

Neutrino Anomalies

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Neutrino Unbound: <http://www.nu.to.infn.it>

EUROnu 2012

4th EUROnu Annual Meeting

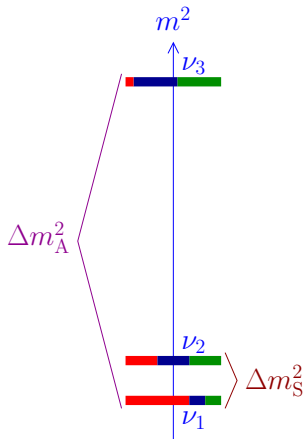
12-15 June 2012, Paris, France

Three-Neutrino Mixing Paradigm

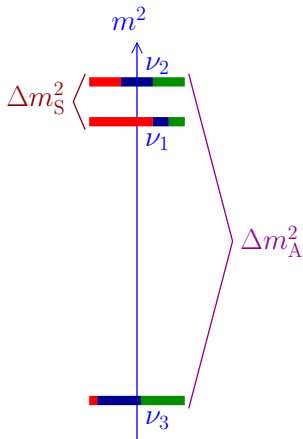
ν_e

ν_μ

ν_τ



Normal Spectrum



Inverted Spectrum

Standard Model

- ▶ Neutrinos are the only massless fermions
- ▶ Neutrinos are the only fermions with only left-handed component ν_L
- ▶ Neutrinos are the only neutral fermions

Extension of the SM: Massive Neutrinos

- ▶ Simplest extension: introduce right-handed component ν_R (singlet of $SU(2)_L \times U(1)_Y$)
- ▶ One generation: Dirac mass $m_D \overline{\nu_R} \nu_L$ + Majorana mass $m_M \overline{\nu_R^c} \nu_R$
 \implies 2 massive Majorana neutrinos
- ▶ Three left-handed fields + N_R right-handed fields:
 $\nu_{eL}, \nu_{\mu L}, \nu_{\tau L} + \nu_{1R}, \dots, \nu_{N_R R}$
 \implies 3 + N_R massive Majorana neutrinos

Sterile Neutrinos

- ▶ Light anti- ν_R are called sterile neutrinos

$$\nu_R^c \rightarrow \nu_{sL} \quad (\text{left-handed})$$

- ▶ Sterile means no standard model interactions
- ▶ Active neutrinos (ν_e, ν_μ, ν_τ) can oscillate into sterile neutrinos (ν_s)
- ▶ Observables:
 - ▶ Disappearance of active neutrinos (neutral current deficit)
 - ▶ Indirect evidence through combined fit of data (current indication)

- ▶ Short-baseline anomalies + 3ν -mixing:

$$\begin{array}{cccccc} \Delta m_{21}^2 & \ll & |\Delta m_{31}^2| & \ll & |\Delta m_{41}^2| & \leq \dots \\ \nu_1 & & \nu_2 & & \nu_3 & & \nu_4 & & \dots \\ \nu_e & & \nu_\mu & & \nu_\tau & & \nu_{s1} & & \dots \end{array}$$

Effective SBL Oscillation Probabilities in 3+1 Schemes

$$P_{\nu_\alpha \rightarrow \nu_\beta} = \sin^2 2\vartheta_{\alpha\beta} \sin^2 \left(\frac{\Delta m_{41}^2 L}{4E} \right) \quad \sin^2 2\vartheta_{\alpha\beta} = 4|U_{\alpha 4}|^2 |U_{\beta 4}|^2$$

No CP Violation!

$$P_{\nu_\alpha \rightarrow \nu_\alpha} = 1 - \sin^2 2\vartheta_{\alpha\alpha} \sin^2 \left(\frac{\Delta m_{41}^2 L}{4E} \right) \quad \sin^2 2\vartheta_{\alpha\alpha} = 4|U_{\alpha 4}|^2 (1 - |U_{\alpha 4}|^2)$$

