



# Stefano Gariazzo

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European  
Commission

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European Union funding  
for Research & Innovation

## Cosmological relic neutrinos, from A to Z

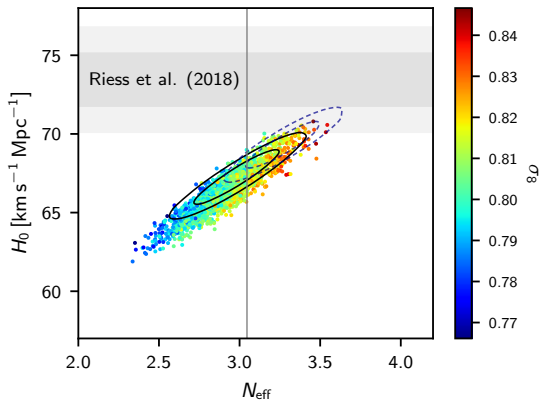
INT-20-1a, Seattle (USA/WA), 30/01/2020

# A Active neutrinos

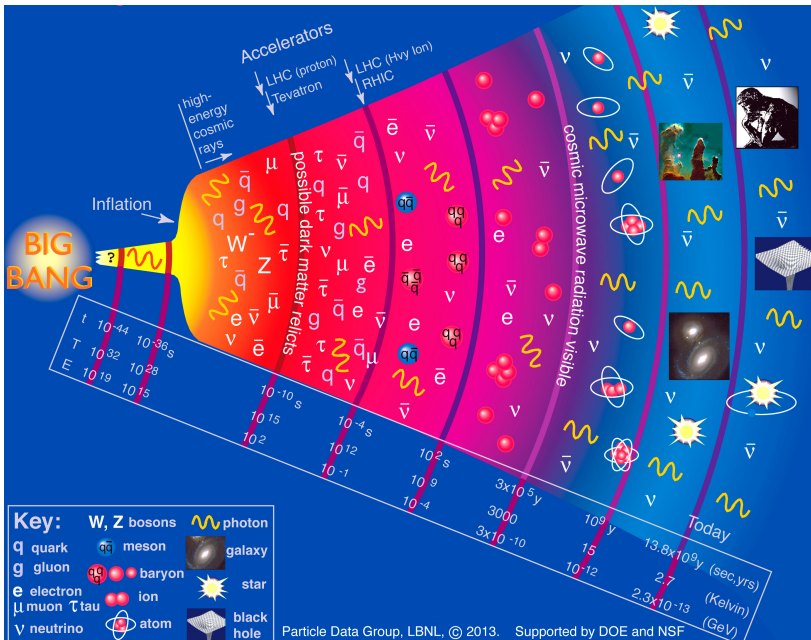
Spoiler: “Sterile” will come later

Based on:

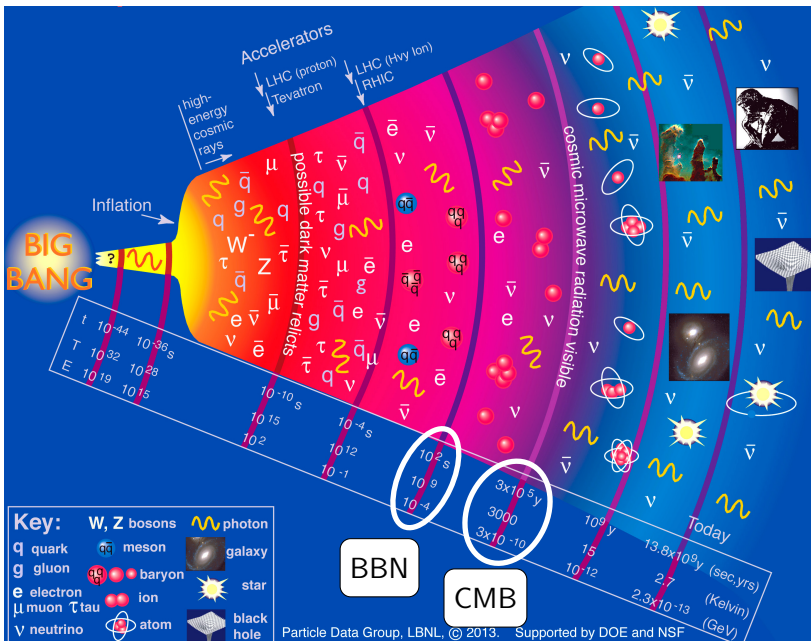
- Planck 2018
- Mangano+ 2005
- de Salas+ 2016
- in preparation (1)



# History of the universe



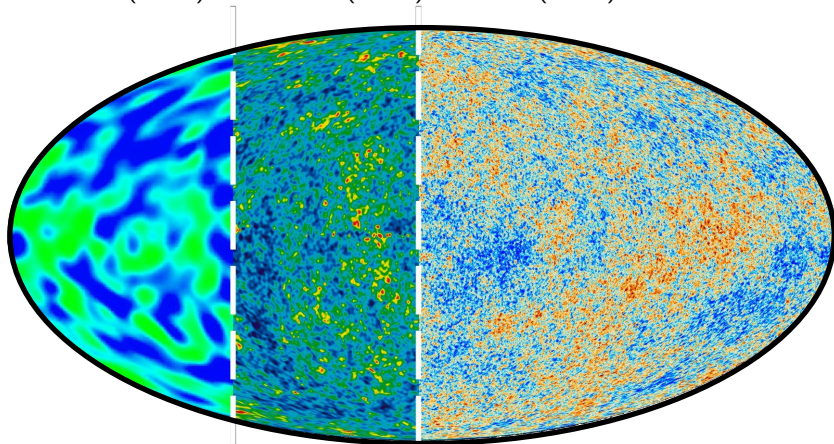
# History of the universe



# The oldest picture of the Universe

The Cosmic Microwave Background, generated at  $t \simeq 4 \times 10^5$  years

COBE (1992)    WMAP (2003)    Planck (2013)



# Big Bang Nucleosynthesis (BBN)

BBN: production of light nuclei at  $t \sim 1\text{s}$  to  $t \sim \mathcal{O}(10^2)\text{s}$

temperature  $T_{fr} \simeq 1\text{ MeV}$   
from nucleon freeze-out

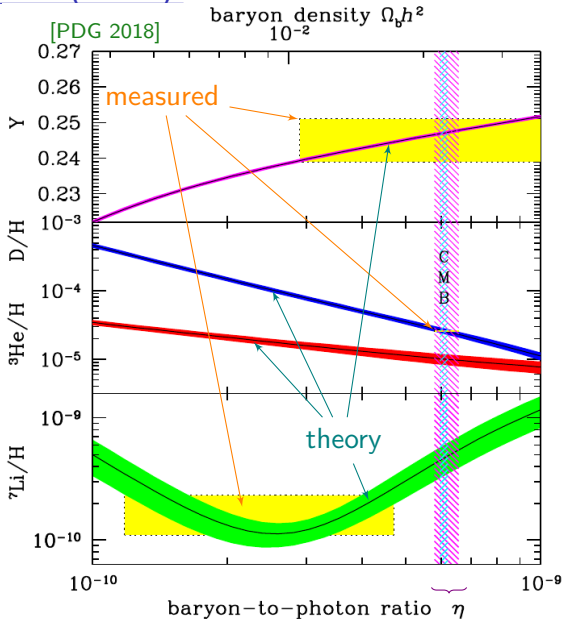
much earlier than CMB!

strong probe for physics  
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e.g. neutrinos!

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universe expansion  
and

reaction rates ( $\nu_e/\bar{\nu}_e$ )  
at BBN time...



BBN concordance

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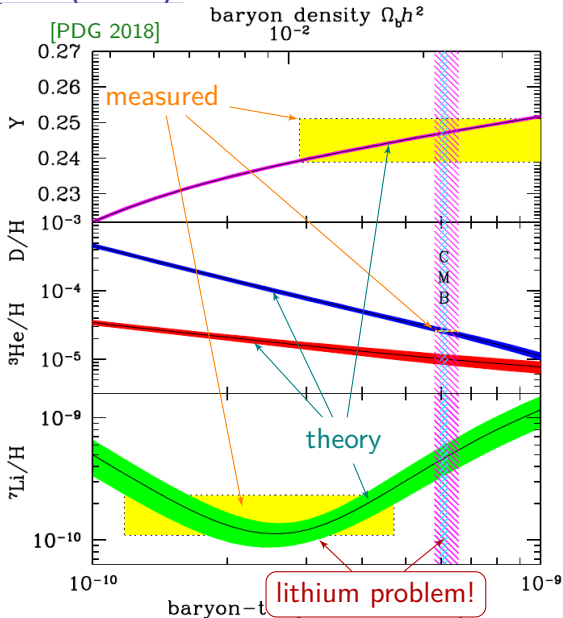
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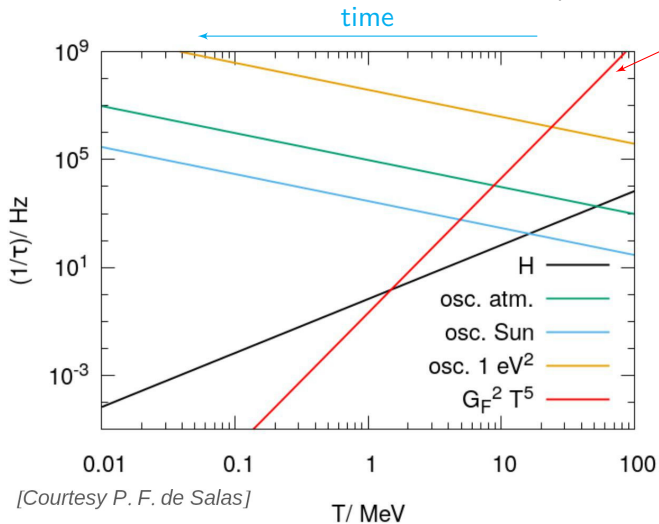
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# Neutrinos in the early Universe

before BBN: neutrinos coupled to plasma ( $\nu_\alpha \bar{\nu}_\alpha \leftrightarrow e^+ e^-$ ,  $\nu e \leftrightarrow \nu e$ )

