

# PO Revitalized



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## Revitalized by what?

*Need for PO Ad Usam Delphini, The sudden 'discovery' of the High - Mass problem, support from my buddies, CSR*

## Why revitalized?

*"What giants?" asked Sancho Panza.*

*(Cervantes' Don Quixote)*





# Higgs @ MC: cfr. arXiv:0812.0578

## definition of production $\otimes$ decay:

the MC *produces* a scalar resonance ( $H$ ), with a momentum distributed according to a Breit–Wigner where peak and width are related to the on-shell mass and width of the Higgs boson.

$$\delta(\hat{s} - M_H^2) \rightarrow \begin{cases} \frac{1}{\pi} \frac{M_H \Gamma_H}{(\hat{s} - M_H^2)^2 + (M_H \Gamma_H)^2} & \text{MC@NLO} \\ \frac{1}{\pi} \frac{\hat{s} \Gamma_H / M_H}{(\hat{s} - M_H^2)^2 + (\hat{s} \Gamma_H / M_H)^2} & \text{Pythia/POWHEG} \end{cases}$$

where  $M_H, \Gamma_H$  are the on-shell mass and width.



# Complex pole scheme → approximations?

## Higgs-boson propagator $\iff$ Breit–Wigner distribution

Given the complex pole (nothing more than a parametrization)

$$s_H = \mu_H^2 - i \mu_H \gamma_H$$

perform the **transformation** (**Bar** – scheme)

$$\overline{M}_H^2 = \mu_H^2 + \gamma_H^2 \quad \mu_H \gamma_H = \overline{M}_H \overline{\Gamma}_H$$

It follows the remarkable identity:

$$\frac{1}{\hat{s} - s_H} = \left(1 + i \frac{\overline{\Gamma}_H}{\overline{M}_H}\right) \left(\hat{s} - \overline{M}_H^2 + i \frac{\overline{\Gamma}_H}{\overline{M}_H} \hat{s}\right)^{-1},$$



## Question time

### ComplexPole FAQ

**Q** What is  $\mu_H$ ?

**A** An input parameter as the OS mass; QFT doesn't provide an answer for them.

**Q** Can I compute  $\gamma_H$ ?

**A** Yes,  $\gamma_H(\mu_H)$ , more or less as you compute  $\Gamma_H^{\text{OS}}(M_H^{\text{OS}})$ .

**Q** What is the difference?

**A** OS quantities are ill defined.

**Q** Are they related?

**A** Yes, in PT which – however – breaks down in the HM region



## From Complex to Real: a fact of life

What is the *common sense* definition of mass and width of an unstable particle?

### Options

$$S_H = \mu_H^2 - i \mu_H \gamma_H,$$

$$S_H = \left( \mu'_H - \frac{i}{2} \gamma'_H \right)^2,$$

$$S_H = \frac{\bar{M}_H^2 - i \bar{\Gamma}_H \bar{M}_H}{1 + \bar{\Gamma}_H^2 / \bar{M}_H^2}$$

### which one is

- correct,
- approximate,
- closer to the **exp** peak
- ... ?







## Dialogue Concerning the Two Chief World Systems: Salviati, Sagredo, Simplicio

**TH** How do you want to proceed? Full scenario?

**EX** No, we separate Higgs production and decay, and MCs implement an ad-hoc Breit-Wigner

**TH** Hope you are not going for high-mass!

**EX** Up to 600 GeV via ggF(+VBF) ( $H \rightarrow WW \rightarrow l\nu qq$ )

**TH** Then you got problems, the three bricks need a proper definition:

- ① The full  $S$ -matrix element is  $S \oplus B$
- ②  $S$  is [ production  $\otimes$  propagation  $\otimes$  decay ]
- ③ each of them must be defined consistently

**EX** We are working with a mass spectrum peak, but what about the on-shell mass peak? Are there other definitions?

**TH** This I told you before



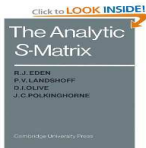
## High-Mass

What is the physical meaning of an *heavy Higgs* search?

## New Physics

- An Higgs above 600 GeV requires new physics at 1 TeV;
- This is based on partial-wave unitarity but should not be taken quantitatively or too literally:
  - With Fermi theory the unitarity bound is at  $\mathcal{O}(10^2)$  GeV and we have been lucky that the vector boson scale is 80–90 GeV
- Violation of unitarity bound  $\leftrightarrow J = 0, 1$ , resonances
  - but there is no way to predict their masses, simply scaling the  $\pi-\pi$  system gives you the 1 TeV ballpark.
- Anyway, it would be a good idea to address it as *search* for  $J = 0, 1$  *heavy new resonances* decaying into  $VV \rightarrow 4f$ .





## Do we want to go back to the Sixties?

- This is not anymore our beloved Lagrangian QFT landmark;
- it is the territory of other keywords:
  - *unitarized partial waves*,
  - *N/D formalism*, etc, etc.
- For high-mass VBF should be a *Fitter* more than a *Calculator*.
  - one should be more interested in a model-independent parametrization of  $VV$  scattering than in its SM determination



[14] of  $WZ$  and  $W^\pm W^\pm$  channels at hadron colliders.

