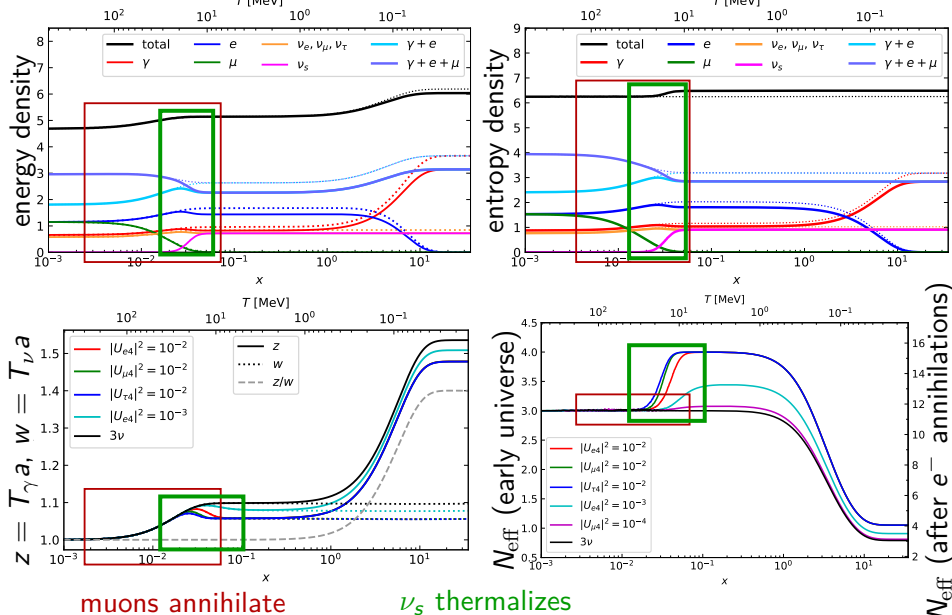
muons annihilate



N_{eff} (after e^- annihilations)

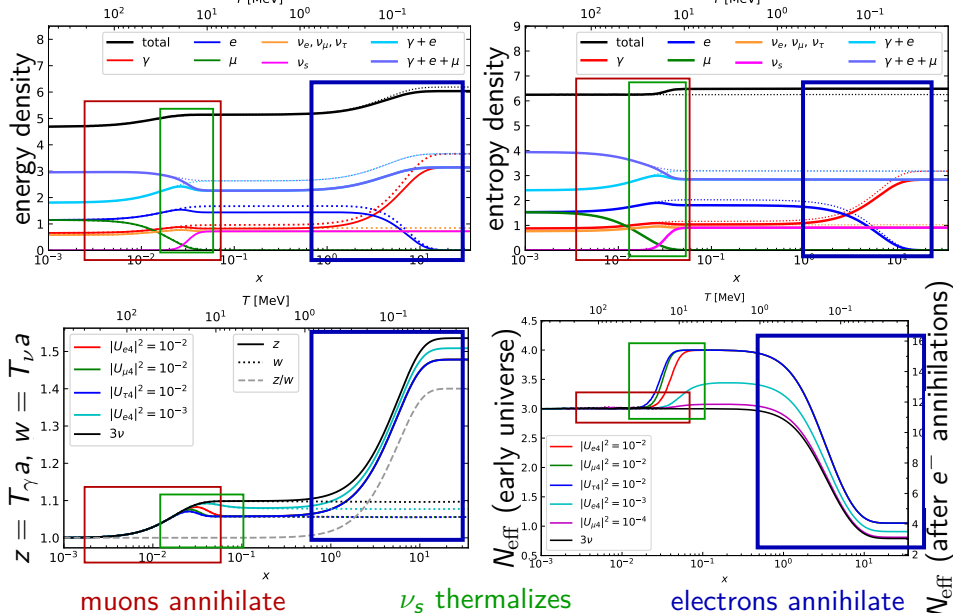
Energy, entropy, temperatures, N_{eff}

dashed: 3ν , solid: $|U_{e4}|^2 = 10^{-2}$, $|U_{\mu 4}|^2 = |U_{\tau 4}|^2 = 0$. $\Delta m_{41}^2 = 1.29 \text{ eV}^2$ always