Perturbation of 3 ν Mixing

$$|U_{e4}|^2 \ll 1, \quad |U_{\mu 4}|^2 \ll 1, \quad |U_{\tau 4}|^2 \ll 1, \quad |U_{s4}|^2 \simeq 1$$

$$U = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} & U_{\mu 4} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} & U_{\tau 4} \\ U_{s1} & U_{s2} & U_{s3} & U_{s4} \end{pmatrix}$$

↑
SBL

$$\sin^2 2\vartheta_{\alpha\alpha} \ll 1$$



$$|U_{\alpha 4}|^2 \simeq \frac{\sin^2 2\vartheta_{\alpha\alpha}}{4}$$

Effective SBL Oscillation Probabilities in 3+2 Schemes

$$\phi_{kj} = \Delta m_{kj}^2 L / 4E$$

$$\eta = \arg[U_{e4}^* U_{\mu 4} U_{e5} U_{\mu 5}^*]$$

$$P_{\nu_{\mu} \rightarrow \nu_e}^{(-) \quad (-)} = 4|U_{e4}|^2 |U_{\mu 4}|^2 \sin^2 \phi_{41} + 4|U_{e5}|^2 |U_{\mu 5}|^2 \sin^2 \phi_{51} \\ + 8|U_{\mu 4} U_{e4} U_{\mu 5} U_{e5}| \sin \phi_{41} \sin \phi_{51} \cos(\phi_{54} \overset{(+)}{-} \eta)$$

$$P_{\nu_{\alpha} \rightarrow \nu_{\alpha}}^{(-) \quad (-)} = 1 - 4(1 - |U_{\alpha 4}|^2 - |U_{\alpha 5}|^2)(|U_{\alpha 4}|^2 \sin^2 \phi_{41} + |U_{\alpha 5}|^2 \sin^2 \phi_{51}) \\ - 4|U_{\alpha 4}|^2 |U_{\alpha 5}|^2 \sin^2 \phi_{54}$$

- ▶ More parameters: 7 (vs 3 in 3+1)
- ▶ CP violation

[Sorel, Conrad, Shaevitz, PRD 70 (2004) 073004; Maltoni, Schwetz, PRD 76 (2007) 093005; Karagiorgi et al, PRD 80 (2009) 073001; Kopp, Maltoni, Schwetz, PRL 107 (2011) 091801; Giunti, Laveder, PRD 84 (2011) 073008; Donini et al, arXiv:1205.5230]

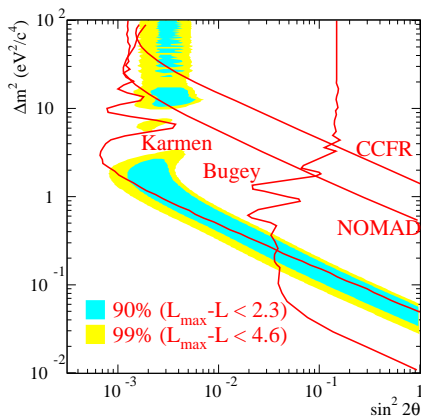
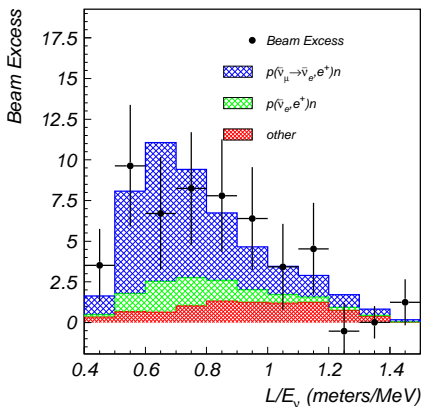
LSND

[LSND, PRL 75 (1995) 2650; PRC 54 (1996) 2685; PRL 77 (1996) 3082; PRD 64 (2001) 112007]

$$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$$

$$L \simeq 30 \text{ m}$$

$$20 \text{ MeV} \leq E \leq 200 \text{ MeV}$$



$$\Delta m_{\text{LSND}}^2 \gtrsim 0.2 \text{ eV}^2 \quad (\gg \Delta m_{\text{ATM}}^2 \gg \Delta m_{\text{SOL}}^2)$$