How reliable is the simple  $N/D$  result for a vector resonance? As already mentioned, the full  $N/D$  for the vector channel has no solution because of bad high-energy behavior. This means that  $N/D$  iteration would not converge and our simple  $N/D$  solution should be regarded as the first term of an asymptotic series. On the other hand, the vector coupling is reasonably small even for relatively large vector masses, as may be seen from the narrowness of the resonance compared to the scalar. This implies

that the single iteration can be a good approximation. If one measures the convergence as we did for the scalar case by the condition that  $D_{11}(-m_V^2)$  deviates from 1 by within, say, 15%, one finds  $m_V < 2.2$  TeV.

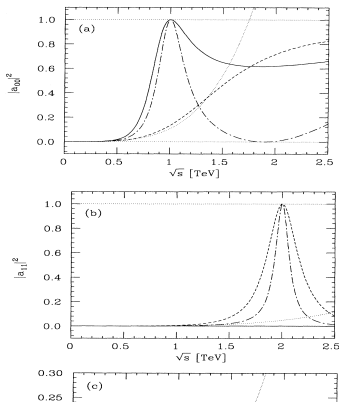
#### IV. COMPARISON WITH DIFFERENT APPROACHES

Various methods [15] have been used to obtain unitary amplitudes. The most widely used methods are  $K$  matrix unitarization and the Padé approximant. Here we compare these methods with our simple  $N/D$  approach. The  $N/D$  language provides a convenient basis for the comparison, since it allows us a unified description of all these methods. Since elastic unitarity for the partial wave amplitude  $a$  is equivalent to Eq. (3), any unitarized amplitude can be written in the form  $a = N/D$  with  $N$  real and  $\text{Im}D = -N$  (in the physical region  $s > 0$ ). Various unitarization schemes correspond to different choices of  $N$  and  $\text{Re}D$ .

Suppose that we have an approximation amplitude  $a_0$  which is real and therefore nonunitary. The  $K$  matrix unitarization is equivalent to setting  $N = a_0$  and  $\text{Re}D = 1$  (with  $\text{Im}D = -N$ ). Though being unitary, the  $K$ -matrix-unitarized amplitude does not necessarily satisfy analyticity [16]. On the other hand, in the simple  $N/D$  approach, we set  $N = a_0$  and calculate  $D$  by a dispersion relation. The result always gives an analytic amplitude.

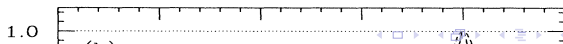
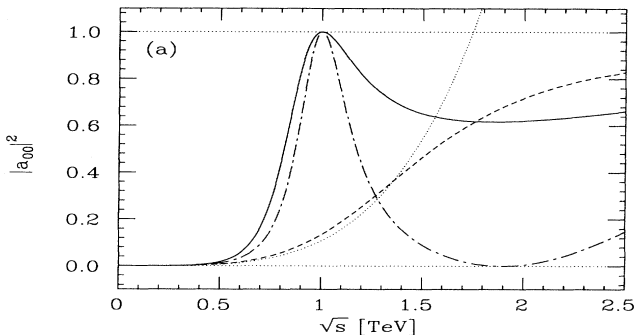
The Padé approximant can be used if the first two terms of an expansion (in coupling constant or energy) are known. For a real amplitude of the form  $a_0 = a_\#(1 + \delta)$ , the  $[1,1]$  Padé is equivalent to  $N = a_\#$ ,  $\text{Re}D = 1 - \delta$ . Analyticity of the result is again not obvious. [If the  $K$  matrix is used for the same amplitude, one finds  $N = a_\#$ ,  $\text{Re}D = 1/(1 + \delta)$ .]

These unitarization methods are often used [17–20] in the chiral Lagrangian approach. The chiral Lagrangian for  $ww$  scattering is nothing but low-energy expansion with the constraint of the low-energy theorem. One starts with the expansion to  $O(s^2)$ :  $a_0(s) = As(1 + Cs)$ , where  $A$  is fixed by the low-energy theorem and  $C$  depends on the parameters of the chiral expansion. A unitary amplitude is obtained by setting  $N = As$ ,  $\text{Re}D = 1 - Cs$  (Padé) or  $\text{Re}D = 1/(1 + Cs)$  ( $K$  matrix). These two methods are known to give very different re-



[14] of  $WZ$  and  $W^\pm W^\pm$  channels at hadron colliders.

How reliable is the simple  $N/D$  result for a vector resonance? As already mentioned, the full  $N/D$  for the vector channel has no solution because of bad high-energy behavior. This means that  $N/D$  iteration would not converge and our simple  $N/D$  solution should be regarded as the first term of an asymptotic series. On the other hand, the vector coupling is reasonably small even for relatively large vector masses, as may be seen from the narrowness of the resonance compared to the scalar. This implies



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# N/D in a nutshell: cfr. Phys.Rev.D48:3055-3061,1993

$$a(s) = \frac{N(s)}{D(s)}$$

- Elastic unitarity + analiticity

$$\text{Im } D(s) = -N(s), \quad s > 0$$

$$D(s) = 1 - \frac{s}{\pi} \int_0^\infty d\tau \frac{N(\tau)}{\tau(\tau - s)}$$

- Define the width from peak  $M_S$

$$a(s) \sim - \frac{M_S \Gamma_S}{s - M_S^2 + i M_S \Gamma_S}, \quad \Gamma_S = - \frac{N(M_S^2)}{M_S \text{Re } D'(M_S^2)}$$

- $a(s)$  is a partial wave
- Invent  $N$ ,
- derive  $D$
- get a plot
- baptize your resonance