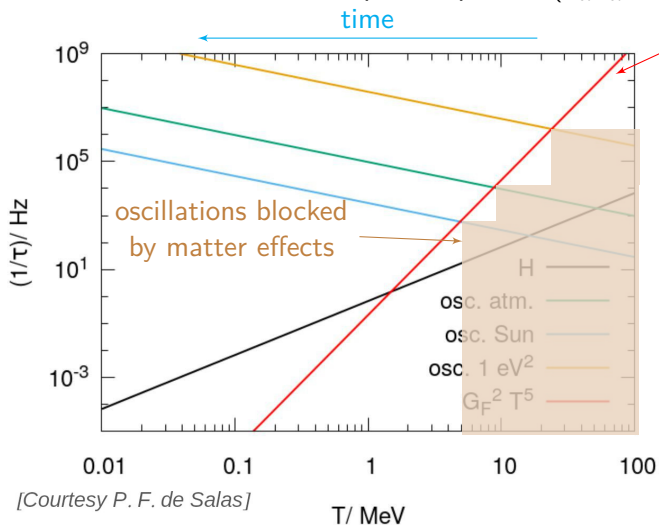


[Courtesy P. F. de Salas]



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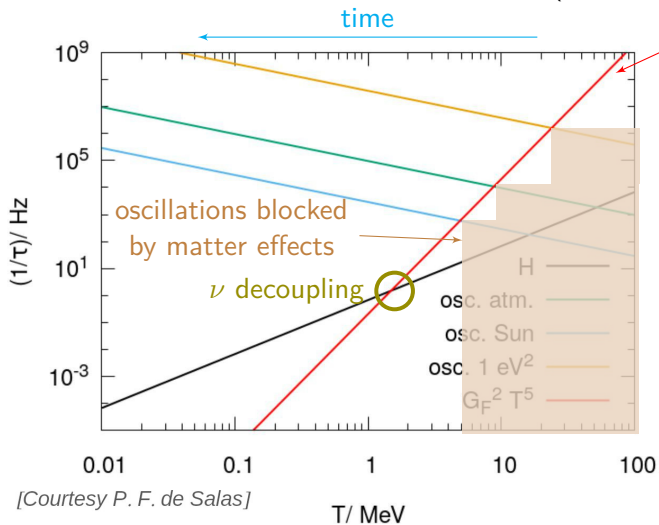
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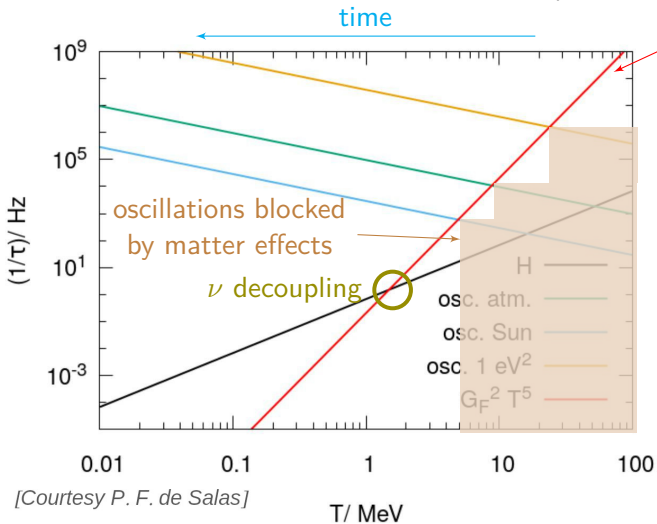


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$$T_\nu \simeq (4/11)^{1/3} T_\gamma$$

after  $e^+ e^- \rightarrow \gamma\gamma$

$f_\nu$ : frozen Fermi-Dirac distribution

Today:

$$T_{\nu,0} = 1.945 \text{ K} \simeq 1.676 \times 10^{-4} \text{ eV}$$

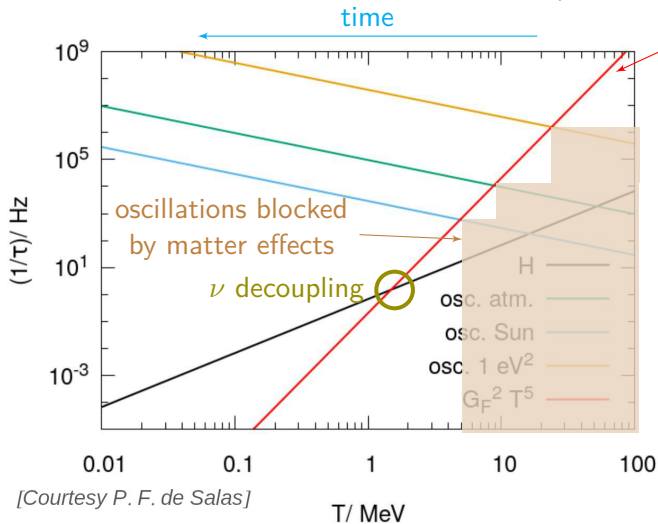
$$\langle E_\nu \rangle \simeq 3.1 T_{\nu,0} \simeq 5 \times 10^{-4} \text{ eV}$$

$$n_0 = n_{\nu,0} = n_{\bar{\nu},0} \simeq 56 \text{ cm}^{-3} \text{ per family}$$

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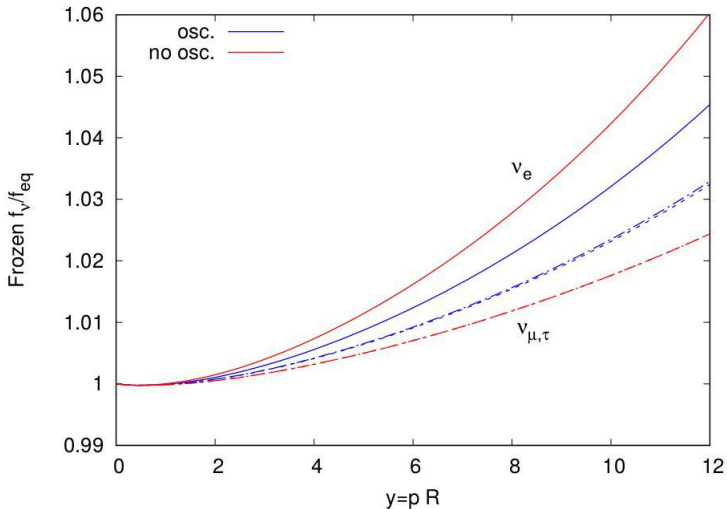
$\nu$  decouple mostly before  $e^+ e^- \rightarrow \gamma\gamma$  annihilation!  
 actually, the decoupling  $T$  is momentum dependent!

distortions to equilibrium  $f_\nu$ !

# Neutrino momentum distribution and $N_{\text{eff}}$

[deSalas+, 2016]

Distortion of the momentum distribution ( $f_{\text{eq}}$ : Fermi-Dirac)



# Neutrino momentum distribution and $N_{\text{eff}}$

$$N_{\text{eff}} = \frac{8}{7} \left( \frac{11}{4} \right)^{4/3} \frac{\rho_\nu}{\rho_\gamma} = \frac{8}{7} \left( \frac{11}{4} \right)^{4/3} \frac{1}{\rho_\gamma} \sum_i g_i \int \frac{d^3 p}{(2\pi)^3} E(p) f_{\nu,i}(p)$$

[Mangano+, 2005]

two-neutrino approximation:

| Case                       | $z_{\text{fin}}$ | $\delta\bar{\rho}_{\nu_e}$ (%) | $\delta\bar{\rho}_{\nu_\mu,\tau}$ (%) | $N_{\text{eff}}$ | $\Delta Y_p$          |
|----------------------------|------------------|--------------------------------|---------------------------------------|------------------|-----------------------|
| No mixing                  | 1.3978           | 0.94                           | 0.43                                  | 3.046            | $1.71 \times 10^{-4}$ |
| No mixing (no QED)         | 1.3990           | 0.95                           | 0.43                                  | 3.035            | $1.47 \times 10^{-4}$ |
| No mixing (all $\nu_e$ )   | 1.3966           | 0.95                           | 0.95                                  | 3.066            | $3.57 \times 10^{-4}$ |
| No mixing (all $\nu_\mu$ ) | 1.3986           | 0.35                           | 0.35                                  | 3.031            | $1.35 \times 10^{-4}$ |

full three-neutrino results (with oscillations):

| Case                            | $z_{\text{fin}}$ | $\delta\bar{\rho}_{\nu_e}$ (%) | $\delta\bar{\rho}_{\nu_\mu}$ (%) | $\delta\bar{\rho}_{\nu_\tau}$ (%) | $N_{\text{eff}}$ | $\Delta Y_p$          |
|---------------------------------|------------------|--------------------------------|----------------------------------|-----------------------------------|------------------|-----------------------|
| $\theta_{13} = 0$               | 1.3978           | 0.73                           | 0.52                             | 0.52                              | 3.046            | $2.07 \times 10^{-4}$ |
| $\sin^2 \theta_{13} = 0.047$    | 1.3978           | 0.70                           | 0.56                             | 0.52                              | 3.046            | $2.12 \times 10^{-4}$ |
| Bimaximal ( $\theta_{13} = 0$ ) | 1.3978           | 0.69                           | 0.54                             | 0.54                              | 3.045            | $2.13 \times 10^{-4}$ |