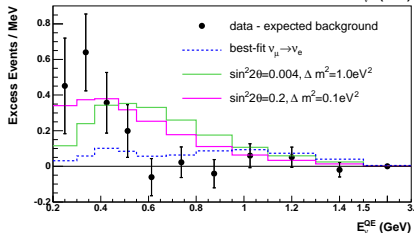
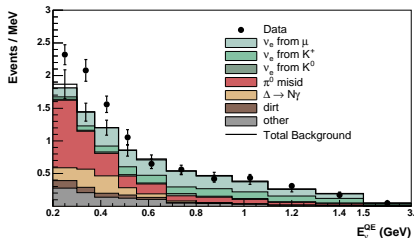
MiniBooNE Neutrinos

[PRL 98 (2007) 231801; PRL 102 (2009) 101802]

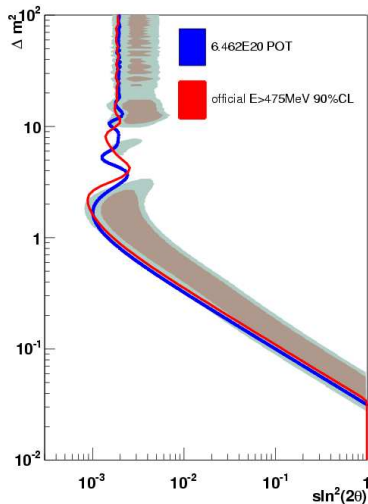
$$\nu_{\mu} \rightarrow \nu_e$$

$$L \simeq 541 \text{ m}$$

$$200 \text{ MeV} \leq E \lesssim 3 \text{ GeV}$$



[MiniBooNE, PRL 102 (2009) 101802]



[Djurcic, arXiv:0901.1648]

- ▶ no $\nu_{\mu} \rightarrow \nu_e$ signal corresponding to LSND $\bar{\nu}_{\mu} \rightarrow \bar{\nu}_e$ signal ($E > 475 \text{ MeV}$)
- ▶ low-energy anomaly

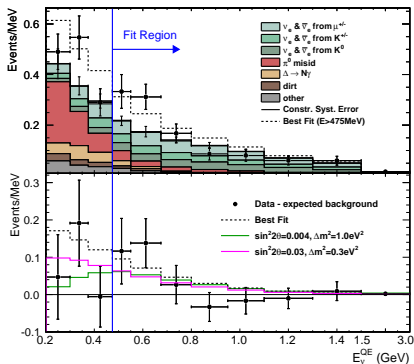
MiniBooNE Antineutrinos - 2009-2010

[PRL 103 (2009) 111801; PRL 105 (2010) 181801]

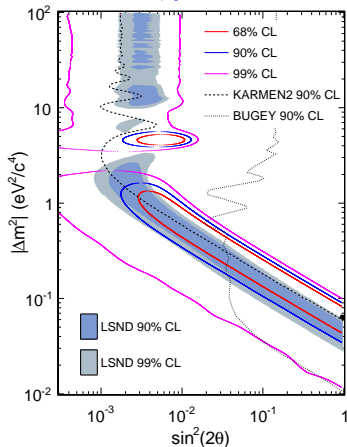
$$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$$

$$L \simeq 541 \text{ m}$$

$$200 \text{ MeV} \leq E \lesssim 3 \text{ GeV}$$



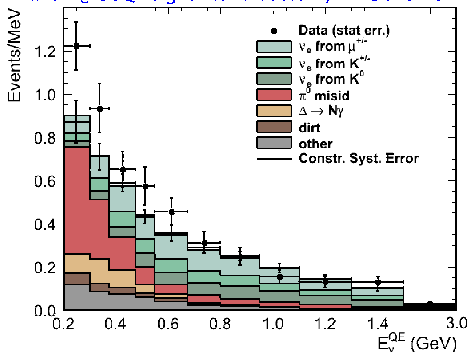
[MiniBooNE, PRL 105 (2010) 181801]