## Or you go Higgsless

There have been several alternatives proposed. All of the alternative mechanisms use strongly interacting dynamics to produce a vacuum expectation value that breaks EWSB. A partial list of these alternative mechanisms includes:

- Technicolor models
- Extra-dimensional Higgsless models
- Models of composite  $W, Z$  vector bosons
- Top quark condensate
- Unitary Weyl gauge
- Asymptotic safety of some nonlinear sigma models
- Regular Charge Monopole Theory
- Ribbon model



# About interference

## Hot @ High *mass*

$$A_T = A_{LO}^S + \exp(i\theta_s) A_{NLO}^S + \exp(i\theta_b) A_{LO}^B$$

- LO = lowest (non zero) order
- S= signal, B= background,  $\theta_{s,b}$  = phases.

## What's available?

•  $|A_{LO}^S|^2, |A_{NLO}^S|^2 + \dots, |A_{LO}^B|^2$

?  $|A_{LO}^S + \exp(i\theta_b) A_{LO}^B|^2 \rightsquigarrow$  LO interference

!  $\sigma_{NLO} = K \sigma_{LO}$  does not imply  $\text{interference}_{NLO} = K \text{interference}_{LO}$





## About interference II

**For**

$$\sqrt{s} = 14 \text{ TeV } M_H = 600 \text{ GeV}$$

$$\begin{aligned} \sigma(gg \rightarrow l\nu l'\nu') &= 60 \text{ fb} \\ \sigma_c(gg \rightarrow l\nu l'\nu') &= 1.4 \text{ fb} \\ \sigma(gg \rightarrow H) &= 2.4 \text{ pb} \\ \text{BR}(H \rightarrow l\nu l'\nu') &= 7 \cdot 10^{-2} \end{aligned}$$

- Cut dependence?  $\implies$
- T. Binoth et al.  $\implies$

- $I = \pm 90 | \cos \theta | \%$
- $I_c = \pm 20 | \cos \theta | \%$
- $\theta = \text{B/S (unknown) phase}$   
 $\rightsquigarrow$  Action needed
- Exact  
 $I(I_c) = -0.7\% (10.6 \%)$   
at 200 GeV.
- Exact  
 $I(I_c) = -5.2\% (-3.8 \%)$   
at 140 GeV.

## Example

$$\sigma (gg(\rightarrow H) \rightarrow WW \rightarrow l\bar{\nu}l'\nu')$$

arXiv:hep-ph/0611170v1 14 TeV

sel.	$\sigma(S)$ [fb]	$\sigma(B_{gg})$ [fb]	$\sigma(S + B_{gg})$ [fb]	$\approx \theta_b$
tot	75.4	60.0	134.5	90.4°
bkg	1.67	1.74	3.41	84.5°



## About interference III

### Message

For  $I$  we need amplitudes  $A$  (interfacing different codes?) but codes have  $|A|^2$  and  $I = 2 \operatorname{Re}(A_S A_B^*)$

$$M_H < 2 M_t$$

- $A_S$  from EFT ☹
- $A_B$  ☹
- assembling  $A_{S+B}$  ☹

$$M_H > 2 M_t$$

- $A_S$  ☹
- finite width effect ☹

### consistency

$S$  known at NLO,  $B$  at LO  $\rightsquigarrow I = I_{\text{app}}$  at NLO



## Moving towards modernity

### Which

best language to simulate intuition?

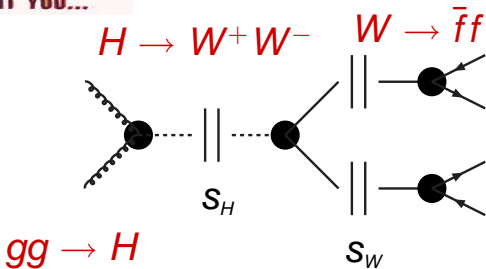
- production of on-shell Higgs
- intermediate Breit–Wigner
- Higgs on-shell decay
- *production* of a Higgs at its complex pole
- Dyson resummed propagator
- Higgs *decay* at its complex pole

### Right column

cannot yet produce fast answers, that's why the PO oblivion



# LHC example of POs



# Subliminal messaging

## @ Low masses

CPs are for high-precision physics (after my retirement?)

## @ High masses

CPs also tell us that it is difficult to accommodate a heavy Higgs;  $W, Z, H$  and  $t$  complex poles are solutions of a (coupled) system of equations

$$f_i(s_W, s_Z, s_H, s_T) = 0, \quad i = W, Z, H, t$$

but for  $W, Z$  and (partially)  $t$  we can compare with the *exp* CPs





$\gamma_H$  [GeV] for  $\gamma_{W,t}$  fixed and complete calculation

$\mu_H$ [GeV]	$\gamma_{W,t}$ fixed	complete
200	1.264	1.262
	2.093	1.932
	1.481	1.171
250	3.369	3.364
	2.093	1.822
	1.481	0.923
300	7.721	7.711
	2.093	1.738
	1.481	0.689