## ■ How precise is $N_{\text{eff}} = 3.04\dots$ ?

Long list of previous works. . . always less than  $3\nu$  mixing

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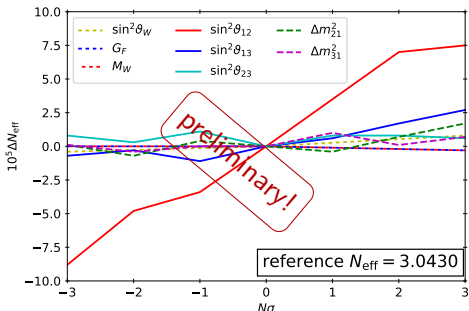
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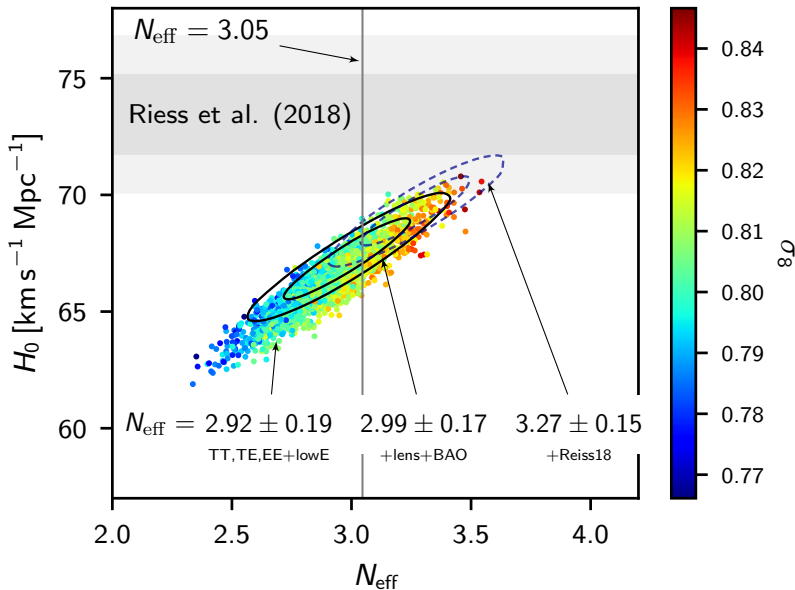
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[in preparation]:  
uncertainty from  
neutrino mixing  
and other  
parameters?

$\Delta N_{\text{eff}} \simeq 10^{-4}$   
at most





# $N_{\text{eff}}$ and BBN

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at  $t \sim 1\text{s}$  to  $t \sim \mathcal{O}(10^2)\text{s}$

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$$\Gamma_{n \leftrightarrow p} \sim G_F^2 T^5 = H \sim \sqrt{g_* G_N} T^2$$

$$T_{\text{fr}} \simeq (g_* G_N / G_F^4)^{1/6}$$

enters

$$n/p = \exp(-Q/T_{\text{fr}})$$

which controls element abundances

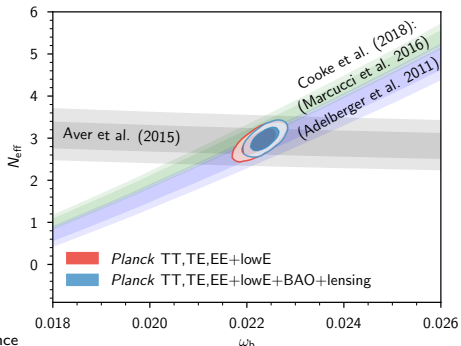
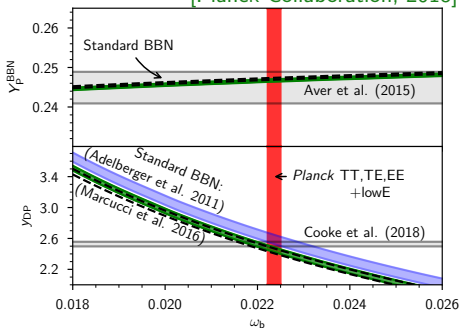
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$G_F$  Fermi constant     $n, p$ : neutron, proton density number  
 $G_N$  Newton constant     $Q = 1.293\text{ MeV}$  neutron-proton mass difference

S. Gariazzo    "Cosmological relic neutrinos, from A to Z"

[Planck Collaboration, 2018]



INT Seattle, 30/01/2020

8/29

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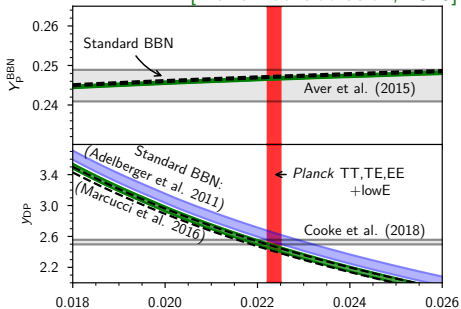
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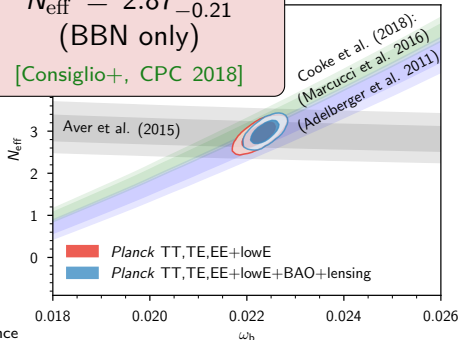
[Planck Collaboration, 2018]



$$N_{\text{eff}} = 2.87^{+0.24}_{-0.21}$$

(BBN only)

[Consiglio+, CPC 2018]



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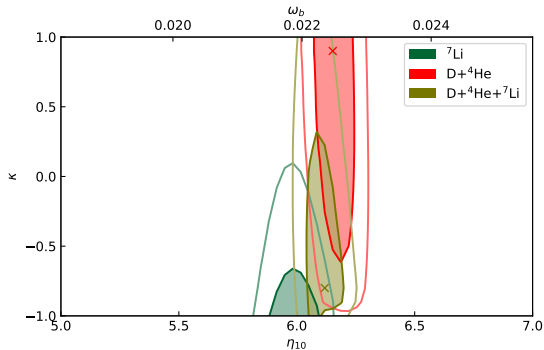
8/29

# B Bosonic neutrinos

(?!? what?)

Based on:

- JCAP 03 (2018) 050





## Motivation

Neutrinos are fermions  $\longrightarrow$  they obey Fermi-Dirac statistics

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electrons

no violations for atomic electrons  
e.g. look for anomalous  $X$ -rays from  
atomic decays

[Goldhaber&Scharff-Goldhaber, 1948]

[Fischbach&Kirsten&Schaeffer, 1968]

[Reines&Sobel, 1974]

...

nucleons

no violations for protons/neutrons  
e.g. look for anomalous star (Sun)  
dynamics or transitions in nuclei

[Plaga, 1989]

[Miljanić+, 1990]

[Borexino, 2004]

...

see detailed discussion in [Dolgov&Smirnov, PLB 2005]

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important: since spin-statistics relation confirmed for electrons,  
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 $A \rightarrow A' + 2\bar{\nu} + 2e^-$  or  $A \rightarrow A' + 2\nu + 2e^+$

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**Fermi-Bose parameter**  $\kappa_\nu$  [Dolgov+, JCAP 2005]

$$f_\nu(E) = \frac{1}{\exp(E/T) + \kappa_\nu}$$

“mixed” distribution!

BE  $\leftarrow \kappa_\nu = -1$   $\xleftrightarrow[\text{MB}]{\kappa_\nu = 0}$   $\kappa_\nu = +1 \rightarrow$  FD

[Barabash+, NPB 2007]:  $\kappa_\nu \gtrsim -0.2$

100% violation excluded [Barabash+, NPB 2007],  
but still 50% admixture of bosonic component allowed

## Constraints on $\kappa_\nu$ from BBN

what can cosmology say about  $\kappa_\nu$ ?

different  $f_\nu(p)$  affects BBN!

statistics factor becomes  $(1 - \kappa_\nu f_\nu)$

$(1 + f_\nu) \rightarrow$  Bose enhancement,

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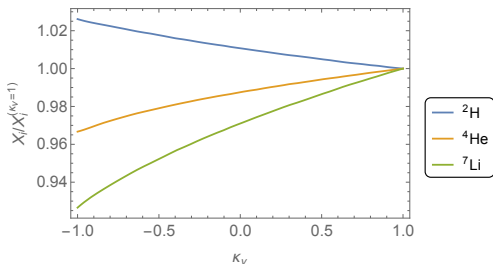
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change of n/p ratio at BBN

[Dolgov+, JCAP 2005]

less He, more D, less Li



deviation from  $\kappa_\nu = 1$   
obtained with a modified version  
of PARthENoPE

[Consiglio+, CPC 2018]



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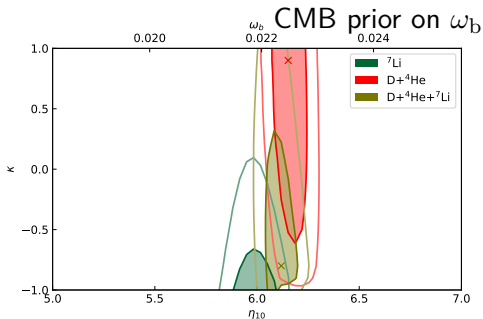
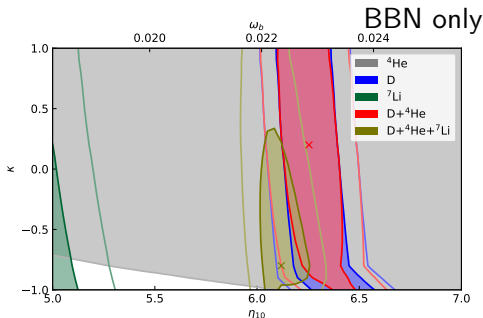
less He, more D, less Li