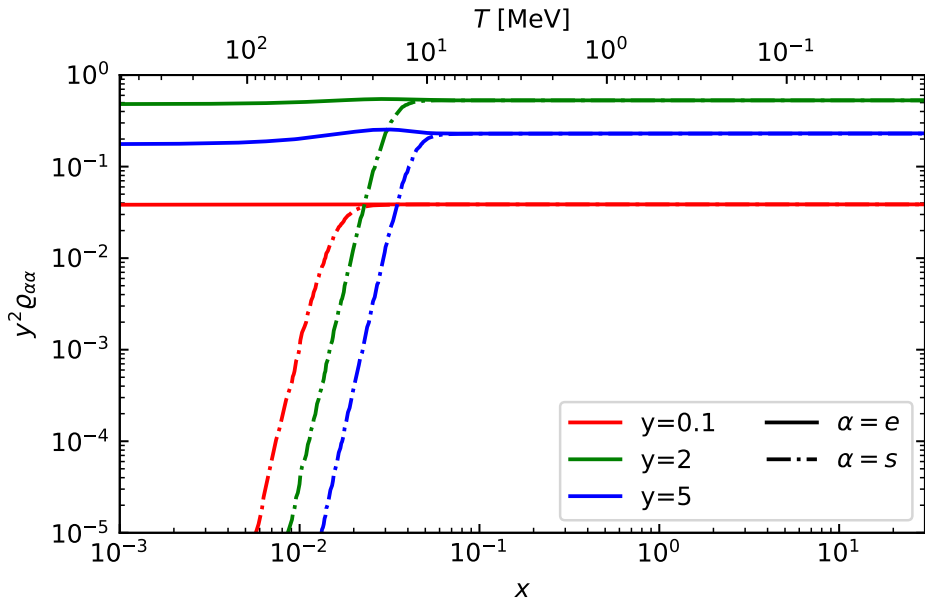


Energy, entropy, temperatures, N_{eff}

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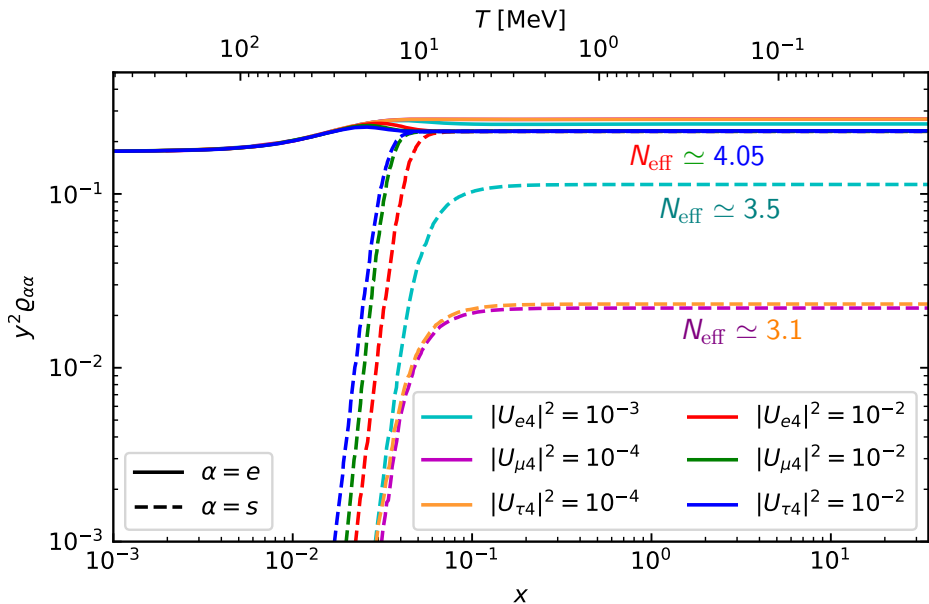


$$\Delta m_{41}^2 = 1.29 \text{ eV}^2, |U_{e4}|^2 = 10^{-2}, |U_{\mu 4}|^2 = |U_{\tau 4}|^2 = 0, N_{\text{eff}} \simeq 4.05$$