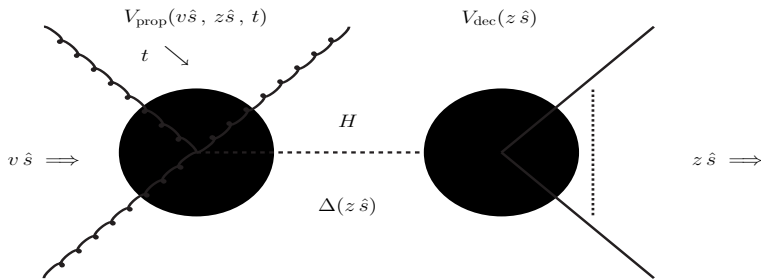
# Bar-scheme vs OS-scheme

$\mu_H$ [GeV]	$\Gamma_H^{\text{OS}}$ [GeV] (YR)	$\gamma_H$ [GeV]	$\overline{M}_H$ [GeV]	$\overline{\Gamma}_H$ [GeV]
200	1.43	1.26	200	1.26
400	29.2	24.28	400.7	24.24
600	123	102.17	608.6	100.72
700	199	159.54	<b>717.95</b>	<b>155.55</b>
800	304	228.44	<b>831.98</b>	<b>219.66</b>
900	449	307.63	<b>951.12</b>	<b>291.09</b>





# Scales



$$\Rightarrow \sigma_{gg \rightarrow H+X}(v\hat{s}, \hat{t}, s_H) \frac{(z\hat{s})^2}{|z\hat{s} - s_H|^2} \frac{\Gamma_{H \rightarrow f}(s_H)}{|s_H|^{1/2}}$$



# What is signal?

## Complete Amplitude (simplified, no $p_T$ )

$$A(s) = V_{\text{prod}}(s) \Delta_{\text{prop}}(s) V_{\text{dec}}(s) + A_{\text{bckg}}(s)$$

- $V_{\text{prod}} \longleftarrow gg \rightarrow H$
- $V_{\text{dec}} \longleftarrow H \rightarrow \gamma\gamma, 4f \text{ etc.}$

If no attempt is made to *split*  $A(s)$  no ambiguity arises but, usually, the two components are known at different orders.

- Ho to *define* the **Signal**?



## Options

- at present **ONBW**

$$A_{\text{sig}}(s) = V_{\text{prod}}(\mu_H^2) \Delta_{\text{prop}}(s) V_{\text{dec}}(\mu_H^2)$$

$$\Delta_{\text{prop}}(s) = \text{Breit-Wigner}$$

- in general violates gauge invariance, neglects the Higgs off-shellness and introduces an *ad hoc* BW
- Also possible **OFFBW**

$$A_{\text{sig}}(s) = V_{\text{prod}}(s) \Delta_{\text{prop}}(s) V_{\text{dec}}(s)$$

$$\Delta_{\text{prop}}(s) = \text{Breit-Wigner}$$

- in general violates gauge invariance, and introduces an *ad hoc* BW



## Options

- improving **ONP**

$$A_{\text{sig}}(s) = V_{\text{prod}}(\mu_H^2) \Delta_{\text{prop}}(s) V_{\text{dec}}(\mu_H^2)$$

$$\Delta_{\text{prop}}(s) = \text{propagator}$$

- in general violates gauge invariance and neglects the Higgs off-shellness
- Also possible **OFFP**

$$A_{\text{sig}}(s) = V_{\text{prod}}(s) \Delta_{\text{prop}}(s) V_{\text{dec}}(s)$$

$$\Delta_{\text{prop}}(s) = \text{propagator}$$

- in general violates gauge invariance



## Options

- **Ideal CPP**

$$A_{\text{sig}}(s) = V_{\text{prod}}(S_H) \Delta_{\text{prop}}(s) V_{\text{dec}}(S_H)$$

$$\Delta_{\text{prop}}(s) = \text{propagator}$$

- Only the pole, the residue and the remainder of  $A(s)$  are gauge invariant!
- Furthermore **CPP** allows to identify POs

$$\sigma_{\text{prod}} \quad \Gamma_{\text{dec}}$$

- by putting in one-to-one correspondence robust theoretical quantities and experimental data



# What is background?

## Consistent definition of $S, B$

$$A_{\text{sig}}(s) = \frac{V_{\text{prod}}(s_H) V_{\text{dec}}(s_H)}{s - s_H}$$

$$A_{\text{bckg}}(s) = A_B(s) + V_{\text{prod}}(s_H) V_{\text{dec}}^R(s) + V_{\text{dec}}(s_H) V_{\text{prod}}^R(s)$$

$$V(s) = V(s_H) + (s - s_H) V^R(s)$$

**!** the remainder  $\implies$  background



## Conclusion?

- What is the best choice for heavy Higgs NLO MCs?
- Well,

*that all true believers break their eggs at the convenient end.*

*Jonathan Swift's Travels into Several Remote Nations of the World*

*But nobody touch QFT. Someone do something quick,  
before we're all killed. El sueño de la razón produce  
monstruos*

*Francisco Goya*



## Short Dialogue of Natural Philosophy

**EX** In trying to understand MC for a heavy Higgs, I am increasingly suspicious of theoretical treatment for such cases, including cross sections.

**TH** God could have made the universe any way he wanted to and still made it appear to us the way it does

(*Galileo, Dialogo sopra i due massimi sistemi del mondo*)

among THs: "Who shall go in?" said one. "Not I," said the other. "Nor I," rejoined his companion but numbers are here it appears!