He or D alone cannot constrain  $\kappa_\nu$

Li problem drives  $\omega_b$  down

and  $\kappa_\nu$  to -1

also when prior on  $\omega_b$  is included



Neutrino densities and  $\kappa_\nu$ 

$$f_\nu(E) = \frac{1}{\exp(E/T) + \kappa_\nu}$$

$\kappa_\nu$  affects

background evolution:

$$\rho_\nu^{\text{rel}} \simeq \frac{g_\nu}{2\pi^2} \int_0^\infty dp p^3 f_\nu(p)$$

bosons:

$$\frac{\pi^2}{30} g_i T^4$$

fermions:

$$\frac{7}{8} \frac{\pi^2}{30} g_i T^4$$

$$\rho_\nu^{\text{nr}} \simeq m_\nu \frac{g_\nu}{2\pi^2} \int_0^\infty dp p^2 f_\nu(p)$$

bosons:

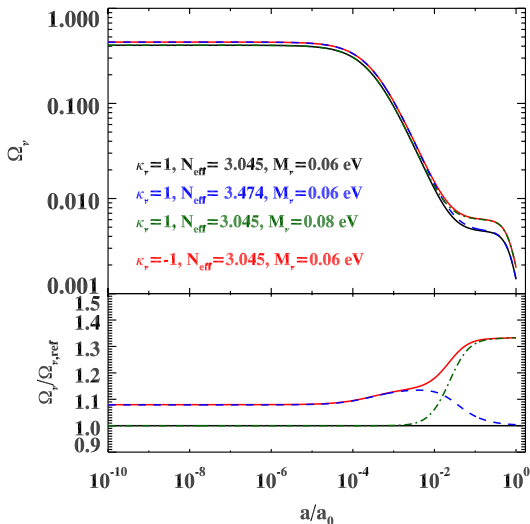
$$\frac{\zeta(3)}{\pi^2} m_\nu g_i T^3$$

fermions:

$$\frac{3}{4} \frac{\zeta(3)}{\pi^2} m_\nu g_i T^3$$

changing  $\kappa_\nu$  “mimics” altering  $N_{\text{eff}}$  or  $\Sigma m_\nu$  (at late or early times)

partial degeneracies with  $N_{\text{eff}}$  and  $\Sigma m_\nu$



need to cover  $\kappa_\nu - \Sigma m_\nu$  degeneracy:  
**vary both!**

degeneracy affects  
 mostly CMB only bounds

with BAO, bound on  $\Sigma m_\nu$  is stronger

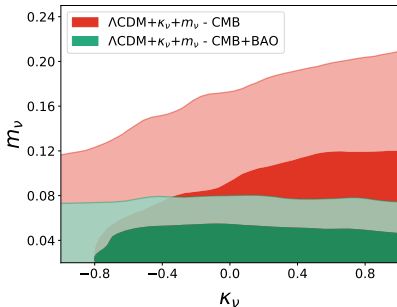
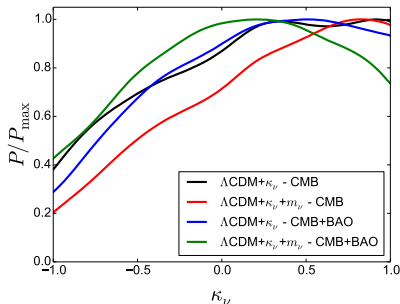
adding radiation (through  $\kappa_\nu$ ) and  $\Omega_\Lambda$  alters  $H_0$  and compensates a bit the larger mass

bounds:  $\kappa_\nu \gtrsim -0.1$  at 68%

$-1 \leq \kappa_\nu \leq 1$  at 95%

$\kappa_\nu = -1$  corresponds to  $N_{\text{eff}} \simeq 3.47$  at early times

inside Planck  $2\sigma$  region!  
 reasonably it's not excluded

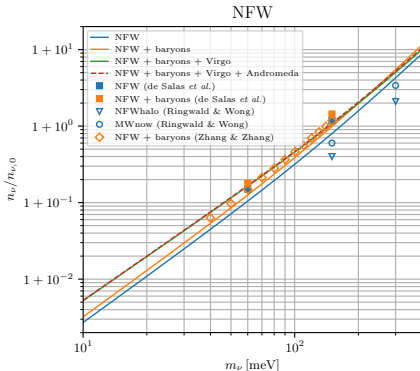


## C

## Clustering in the local Universe

Based on:

- JCAP 09 (2017) 034
- [arxiv:1910.13388](https://arxiv.org/abs/1910.13388)



# $\nu$ clustering with N-one-body simulations

Relic neutrinos are **slow!** [ $c_\nu \sim 160(1+z)(1 \text{ eV}/m_\nu) \text{ km s}^{-1}$ ]

Can be trapped in the gravitational potential of the Milky Way and neighbours

$f_c(m_i) = n_i/n_{i,0}$  clustering factor  $\rightarrow$  How to compute it?

Idea from [Ringwald & Wong, 2004]  $\rightarrow$  **N-one-body** =  $N \times$  single  $\nu$  simulations

$\rightarrow$  each  $\nu$  evolved from initial conditions at  $z = 3$

$\rightarrow$  spherical symmetry, coordinates  $(r, \theta, p_r, l)$

$\rightarrow$  need  $\rho_{\text{matter}}(z) = \rho_{\text{DM}}(z) + \rho_{\text{baryon}}(z)$

Assumptions:

$\nu$ s are independent

only gravitational interactions

$\nu$ s do not influence matter evolution

$(\rho_\nu \ll \rho_{\text{DM}})$

how many  $\nu$ s is "N"?

$\rightarrow$  must sample all possible  $r, p_r, l$

$\rightarrow$  must include all possible  $\nu$ s that reach the MW

(fastest ones may come from  
**several (up to  $\mathcal{O}(100)$ ) Mpc!**)

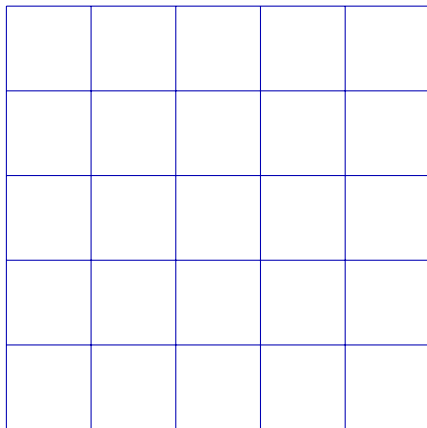
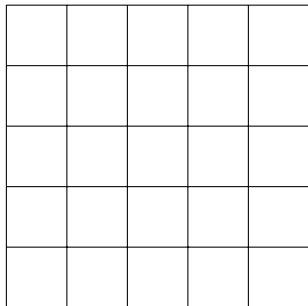
given N  $\nu$ :

$\rightarrow$  weigh each neutrinos

$\rightarrow$  reconstruct final density profile with kernel method from [Merritt & Tremblay, 1994]

## Forward-tracking and back-tracking

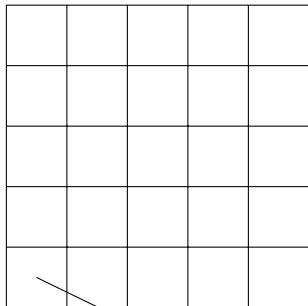
initial phase space,  $z = 4$   $\longrightarrow$  homogeneous Fermi-Dirac distribution



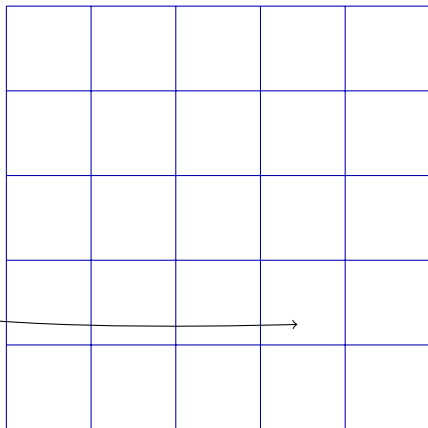
final phase space,  $z = 0$

## Forward-tracking and back-tracking

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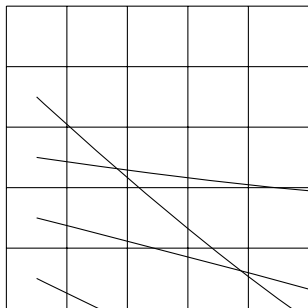
compute final position of each particle



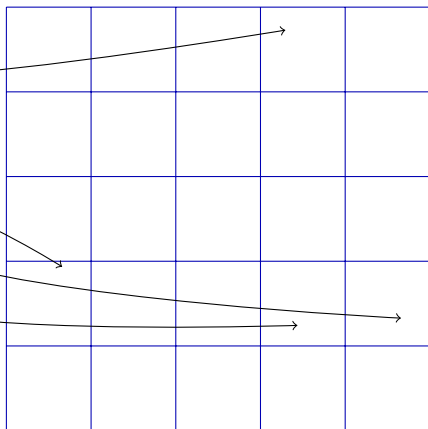
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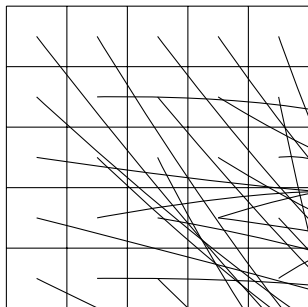


final phase space,  $z = 0$

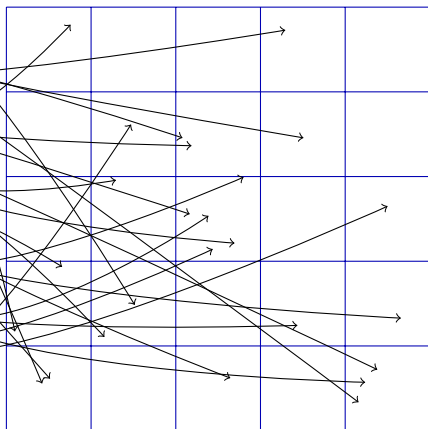


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initial phase space,  $z = 4$   $\longrightarrow$  homogeneous Fermi-Dirac distribution