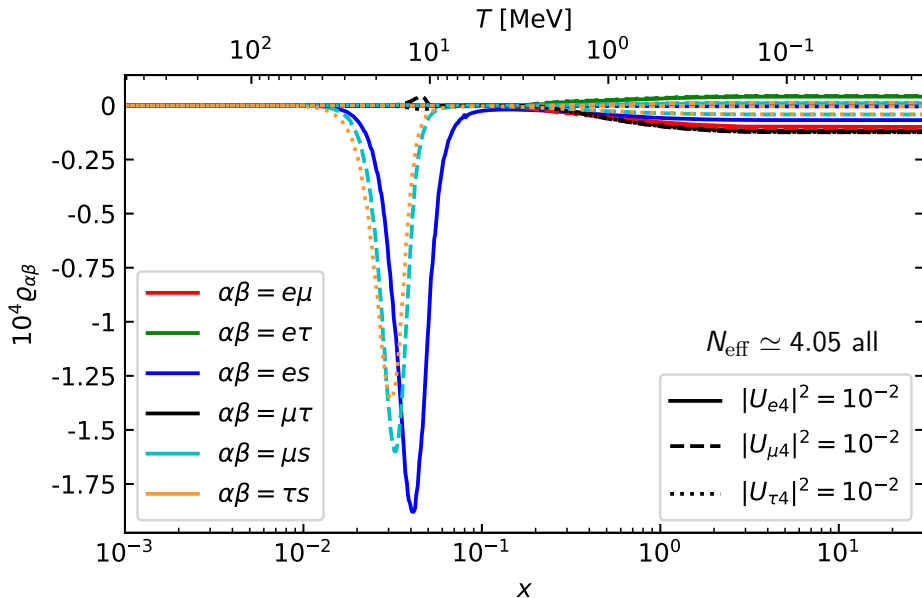
Momentum distributions

$$\Delta m_{41}^2 = 1.29 \text{ eV}^2, \text{ other } |U_{\beta 4}|^2 = 0, y = 5$$

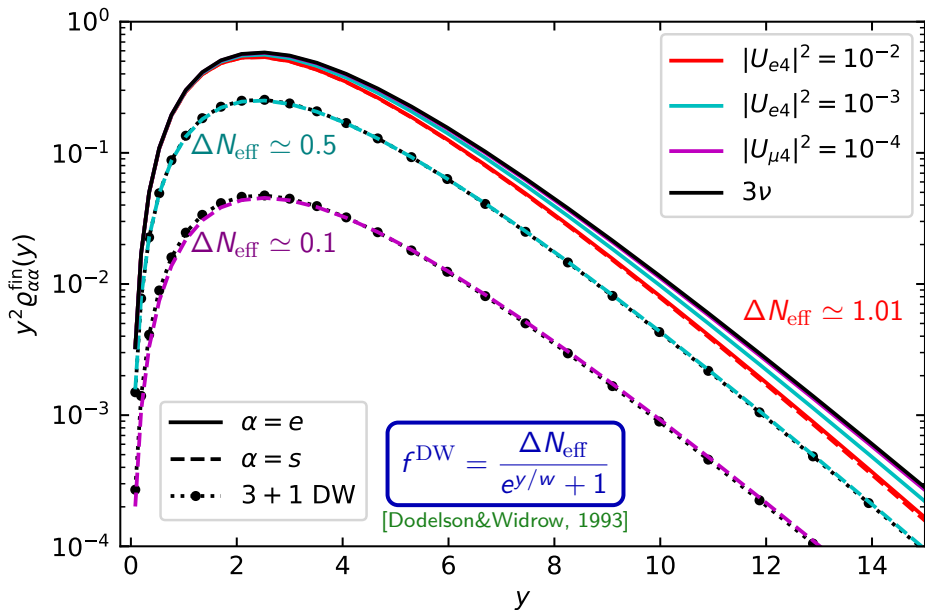


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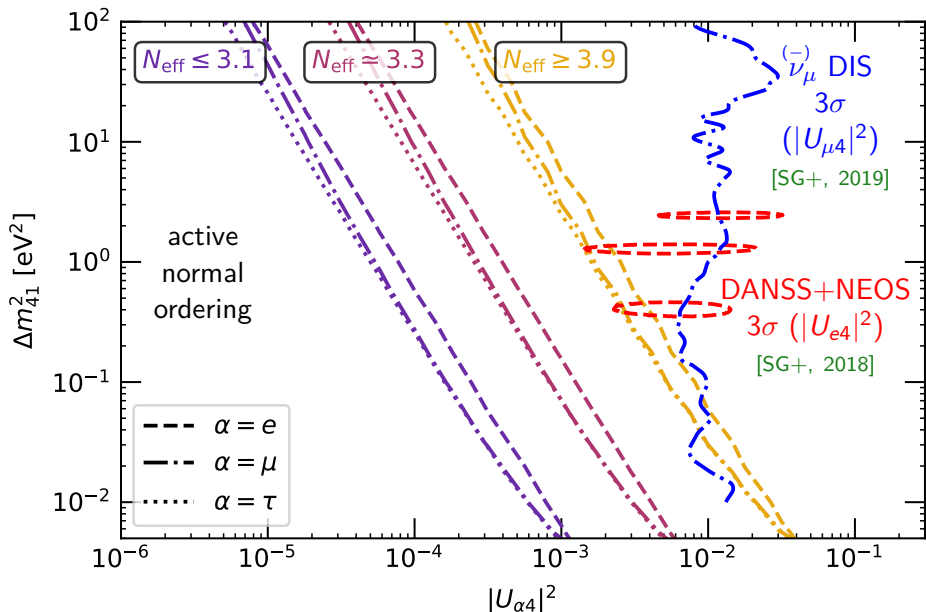


$$\Delta m_{41}^2 = 1.29 \text{ eV}^2, \text{ other } |U_{\beta 4}|^2 = 0, \Delta N_{\text{eff}} = N_{\text{eff}} - N_{\text{eff}}^{\text{active}}$$