- ▶ 5.7e20 POT: agreement with LSND $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ signal ($E > 475 \text{ MeV}$)
- ▶ similar L/E but different L and $E \implies$ oscillations

MiniBooNE $\bar{\nu}$ - Neutrino 2012 - 6 June

anti- ν_e CCQE signal candidates w/ 11.3e20 POT



Higher stat anti-neutrino data is now much more consistent with what was observed in the data taken with a neutrino beam

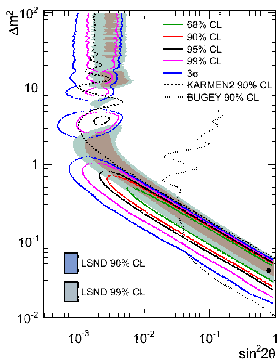
* Systematic error after all other data constraints applied, e.g. ν_μ CCQE, NC π^0 , dirt events, SciBooNE K^+

		1st half			2nd half	
	data	mc	excess	data	mc	excess
200-475	119	100.5±14.3	18.5 (1.3s)	138	100.0±14.1	38 (2.7s)
475-1250	120	99.1±14.0	20.9 (1.5s)	101	103.1±14.4	-2.2 (-0.2s)

agreement with LSND signal is sadly vanishing

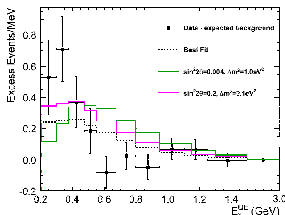
MiniBooNE ν and $\bar{\nu}$ - Neutrino 2012 - 6 June

Simultaneous 3+1 fit to ν and anti- ν data

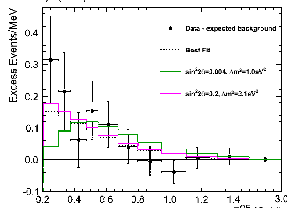


- WS accounted for properly
- Construction of correlated systematic error matrix (Z. Pavlovic)
- $E > 200$ MeV BF preferred at 3.6σ over null

Total Excess: $240.3 \pm 34.5 \pm 52.6$



* Simultaneous fit ($E > 200$ MeV) with fully-correlated systematic to entire MB neutrino and anti-neutrino data

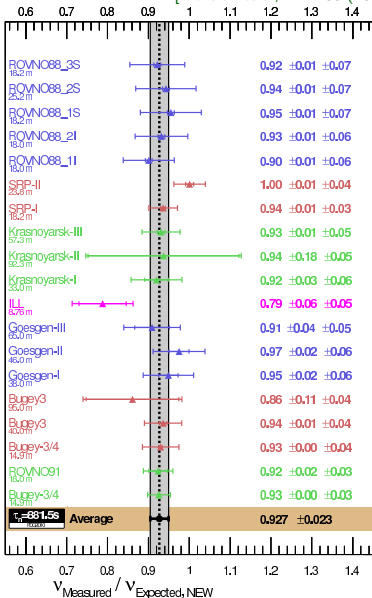


combined	$E > 200$ MeV	$E > 475$ MeV
$\chi^2(\text{null})$	42.53	12.87
Prob(null)	0.1%	35.8%
$\chi^2(\text{bf})$	24.72	10.67
Prob(bf)	6.7%	35.8%

fit of low-energy excesses is excluded by reactor bound

Reactor Electron Antineutrino Anomaly

[Mention et al, PRD 83 (2011) 073006; update in White Paper, arXiv:1204.5379]



new reactor $\bar{\nu}_e$ fluxes

[Mueller et al, PRC 83 (2011) 054615]

[Huber, PRC 84 (2011) 024617]