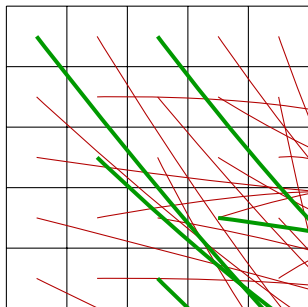
use positions to find neutrino distribution today



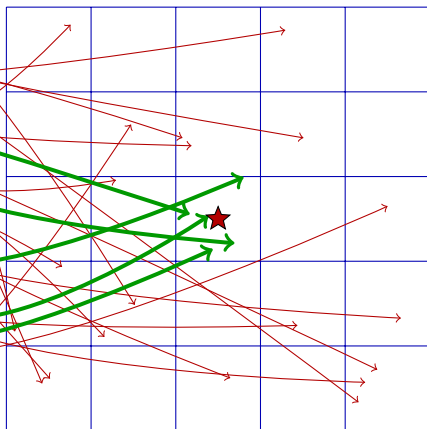
final phase space,  $z = 0$

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only interested in overdensity at Earth? ★

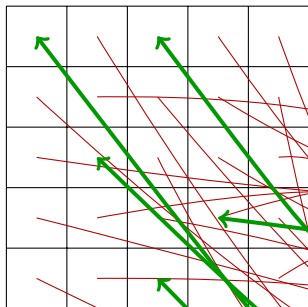


a lot of time is wasted!

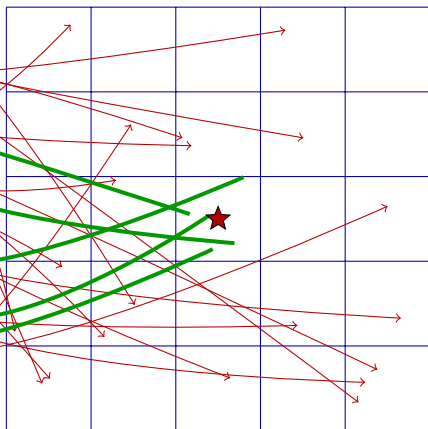
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# Forward-tracking and back-tracking

initial phase space,  $z = 4$   $\longrightarrow$  homogeneous Fermi-Dirac distribution



only interested in overdensity at Earth? ★



a lot of time is wasted!

smarter way: track backwards  
only interesting particles!

final phase space,  $z = 0$

## ■ Advantages of tracking back

First advantage is in computational terms: much less points to compute

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Second advantage: no need to use spherical symmetry!

Forward-tracking

initial conditions need to sample  
1D for position + 2D for momentum  
when using spherical symmetry

with full grid would re-  
quire 3+3 dimensions!

Impossible to relax  
spherical symmetry!

Back-tracking

“Initial” conditions only described  
by 3D in momentum

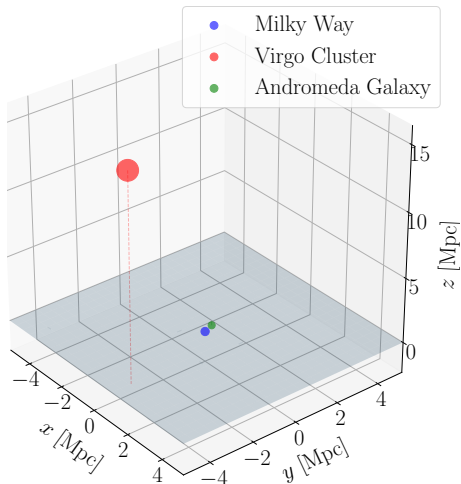
(position is fixed, apart for checks)

can do the calculation with  
any astrophysical setup

## Advantages of tracking back

First advantage is in computational terms: much less points to compute

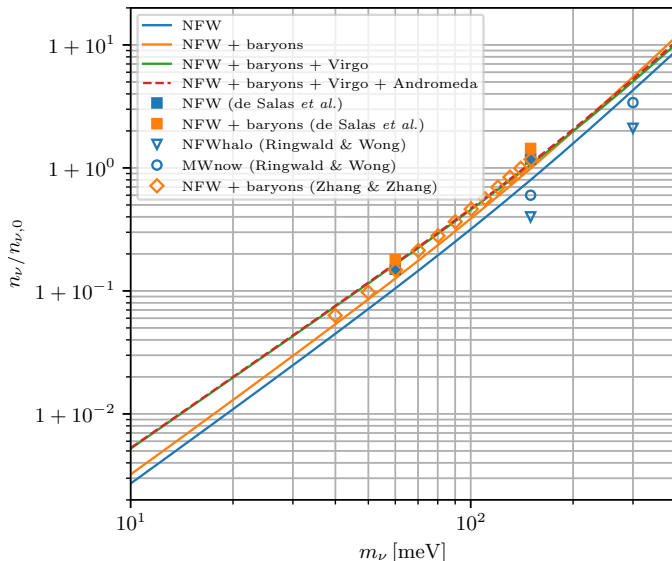
Second advantage: no need to use spherical symmetry!



# Clustering results with back-tracking

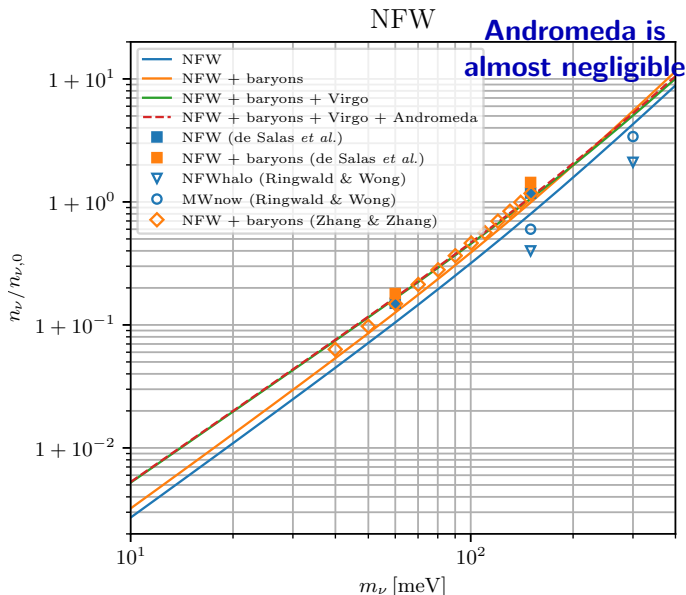
In comparison with previous results:

NFW



# Clustering results with back-tracking

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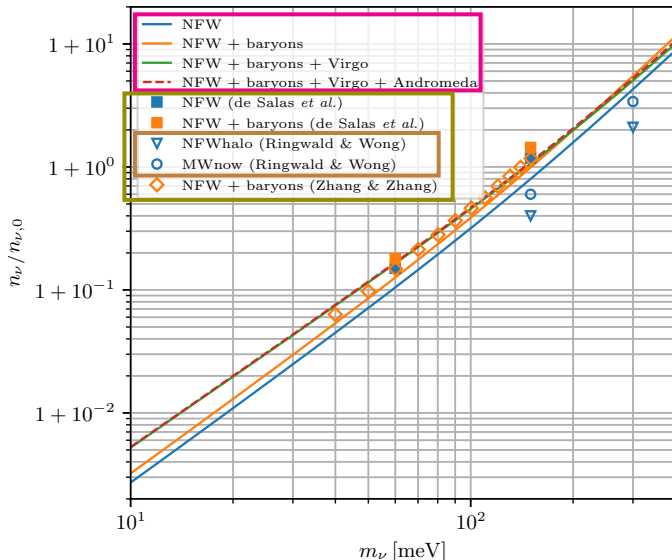




# Clustering results with back-tracking

In comparison with previous results:

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**Warning:** NFW  
is not the same  
for all the cases!

[de Salas+, 2017]

and

[Zhang<sup>2</sup>, 2018]

use  $\gamma \neq 1$ ,  
now we have

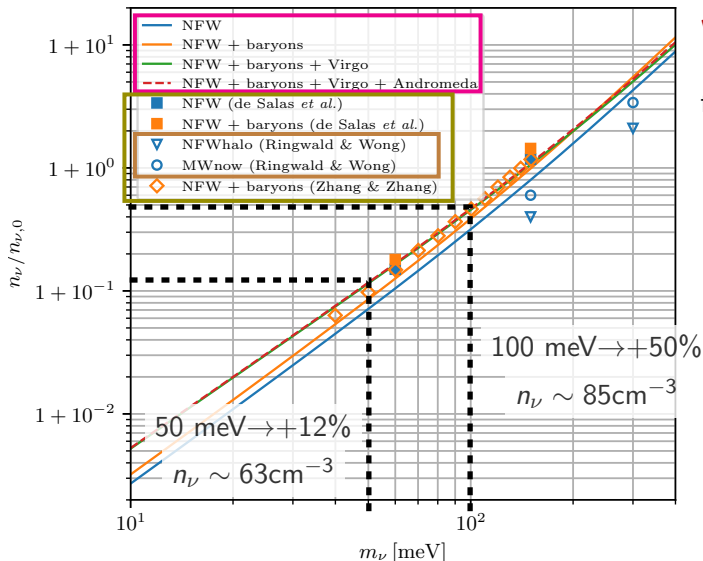
$$\gamma = 1$$

[Ringwald&Wong,  
2004] uses **old**  
parameters

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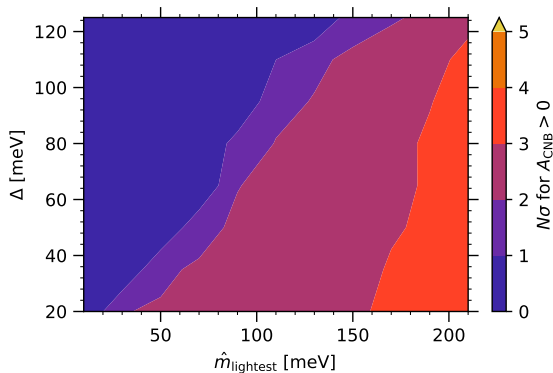
2004] uses old parameters

# D Direct Detection

i.e. currently science-fiction, but in few years...