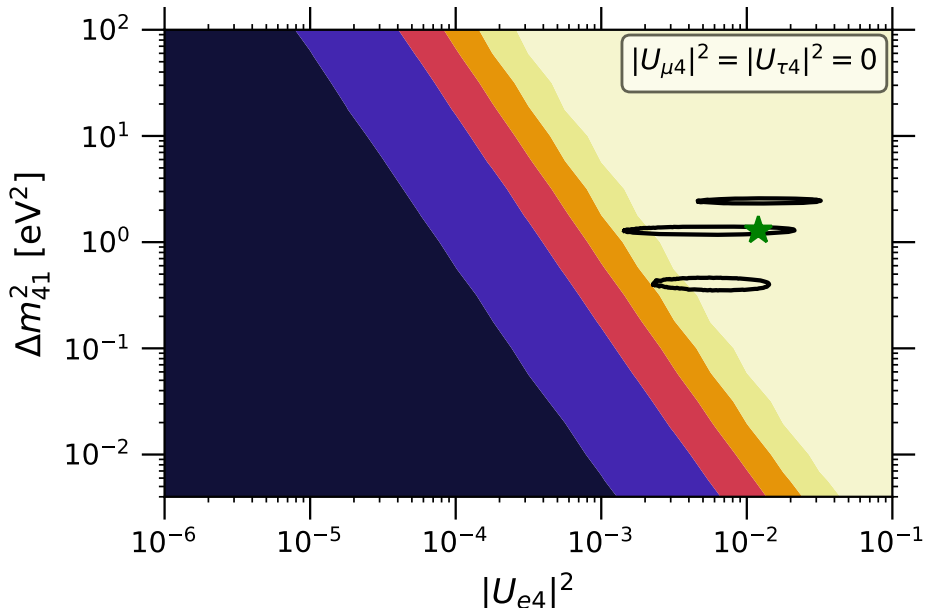
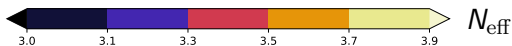


N_{eff} and the new mixing parameters

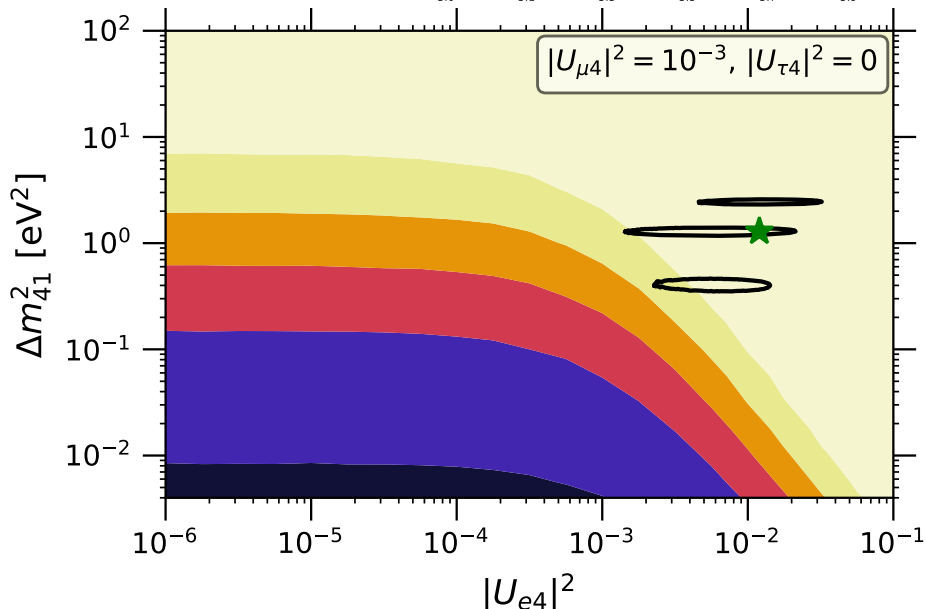
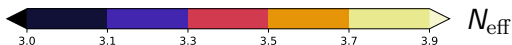
Only vary one angle and fix two to zero: do they have the same effect?