Detection: $\sigma(\bar{\nu}_e + p \rightarrow n + e^+) \propto \tau_n^{-1}$

PDG neutron lifetime τ_n

1995 887.0 ± 2.0 sec

1998 886.7 ± 1.9 sec

2002 885.7 ± 0.8 sec

2011 881.5 ± 1.5 sec

change of predicted event rates

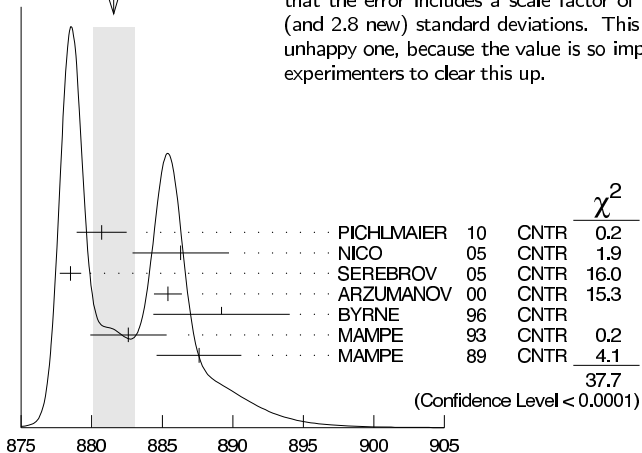
^{235}U	^{238}U	^{239}Pu	^{241}Pu
+3.7%	+9.8%	+4.2%	+4.7%

Neutron Lifetime Problem

WEIGHTED AVERAGE
 881.5 ± 1.5 (Error scaled by 2.7)

At this point, we can think of nothing better to do than to average the seven best but discordant measurements, getting 881.5 ± 1.5 s. Note that the error includes a scale factor of 2.7. This is a jump of 4.2 old (and 2.8 new) standard deviations. This state of affairs is a particularly unhappy one, because the value is so important. We again call upon the experimenters to clear this up.

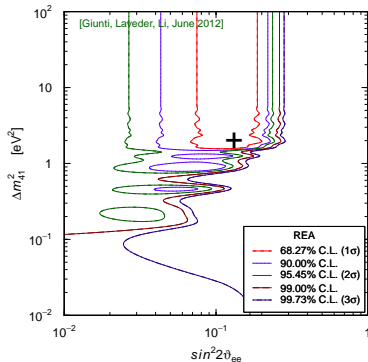
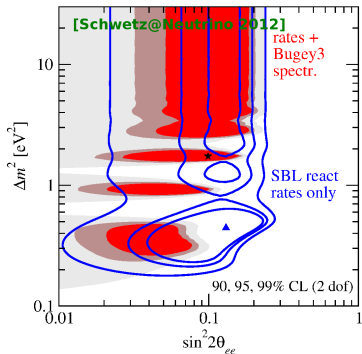
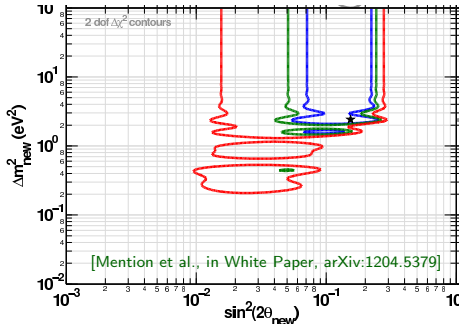
[PDG 2011, <http://pdg.lbl.gov>]



Reactor $\bar{\nu}_e$ Disappearance

$$P_{\nu_e \rightarrow \nu_e} = 1 - \sin^2 2\vartheta_{ee} \sin^2 \left(\frac{\Delta m_{41}^2 L}{4E} \right)$$

$$\sin^2 2\vartheta_{ee} = 4|U_{e4}|^2 (1 - |U_{e4}|^2)$$



Gallium Anomaly

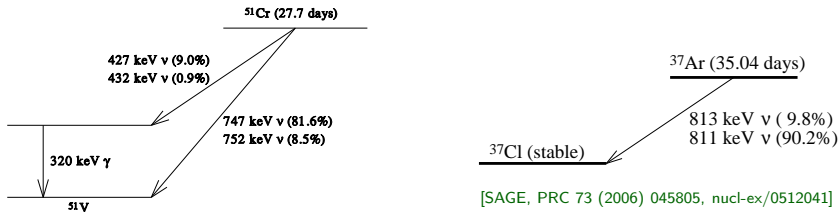
Gallium Radioactive Source Experiments

Tests of the solar neutrino detectors **GALLEX** (Cr1, Cr2) and **SAGE** (Cr, Ar)