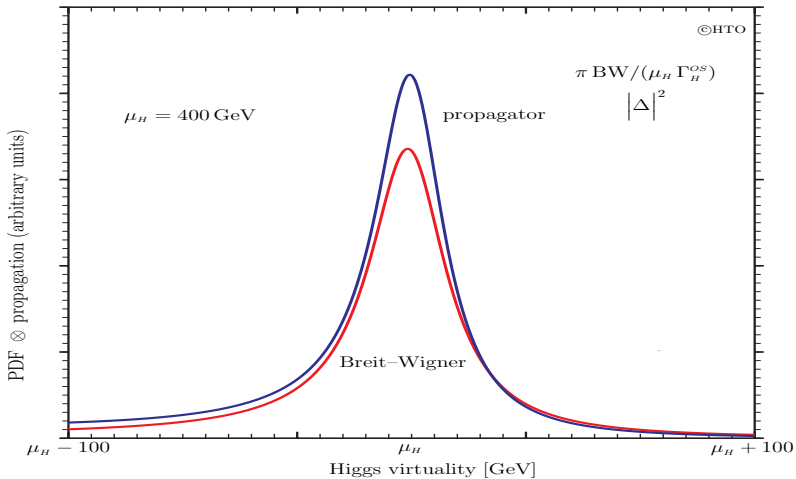


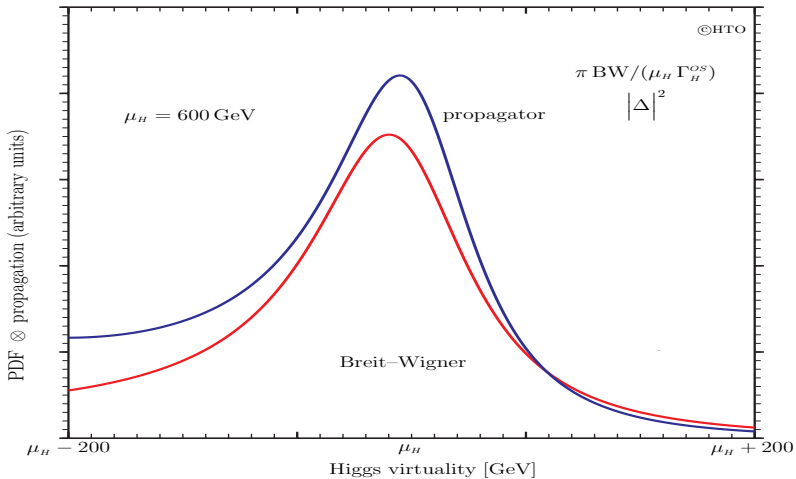
# Legenda

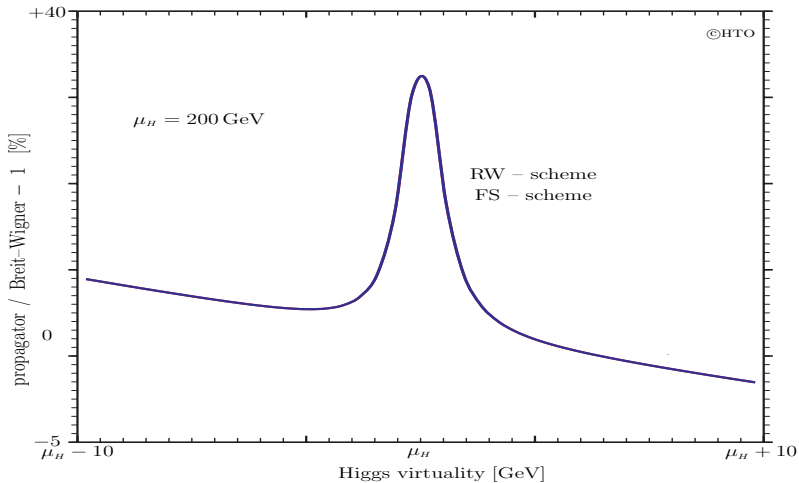
## Abb.

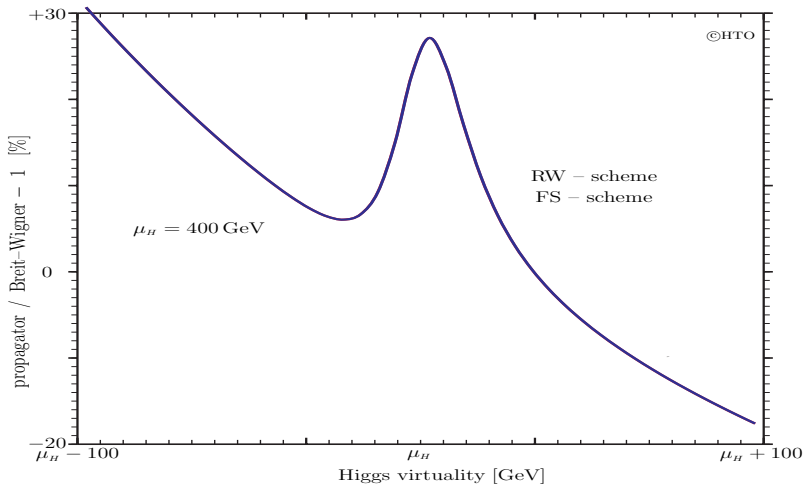
- FW** Breit–Wigner Fixed Width
- RW** Breit–Wigner Running Width
- OS** parameters in On-Shell scheme
- Bar** parameters in Bar-scheme
- FS** Ren (fact) scales fixed
- RS** Ren (fact) scales running (virtuality)