Based on:

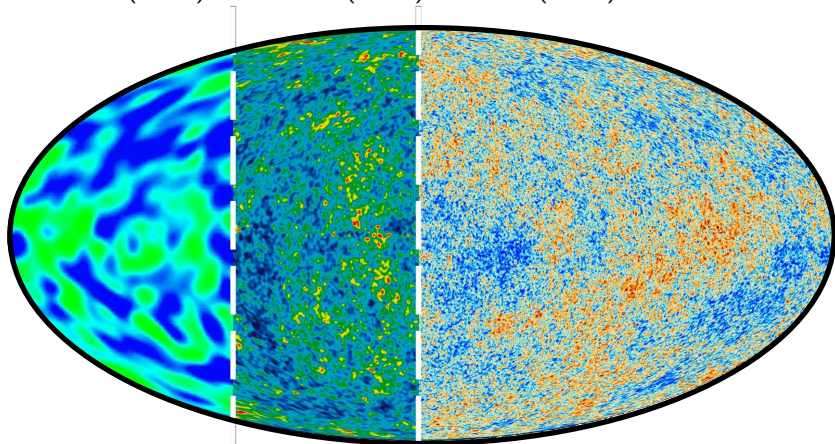
- [arxiv:1808.01892](https://arxiv.org/abs/1808.01892)
- [JCAP 07 \(2019\) 047](https://arxiv.org/abs/1907.047)



# The oldest picture of the Universe

The Cosmic Microwave Background, generated at  $t \simeq 4 \times 10^5$  years

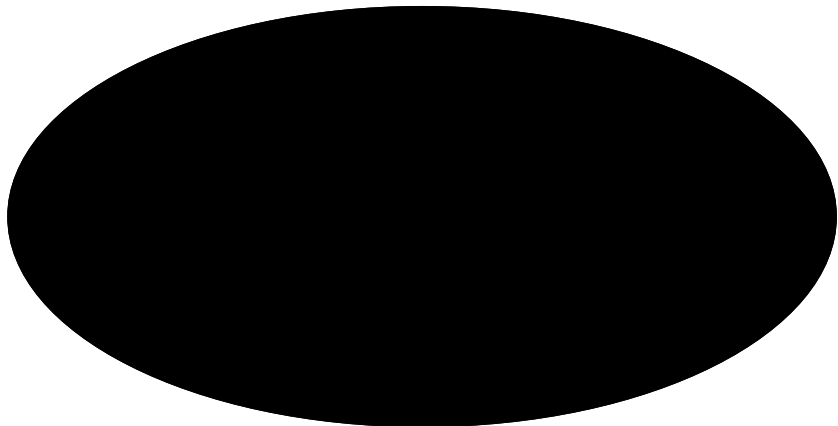
COBE (1992)    WMAP (2003)    Planck (2013)



## The oldest picture of the Universe

The Cosmic Neutrino Background, generated at  $t \simeq 1$  s

... → 2019 → ...



How to directly detect non-relativistic neutrinos?

Remember that  
 $\langle E_\nu \rangle \simeq \mathcal{O}(10^{-4})$  eV today



a process without energy  
 threshold is necessary

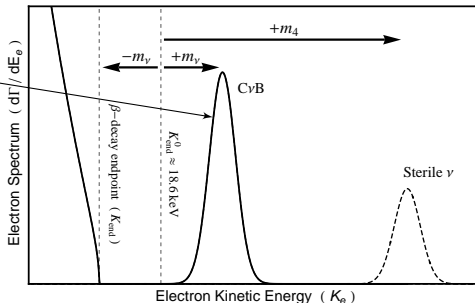
[Weinberg, 1962]: neutrino capture in  $\beta$ -decaying nuclei  $\nu + n \rightarrow p + e^-$

Main background:  $\beta$  decay  $n \rightarrow p + e^- + \bar{\nu}$ !

signal is a peak at  $2m_\nu$   
 above  $\beta$ -decay endpoint

only with a lot of material

need a very good energy resolution



$$\frac{d\tilde{\Gamma}_{\text{CNB}}}{dE_e}(E_e) = \frac{1}{\sqrt{2\pi}\sigma} \sum_{i=1}^{N_\nu} \bar{\sigma} N_T |U_{ei}|^2 n_0 f_c(m_i) \times e^{-\frac{[E_e - (E_{\text{end}} + m_i + m_{\text{lightest}})]^2}{2\sigma^2}}$$

$$\frac{d\Gamma_\beta}{dE_e} = \frac{\bar{\sigma}}{\pi^2} N_T \sum_{i=1}^{N_\nu} |U_{ei}|^2 H(E_e, m_i)$$

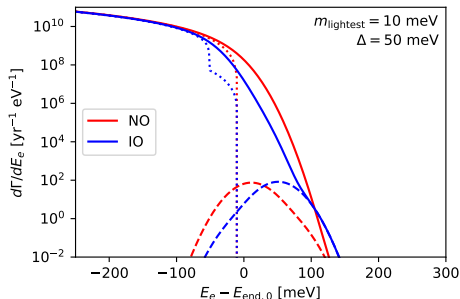
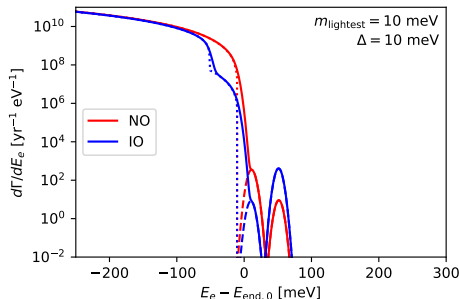
$$\frac{d\tilde{\Gamma}_\beta}{dE_e}(E_e) = \frac{1}{\sqrt{2\pi}\sigma} \int_{-\infty}^{+\infty} dx \frac{d\Gamma_\beta}{dE_e}(x) \exp\left[-\frac{(E_e - x)^2}{2\sigma^2}\right]$$

$\bar{\sigma}$  cross section,  $N_T$  number of tritium atoms in the source (PTOLEMY: 100 g),  $E_{\text{end}}$  endpoint,  $\sigma = \Delta/\sqrt{8 \ln 2}$  standard deviation

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Pontecorvo Tritium Observatory for Light, Early-universe, Massive-neutrino Yield (PTOLEMY)

expected resolution  $\Delta \simeq 0.1 \text{ eV?}$   
 $0.05 \text{ eV?}$

can probe  $m_\nu \simeq 1.4\Delta \simeq 0.1 \text{ eV}$

built mainly for CNB

$M_T = 100 \text{ g}$  of atomic  ${}^3\text{H}$

$$\Gamma_{\text{CNB}} = \sum_{i=1}^3 |U_{ei}|^2 [n_i(\nu_{hR}) + n_i(\nu_{hL})] N_T \bar{\sigma} \sim \mathcal{O}(10) \text{ yr}^{-1}$$

$N_T$  number of  ${}^3\text{H}$  nuclei in a sample of mass  $M_T$      $\bar{\sigma} \simeq 3.834 \times 10^{-45} \text{ cm}^2$      $n_i$  number density of neutrino  $i$

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enhancement from  
 $\nu$  clustering in the galaxy?

enhancement from  
 other effects?

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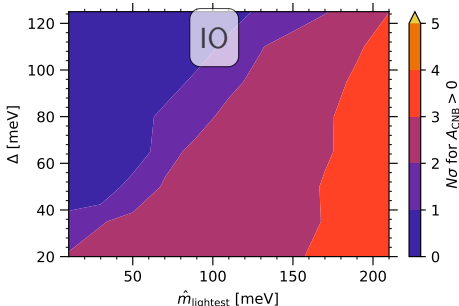
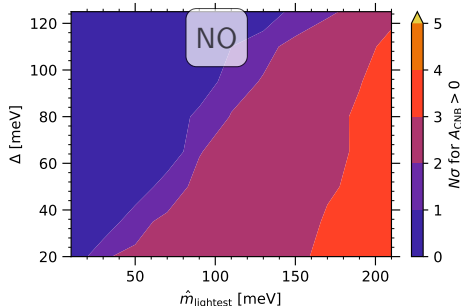
using the definition:

$$N_{\text{th}}^i(\theta) = A_\beta N_\beta^i(\hat{E}_{\text{end}} + \Delta E_{\text{end}}, m_i, U) + \mathbf{A}_{\text{CNB}} N_{\text{CNB}}^i(\hat{E}_{\text{end}} + \Delta E_{\text{end}}, m_i, U) + N_b$$

if  $\mathbf{A}_{\text{CNB}} > 0$  at  $N\sigma$ , direct detection of CNB accomplished at  $N\sigma$

statistical only!

significance on  $\mathbf{A}_{\text{CNB}} > 0$   
as a function of  $\hat{m}_{\text{lightest}}, \Delta$





E-R

(skipping...)

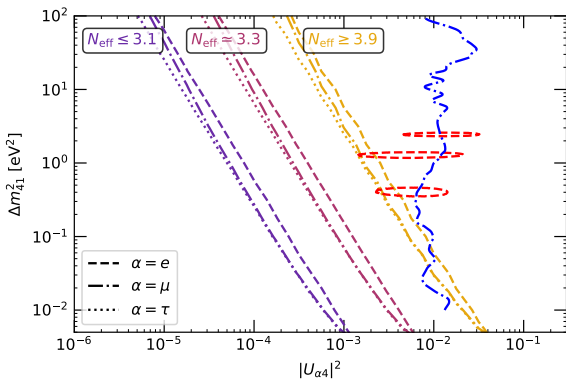
seriously, I cannot go  
through the entire alphabet in 30 minutes!