Detection Process: $\nu_e + {}^{71}\text{Ga} \rightarrow {}^{71}\text{Ge} + e^-$

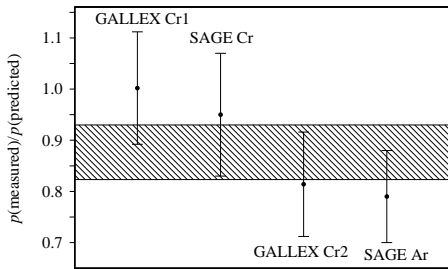
ν_e Sources: $e^- + {}^{51}\text{Cr} \rightarrow {}^{51}\text{V} + \nu_e$ $e^- + {}^{37}\text{Ar} \rightarrow {}^{37}\text{Cl} + \nu_e$

	${}^{51}\text{Cr}$				${}^{37}\text{Ar}$	
E [keV]	747	752	427	432	811	813
B.R.	0.8163	0.0849	0.0895	0.0093	0.902	0.098



[SAGE, PRC 73 (2006) 045805, nucl-ex/0512041]

[SAGE, PRC 59 (1999) 2246, hep-ph/9803418]



$$\langle L \rangle_{\text{GALLEX}} = 1.9 \text{ m}$$

$$\langle L \rangle_{\text{SAGE}} = 0.6 \text{ m}$$

[SAGE, PRC 73 (2006) 045805, nucl-ex/0512041]

$$R_B^{\text{Gallex-Cr1}} = 0.953 \pm 0.11$$

$$R_B^{\text{Gallex-Cr2}} = 0.812^{+0.10}_{-0.11}$$

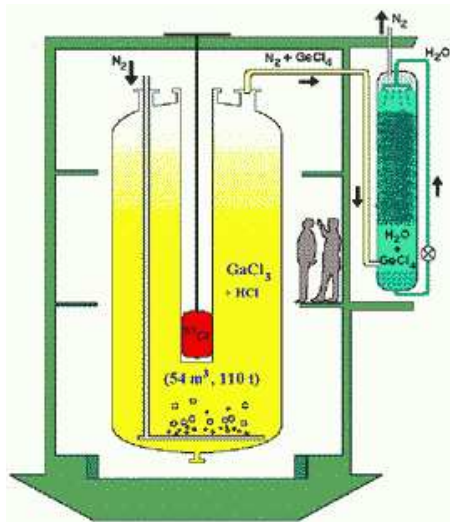
$$R_B^{\text{SAGE-Cr}} = 0.95 \pm 0.12$$

$$R_B^{\text{SAGE-Ar}} = 0.791^{+0.084}_{-0.078}$$

$$R_B^{\text{Ga}} = 0.86 \pm 0.05$$

Bahcall cross section without
uncertainty

[Bahcall, PRC 56 (1997) 3391, hep-ph/9710491]

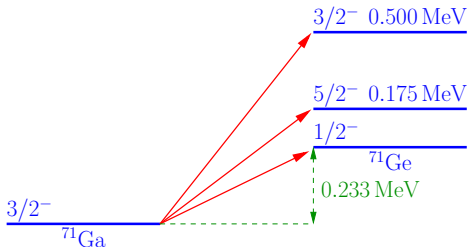


[GALLEX]

- ▶ Deficit could be due to overestimate of

$$\sigma(\nu_e + {}^{71}\text{Ga} \rightarrow {}^{71}\text{Ge} + e^-)$$

- ▶ Calculation: Bahcall, PRC 56 (1997) 3391



- ▶ $\sigma_{\text{G.S.}}$ related to measured $\sigma(e^- + {}^{71}\text{Ge} \rightarrow {}^{71}\text{Ga} + \nu_e)$:

$$\sigma_{\text{G.S.}}({}^{51}\text{Cr}) = 55.3 \times 10^{-46} \text{ cm}^2 (1 \pm 0.004)_{3\sigma}$$

- ▶ $\sigma({}^{51}\text{Cr}) = \sigma_{\text{G.S.}}({}^{51}\text{Cr}) \left(1 + 0.669 \frac{\text{BGT}_{175}}{\text{BGT}_{\text{G.S.}}} + 0.220 \frac{\text{BGT}_{500}}{\text{BGT}_{\text{G.S.}}} \right)$

- ▶ Contribution of Excited States only 5%!