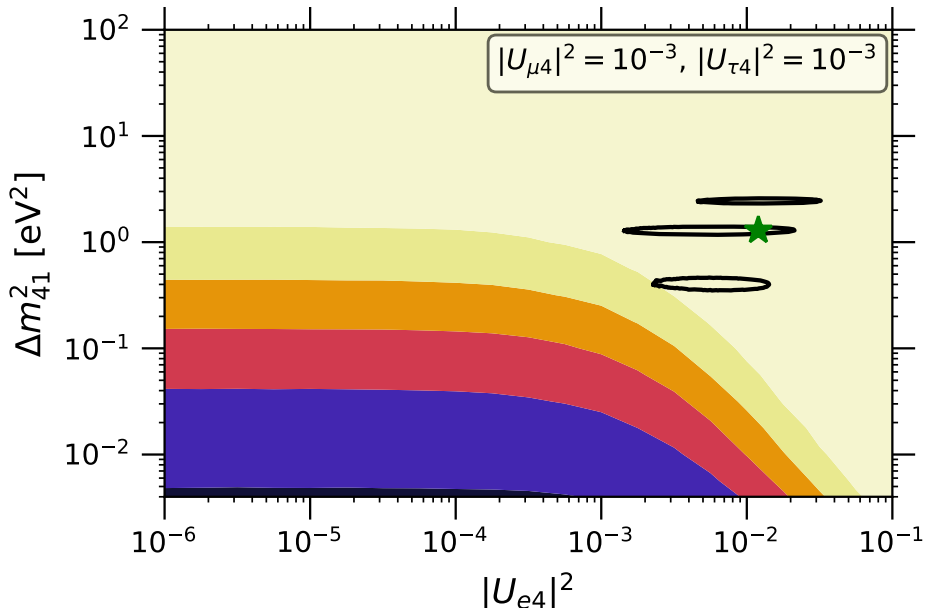
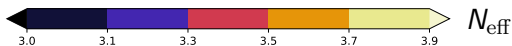
We can vary more than one angle:



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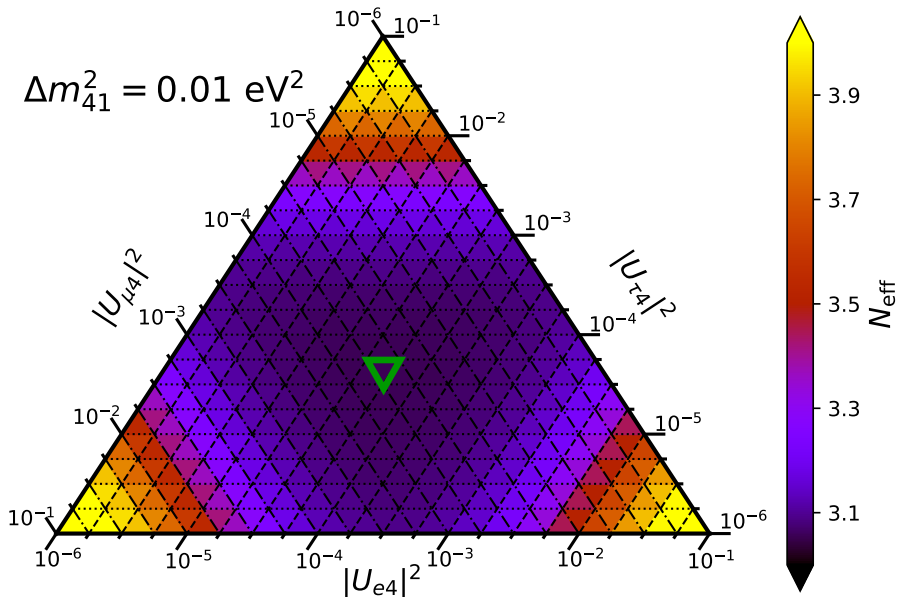


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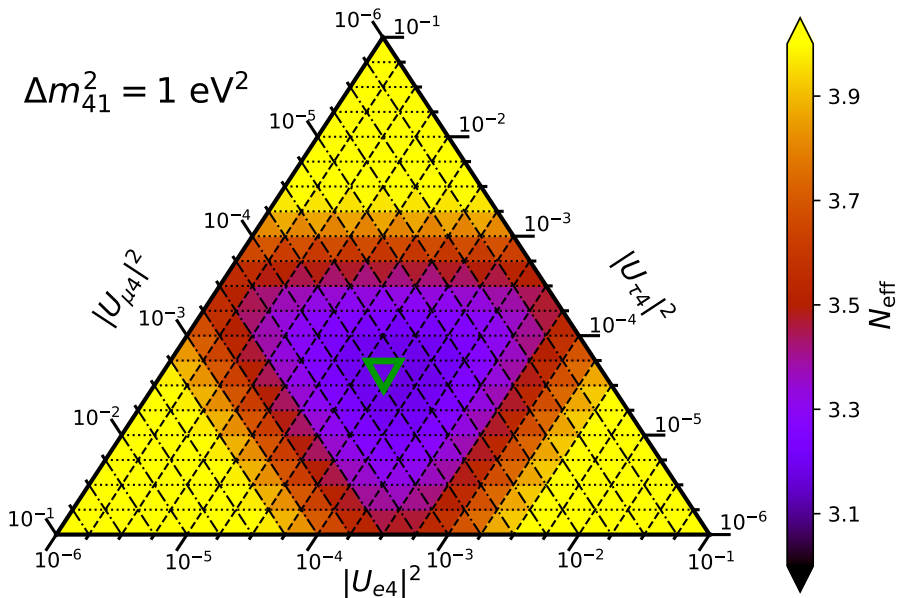