# S (Light) Sterile neutrinos

let's pretend they exist

Based on:

- JCAP 07 (2019) 014
- in preparation (2)



## Sterile neutrino in the early universe

Four neutrinos  $\rightarrow$  new oscillations in the early Universe

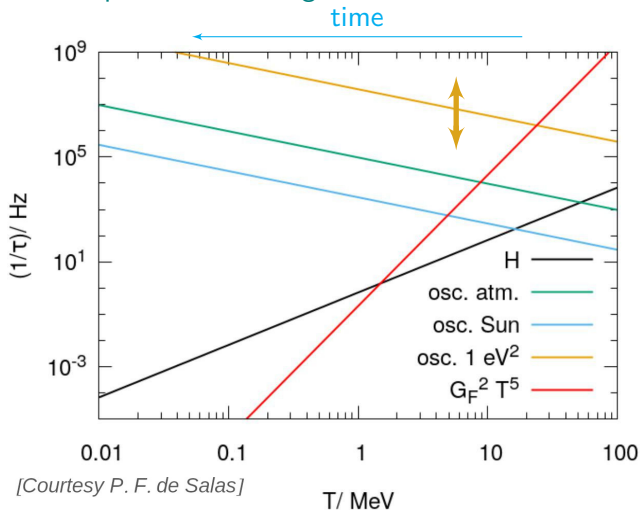
sterile  $\implies$  no weak/em interactions in the thermal plasma

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Four neutrinos  $\rightarrow$  new oscillations in the early Universe

sterile  $\Rightarrow$  no weak/em interactions in the thermal plasma

need to produce it through oscillations, but matter effects may block them



beginning of  
oscillations  
depends on  $\Delta m_{41}^2$

later oscillations  
 $\Downarrow$   
less time before  
 $\nu$  decoupling!

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when are they enough to allow full equilibrium of active-sterile states?

$$0 \longleftarrow \Delta N_{\text{eff}} = N_{\text{eff}}^{4\nu} - N_{\text{eff}}^{3\nu} \longrightarrow \simeq 1$$

no sterile production

active&sterile in equilibrium

$$\frac{\Delta m_{as}^2}{\text{eV}^2} \sin^4(2\vartheta_{as}) \simeq 10^{-5} \ln^2(1 - \Delta N_{\text{eff}}) \quad (1+1 \text{ approx.})$$

[Dolgov&Villante, 2004]

$$\text{e.g.: } \Delta m_{as}^2 = 1 \text{ eV}^2, \sin^2(2\vartheta_{as}) \simeq 10^{-3} \implies \Delta N_{\text{eff}} \simeq 1$$



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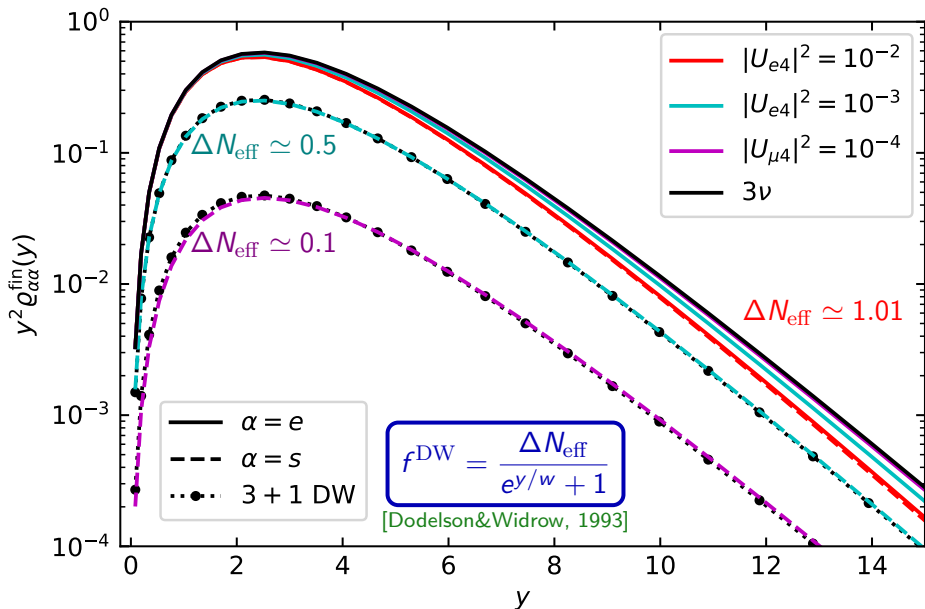
$$\text{e.g.: } \Delta m_{as}^2 = 1 \text{ eV}^2, \sin^2(2\vartheta_{as}) \simeq 10^{-3} \implies \Delta N_{\text{eff}} \simeq 1$$

Full calculation: use numerical code!

FORTran-Evolved Primordial Neutrino Oscillations  
(FortEPiano)

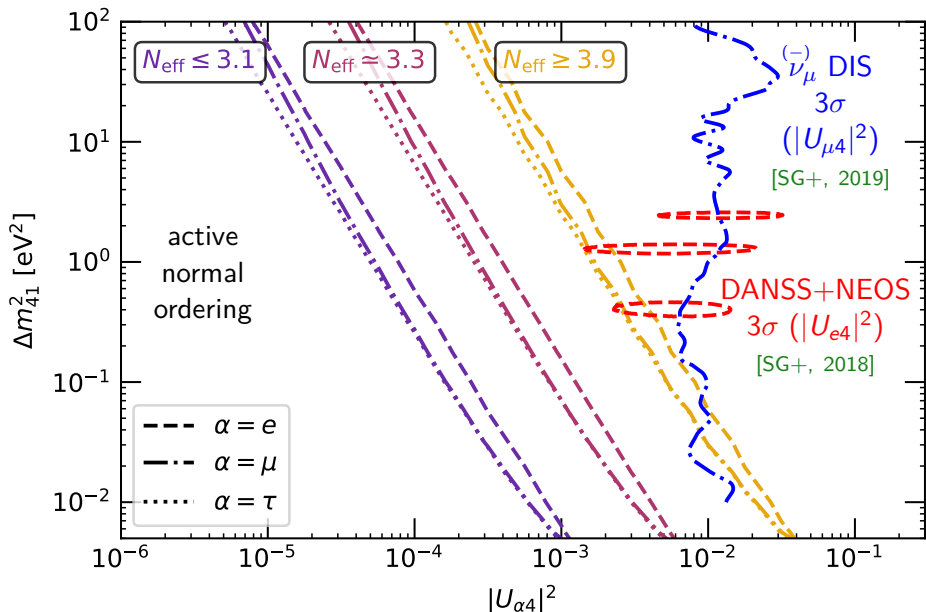
[https://bitbucket.org/ahep\\_cosmo/fortepiano](https://bitbucket.org/ahep_cosmo/fortepiano)

$$\Delta m_{41}^2 = 1.29 \text{ eV}^2, \text{ other } |U_{\beta 4}|^2 = 0, \Delta N_{\text{eff}} = N_{\text{eff}} - N_{\text{eff}}^{\text{active}}$$

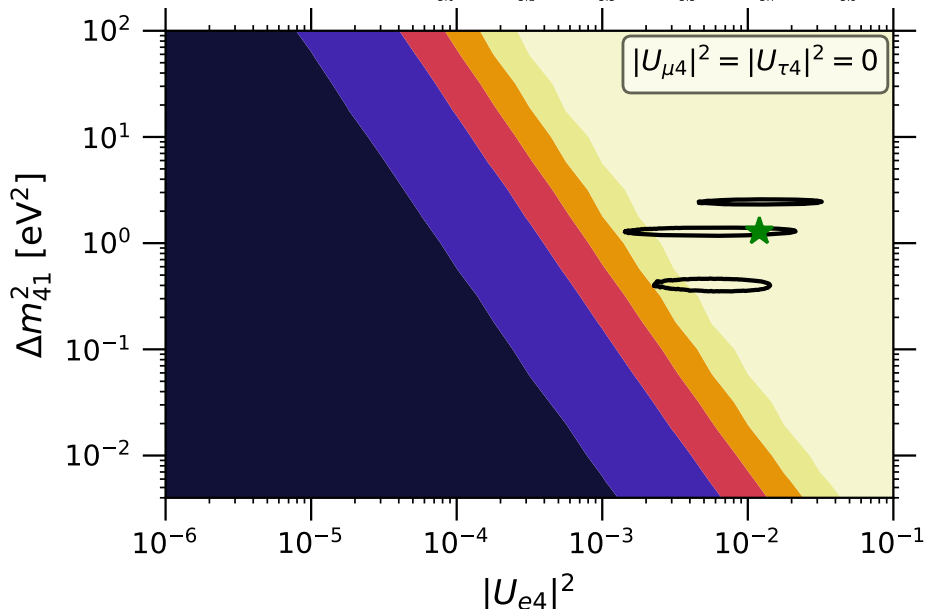
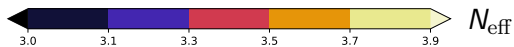


# $N_{\text{eff}}$ and the new mixing parameters

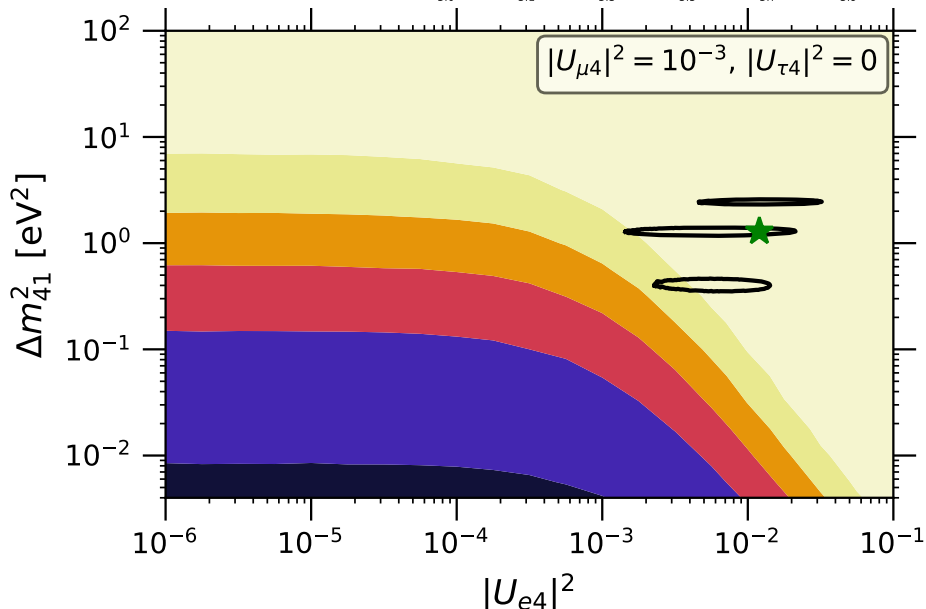
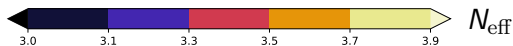
Only vary one angle and fix two to zero: do they have the same effect?