		$\frac{\text{BGT}_{175}}{\text{BGT}_{\text{G.S.}}}$	$\frac{\text{BGT}_{500}}{\text{BGT}_{\text{G.S.}}}$
Krofcheck et al. PRL 55 (1985) 1051	${}^{71}\text{Ga}(p, n){}^{71}\text{Ge}$	< 0.056	0.13 ± 0.02
Haxton PLB 431 (1998) 110	Shell Model	0.19 ± 0.18	
Frekers et al. PLB 706 (2011) 134	${}^{71}\text{Ga}({}^3\text{He}, {}^3\text{H}){}^{71}\text{Ge}$	0.039 ± 0.030	0.202 ± 0.016

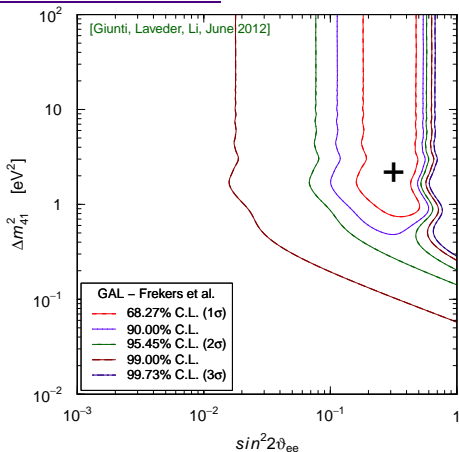
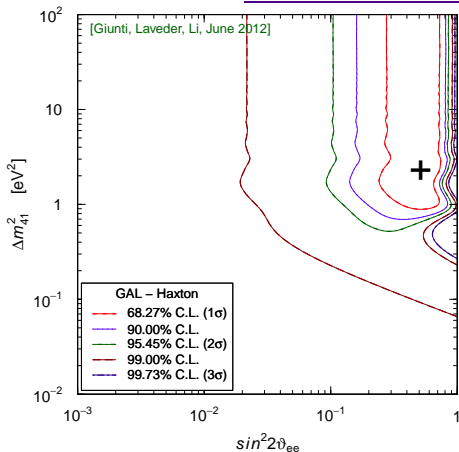
► Haxton:

[Haxton, PLB 431 (1998) 110]

“a sophisticated shell model calculation is performed ... for the transition to the first excited state in ${}^{71}\text{Ge}$. The calculation predicts **destructive interference** between the (p, n) spin and spin-tensor matrix elements”

- 2.7σ discrepancy of $\text{BGT}_{500}/\text{BGT}_{\text{G.S.}}$ measurements
- Anyhow, new ${}^{71}\text{Ga}({}^3\text{He}, {}^3\text{H}){}^{71}\text{Ge}$ data **support** Gallium Anomaly

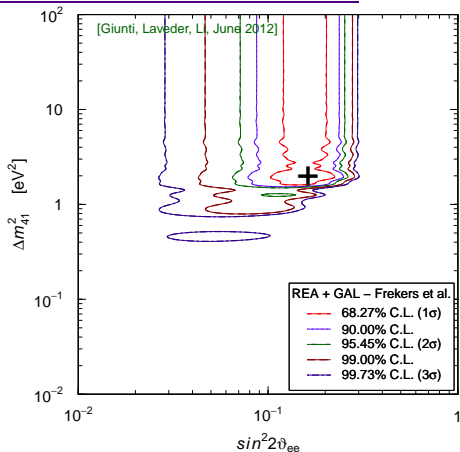
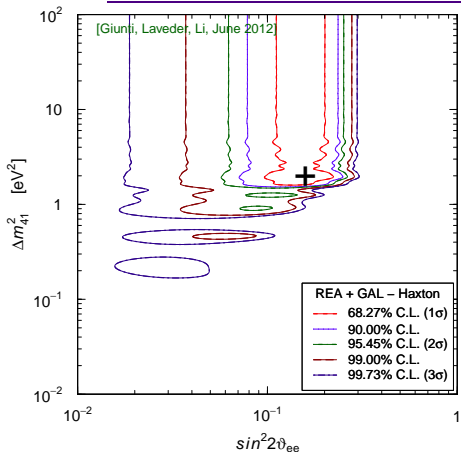
Gallium ν_e Disappearance