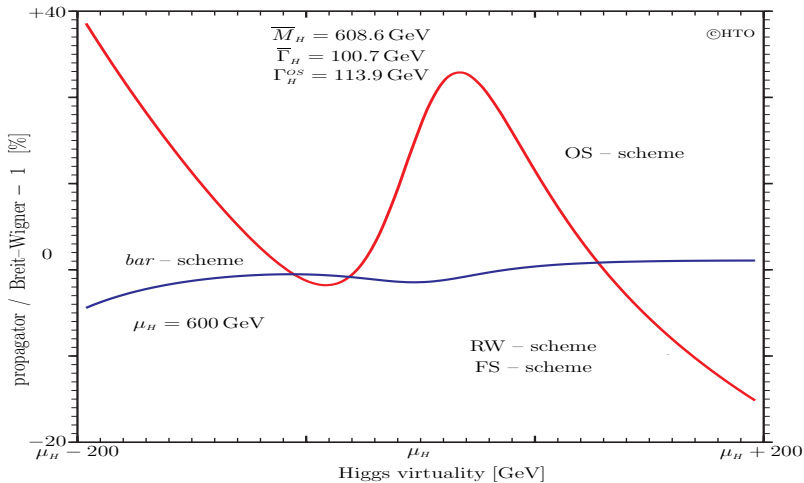












# The $\mu_R$ problem

## QED

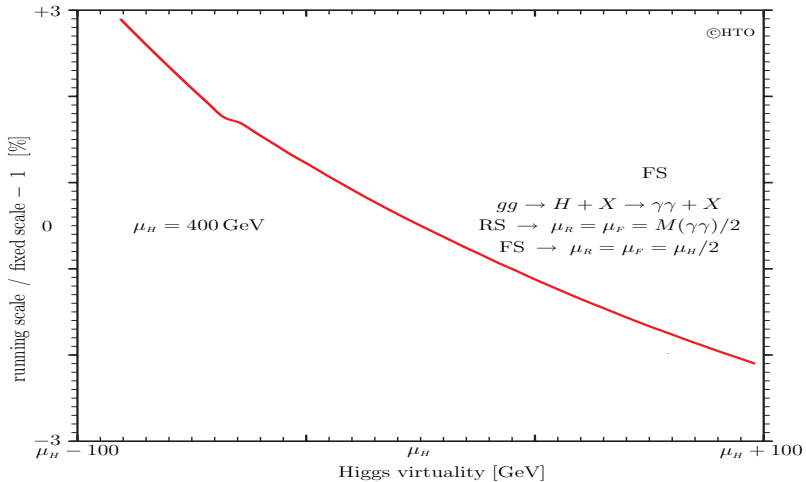
- Is there a  $\mu_R$  in QED? **Yes**
- Is it a problem? **No**,  $q^2 = 0$  is physical!

## EW

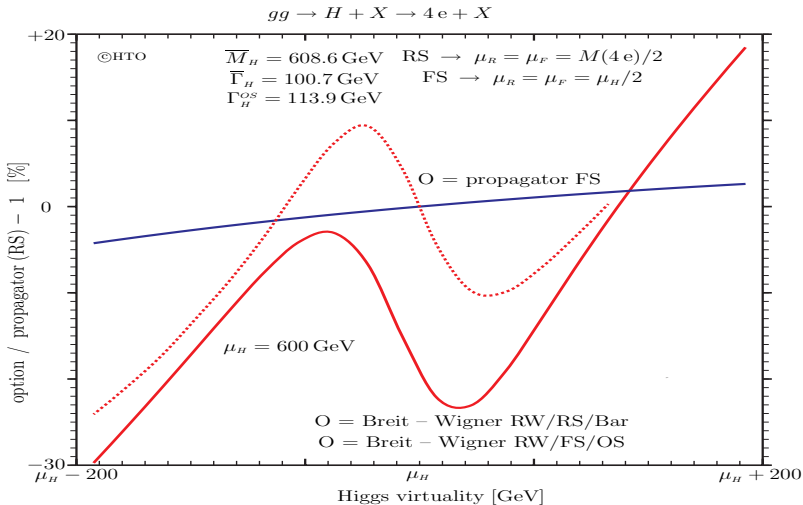
- Is there a  $\mu_R$  in EW? **Yes**
- Is it a problem? **No!**
- Are there large **logs**? **Yes**
- Use  $G_F$  - scheme and not  $\alpha(0)$ , i.e. **resum**

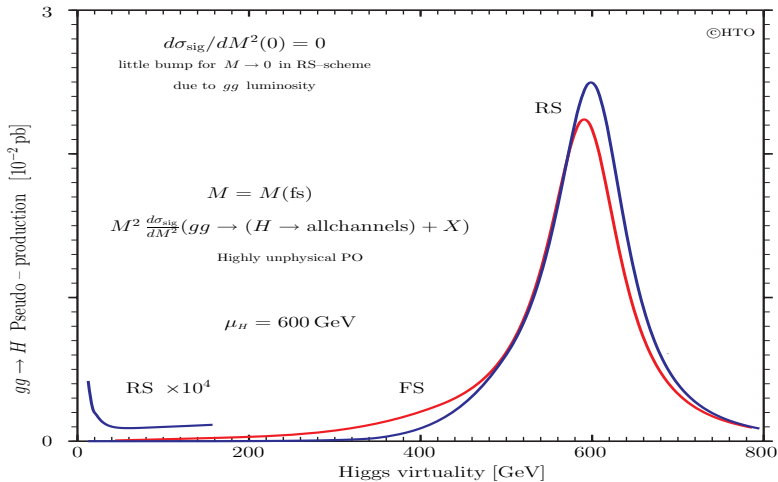
QCD one(multi)-scale? Once again, **resum** or, at least **minimize!**