N_{eff} and the new mixing parameters

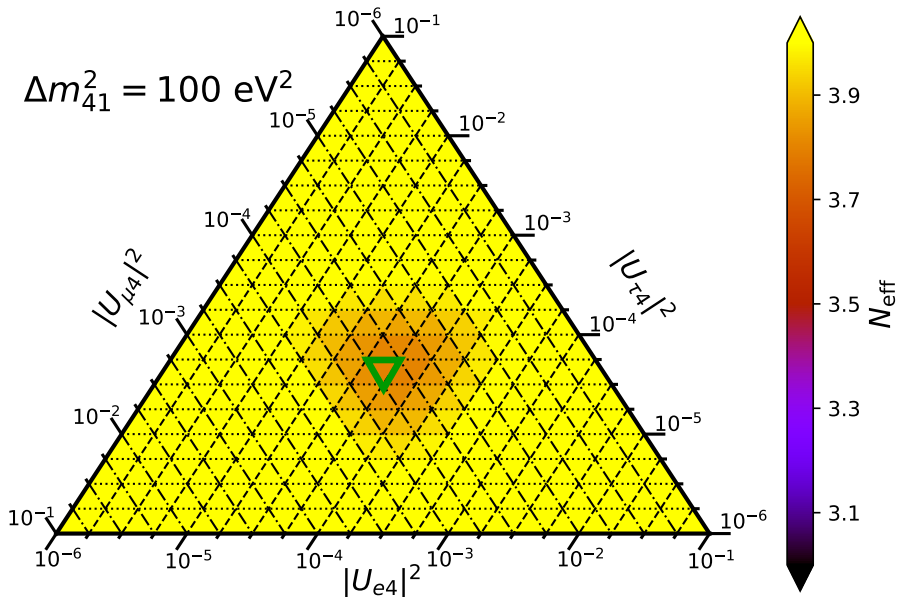
Sort of ternary plot (sum of $|U_{\alpha 4}|^2$ does not add up to 1!):



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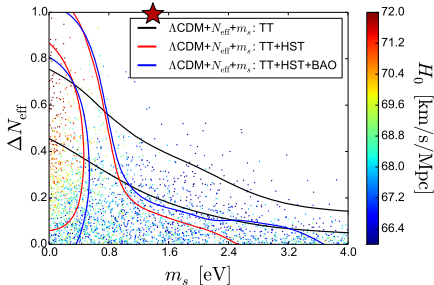
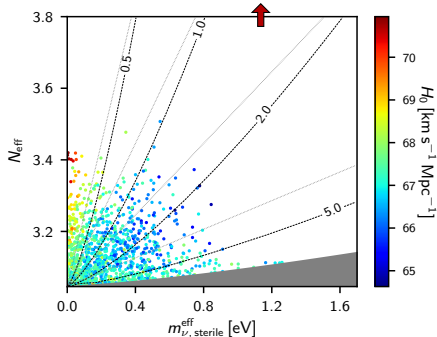
Sort of ternary plot (sum of $|U_{\alpha 4}|^2$ does not add up to 1!):



LS ν constraints from cosmology

CMB+local: [Planck Collaboration, 2018]

[Archidiacono et al., JCAP 08 (2016) 067]



$$\left\{ \begin{array}{l} N_{\text{eff}} < 3.29 \\ m_s^{\text{eff}} < 0.65 \text{ eV} \end{array} \right. \quad (\text{Planck18+BAO}) \quad [m_s < 10 \text{ eV}]$$

dataset	free ΔN_{eff} [$m_s < 10 \text{ eV}$]	$\Delta N_{\text{eff}} = 1$
(TT)	$N_{\text{eff}} < 3.5$	$m_s < 0.66 \text{ eV}$
(+H ₀)	$N_{\text{eff}} < 3.9$	$m_s < 0.55 \text{ eV}$
(+BAO)	$N_{\text{eff}} < 3.8$	$m_s < 0.53 \text{ eV}$

BBN constraints: $N_{\text{eff}} = 2.90 \pm 0.22$ (BBN+ Y_p) [Peimbert et al., 2016]

Summary: $\Delta N_{\text{eff}} = 1$ from LS ν incompatible with CMB and BBN!