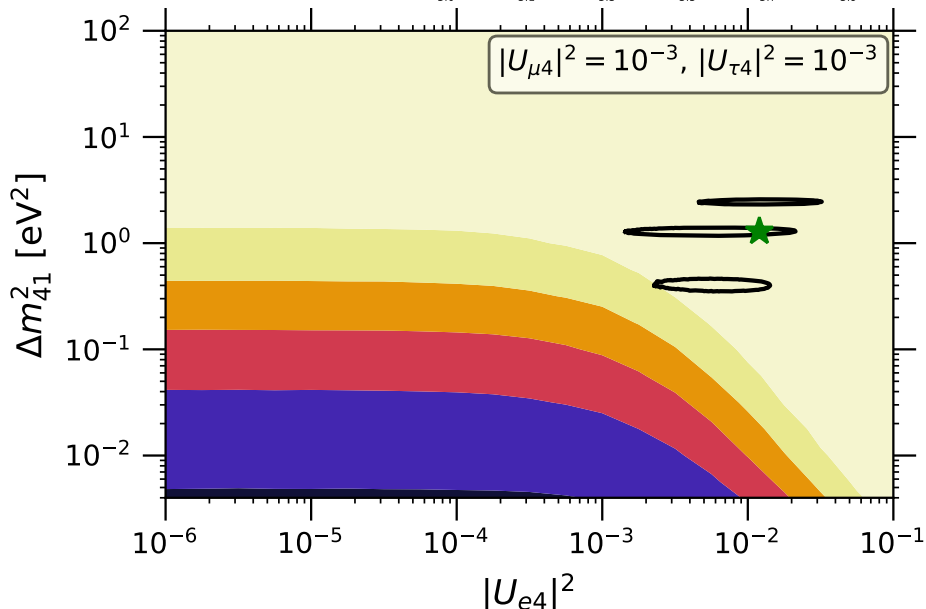
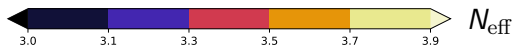
We can vary more than one angle:



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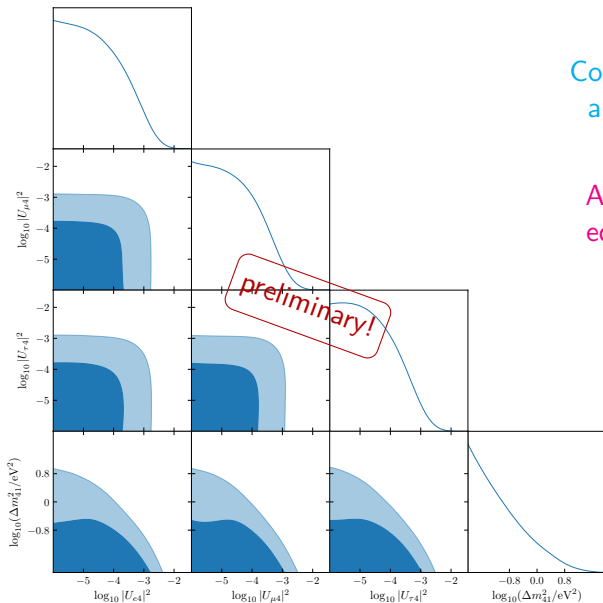


We can vary more than one angle:



# Cosmological constraints on $|U_{\alpha 4}|^2$

Use multi-angle results from FortEPiANO to derive constraints on  $|U_{\alpha 4}|^2$ :



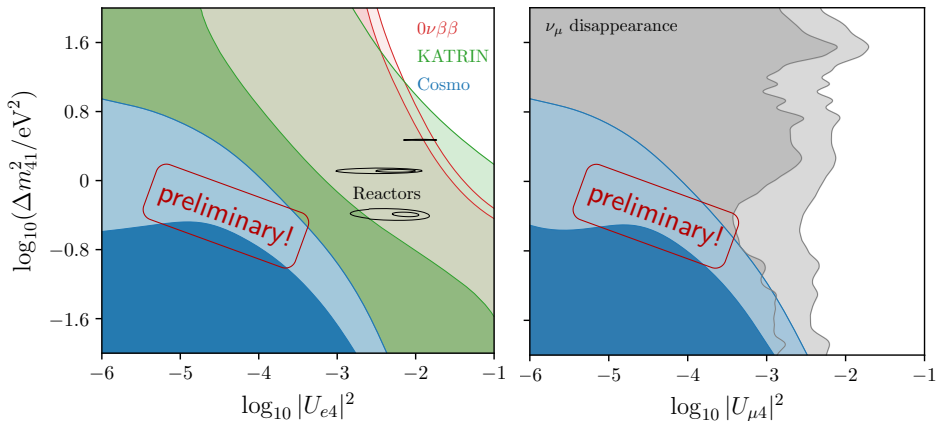
Constraints come from  $N_{\text{eff}}$   
and late-time density  $\Omega_s$

Angles  $|U_{\alpha 4}|^2$  are almost  
equivalent for cosmology

# Comparing constraints

Cosmological constraints are stronger than most other probes

But much more model dependent (as all the cosmological constraints)!

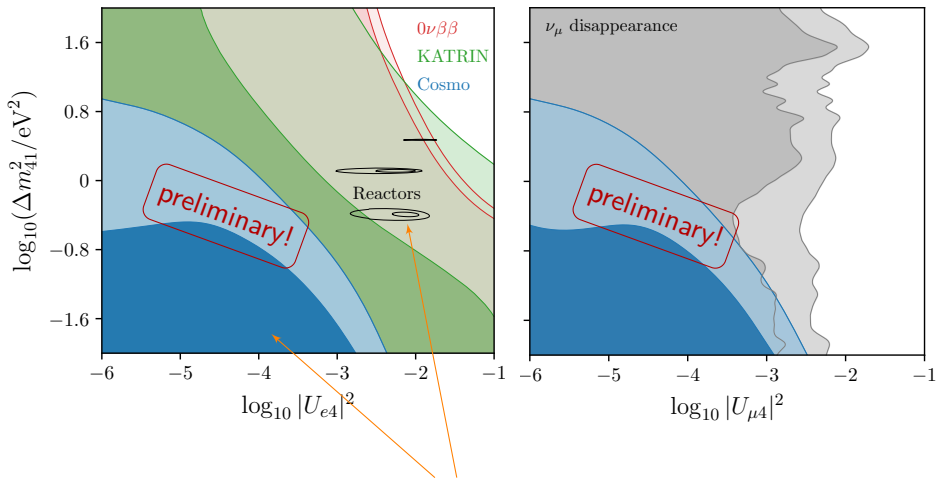




# Comparing constraints

Cosmological constraints are stronger than most other probes

But much more model dependent (as all the cosmological constraints)!



Warning: tension between reactor experiments and CMB bounds!

Z

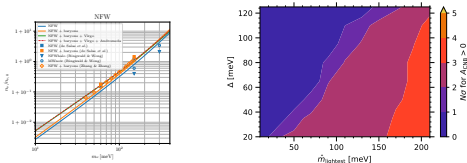
# Conclusions

almost there!

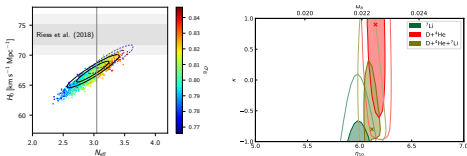


# What do we learn from relic neutrinos?

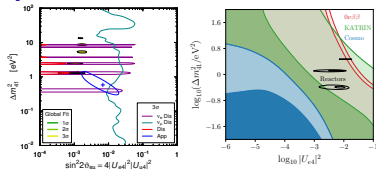
## D Direct detection - wonderful opportunities for the future



## I Indirect probes - what we have now, it's a lot and it will improve

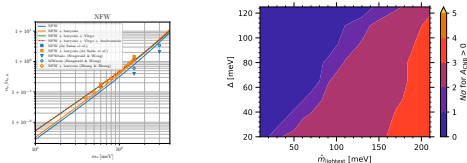


## N New physics - beyond the corner? neutrinos will help us find it!

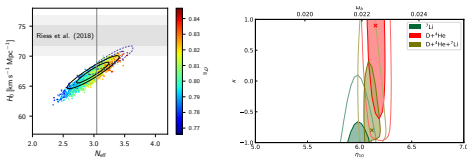


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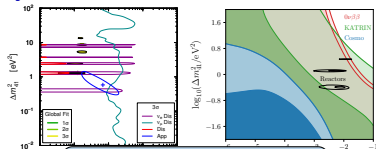
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Thank you!