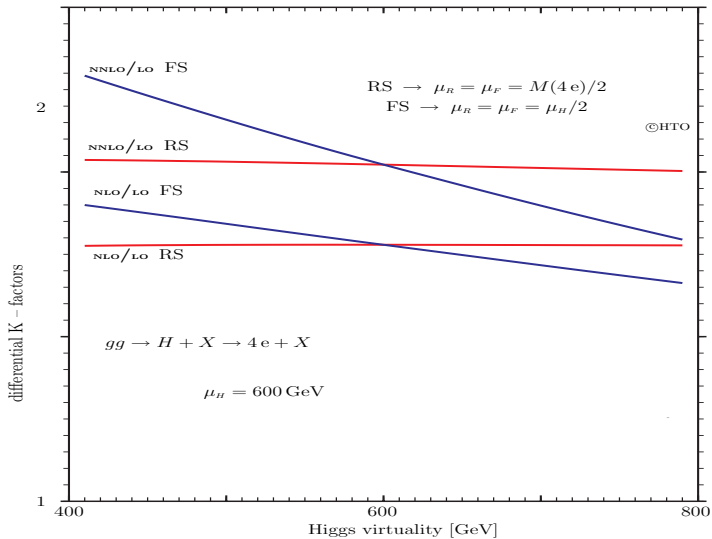


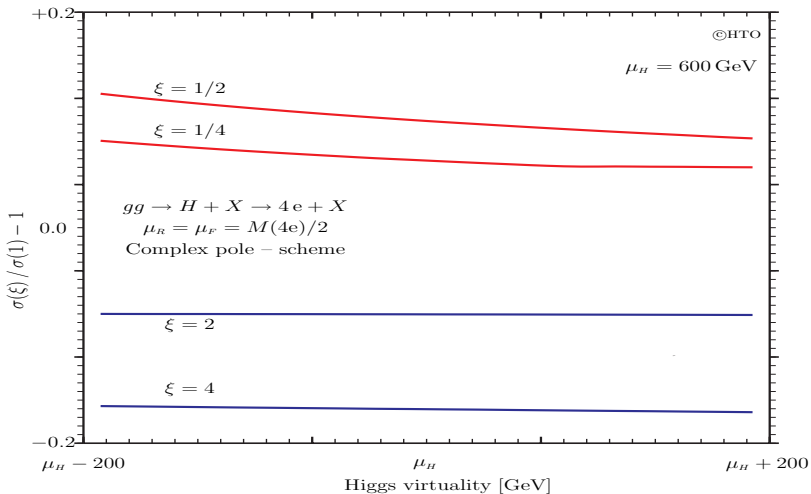


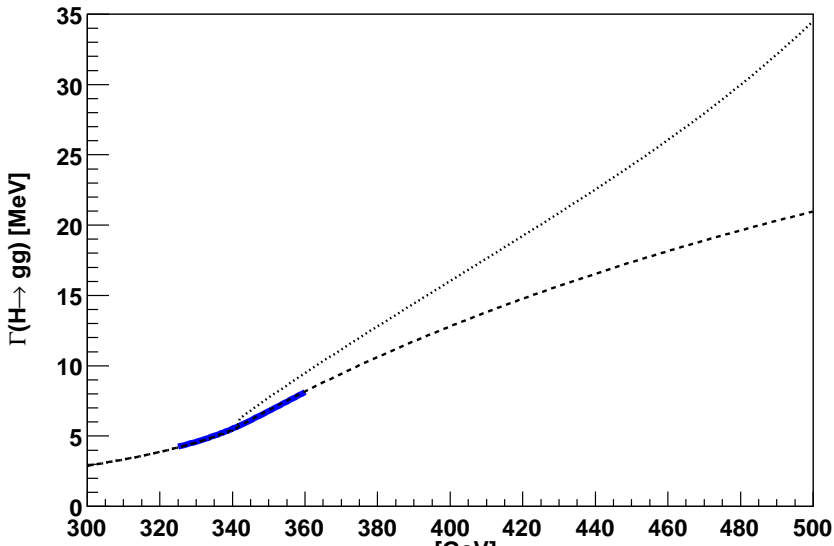












# PO rec.

## Temporary Entries

- Search for heavy Higgs: address it as *search* for heavy Higgs and  $J = 0, 1$  *heavy new resonances* decaying into  $VV \rightarrow 4f$ .
- Use definition of production  $\otimes$  decay (**at least**) with a momentum distributed according to a Breit–Wigner à la Pythia/POWHEG (now also in MC@NLO). Beware, BW parameters are *not* OS parameters (“Thy evil spirit, Brutus: I shall see thee at Philippi”, Shakespeare’s Julius Caesar).
- Assign a *conservative*  $\pm 20\%$  uncertainty for missing interference at high masses ( $\geq 600$  GeV).
- Use *running* QCD scales, taking into account the kinematics of final four fermions in  $gg \rightarrow H + X \rightarrow 4f + X$ .