Incomplete Thermalization

Active-sterile oscillations in the early Universe:

mixing parameters from SBL data $\implies \Delta N_{\text{eff}} \simeq 1$

[SG+, 2019]

Many probes constrain $\Delta N_{\text{eff}} < 1$. Do we need

- a mechanism to suppress oscillations and full thermalization of ν_s ?
- to compensate $\Delta N_{\text{eff}} = 1$ with additional mechanisms in Cosmology?

Some ideas (an incomplete list!):

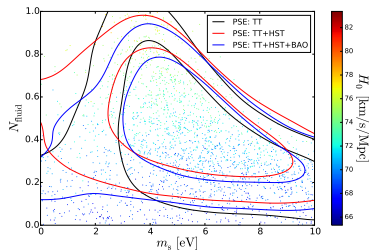
- large lepton asymmetry [Foot et al., 1995; Mirizzi et al., 2012; many more]
- new neutrino interactions [Bento et al., 2001; Dasgupta et al., 2014; Hannestad et al., 2014; Saviano et al., 2014; Archidiacono et al. 2016; many more]
- entropy production after neutrino decoupling [Ho et al., 2013]
- very low reheating temperature [Gelmini et al., 2004; Smirnov et al., 2006]
- time varying dark energy components [Giusarma et al., 2012]
- larger expansion rate at the time of ν_s production [Rehagen et al., 2014]
- freedom in the Primordial Power Spectrum (PPS) of scalar perturbations from inflation compensate damping due to $N_{\text{eff}} \neq 3.046$ [SG et al., 2015]

1 *Light sterile neutrino*

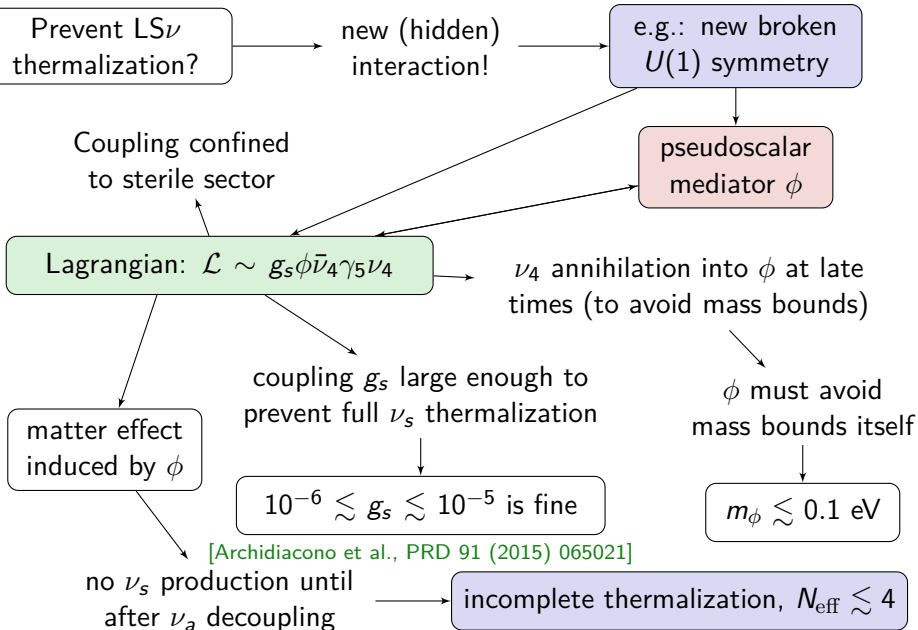
2 *Light sterile neutrino and cosmology*

3 ***A new interaction to solve the thermalization problem?***

4 *Conclusions*



Adding a new interaction



Constraints on the pseudoscalar interaction?

Particle physics constraints
on the pseudoscalar?

IceCube constraints on
secret interactions?

[Ioka et al., 2014] [Cherry et al., 2014]
[Ng et al., 2014] [Cherry et al., 2016]

ϕ coupled to ν_4 + IceCube flux made of
active flavor neutrinos

very small mixing with ν_4
and interaction rate with ϕ
[cross section $\propto g_s^2/s$]

don't apply

fifth force constraints?

pseudoscalar is spin coupling,
but unpolarized medium

don't apply

SN energy loss
[Farzan, 2003]