# PO conclusions: before, after?

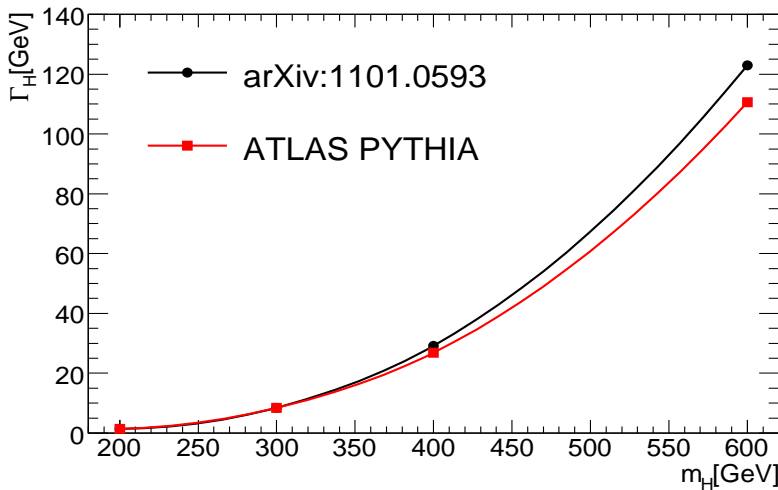


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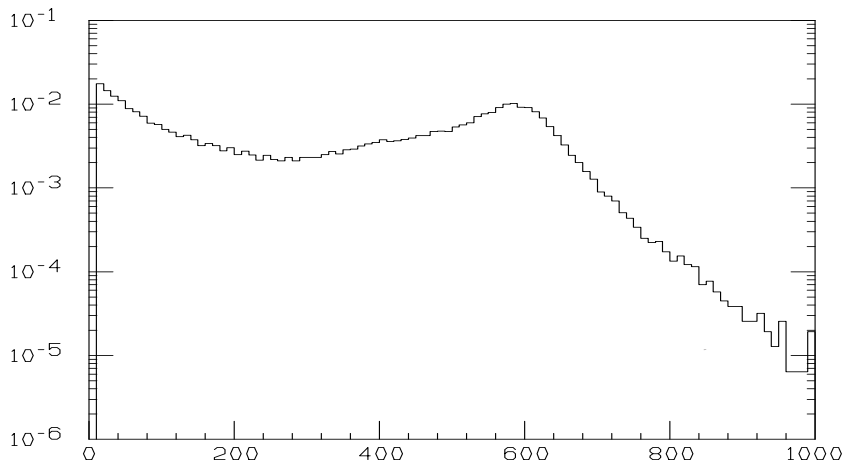


## Backup: courtesy R. Tanaka

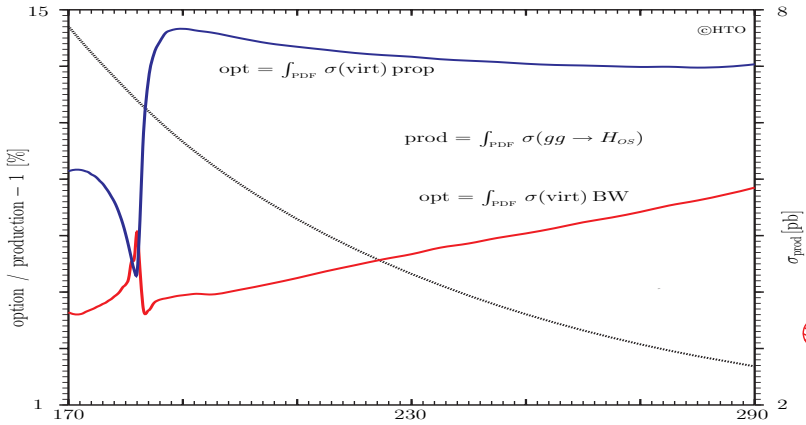




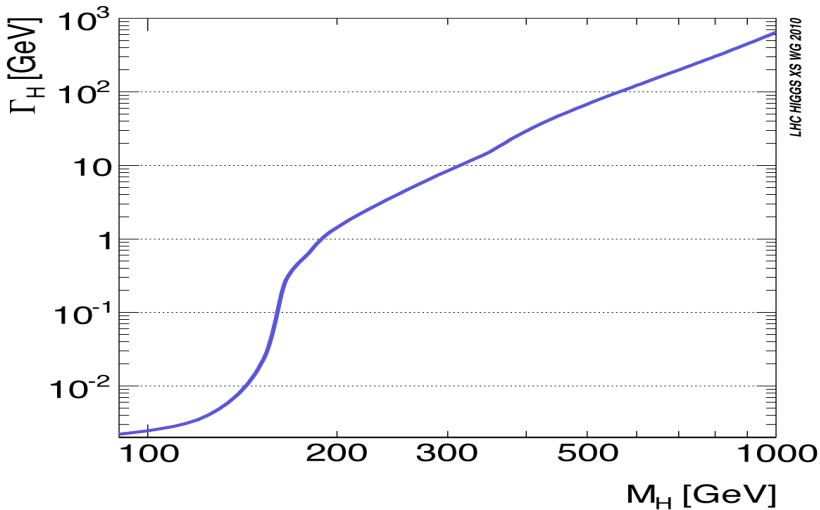
# Backup: courtesy S. Frixione



## Backup



## Backup



## Backup