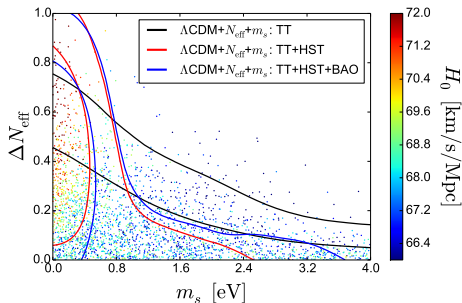
$g_s \lesssim 10^{-4}$

Results

Standard $LS\nu$ model:

$$\Lambda\text{CDM} + N_{\text{eff}} + m_s$$

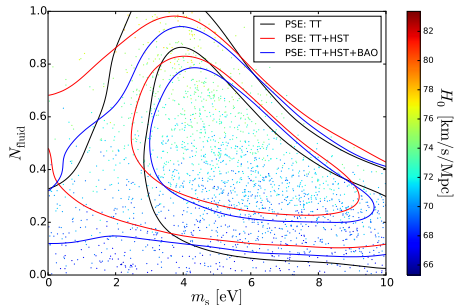
(ΛCDM params + free N_{eff} and m_s)



Pseudoscalar model (PSE):

$$N_{\text{eff}} = 3.046 + N_{\text{fluid}}$$

N_{fluid} : $\nu_s + \phi$ contributions



- Problems with $\Delta N_{\text{eff}} = 1$? **solved** (incomplete thermalization due to suppression of active-sterile oscillations in primordial plasma);
- mass bounds avoided
 - ⇒ large m_s allowed and **(mild) preference** for $m_s \simeq 4$ eV;
- **high values of H_0** predicted by cosmology
 - ⇒ more compatible with local measurements.

1 *Light sterile neutrino*

2 *Light sterile neutrino and cosmology*

3 *A new interaction to solve
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4 **Conclusions**

Conclusions

1

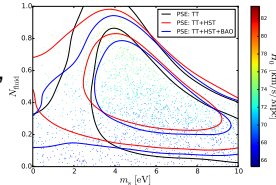
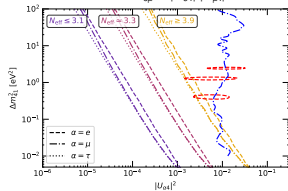
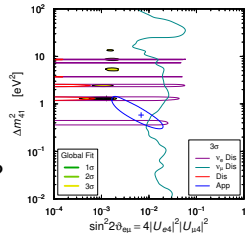
Unclear status of $LS\nu$ searches:
APP-DIS tension!
Systematics or $LS\nu$ or new physics?

2

oscillations in the early universe $\Rightarrow N_{\text{eff}} \simeq 4.05$
Planck constrains $N_{\text{eff}} \lesssim 3.3!$

3

Reconcile $LS\nu$ and cosmology
with new pseudoscalar interaction,
also mitigating H_0 tension!



Conclusions

1

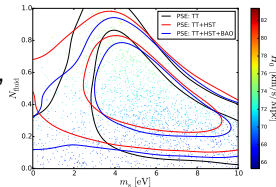
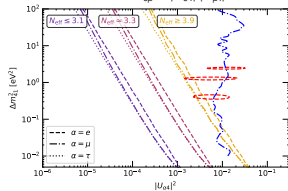
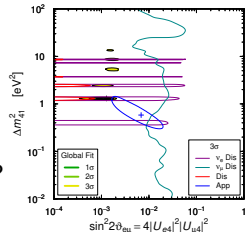
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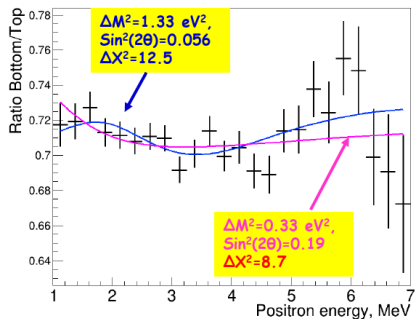
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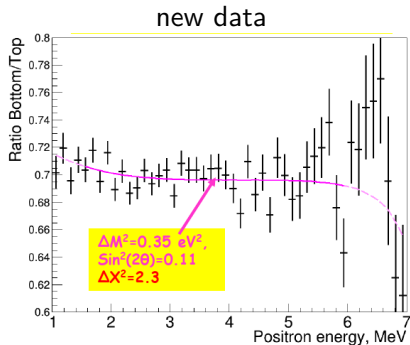
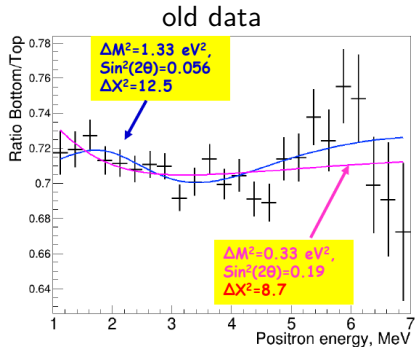
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Thank you for the attention!

old data





New analysis also
 considers systematics!