No Osc.	χ_{\min}^2	14.9
	NDF	4
	GoF	0.5 %
3+1	χ_{\min}^2	4.7
	NDF	2
	GoF	9.5 %
	Δm_{41}^2 [eV ²]	2.24
	$\sin^2 2\vartheta_{ee}$	0.51

No Osc.	χ_{\min}^2	18.2
	NDF	4
	GoF	0.1 %
3+1	χ_{\min}^2	7.9
	NDF	2
	GoF	1.9 %
	Δm_{41}^2 [eV ²]	2.14
	$\sin^2 2\vartheta_{ee}$	0.32

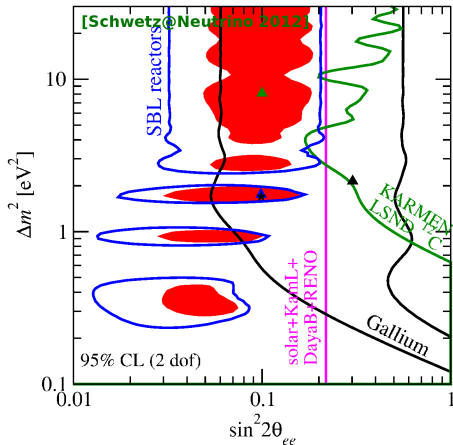
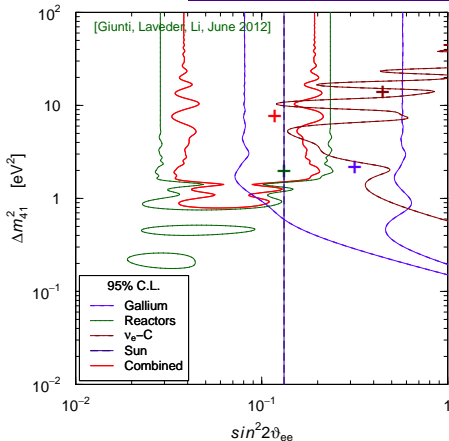
Reactor $\bar{\nu}_e$ and Gallium ν_e Disappearance



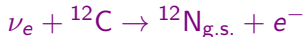
No Osc.	χ^2_{\min}	45.6
	NDF	42
	GoF	32.3 %
3+1	χ^2_{\min}	30.8
	NDF	40
	GoF	85 %
	Δm^2_{41} [eV ²]	1.95
	$\sin^2 2\theta_{ee}$	0.16

No Osc.	χ^2_{\min}	48.9
	NDF	42
	GoF	21.5 %
3+1	χ^2_{\min}	32.2
	NDF	40
	GoF	80 %
	Δm^2_{41} [eV ²]	1.95
	$\sin^2 2\theta_{ee}$	0.16

Global ν_e and $\bar{\nu}_e$ Disappearance



KARMEN + LSND



[Conrad, Shaevitz, PRD 85 (2012) 013017]

[Giunti, Laveder, PLB 706 (2011) 200]

SUN&KamLAND + ϑ_{13}

[Giunti, Li, PRD 80 (2009) 113007]

[Palazzo, PRD 83 (2011) 113013]

[Palazzo, PRD 85 (2012) 077301]

SUN&KamLAND + ϑ_{13} bound on $|U_{e4}|^2$

[Giunti, Li, PRD 80 (2009) 113007; Palazzo, PRD 83 (2011) 113013, PRD 85 (2012) 077301]

3+1 with simplifying assumptions: $U_{\mu 4} = U_{\tau 4} = 0$, no CP violation

$$U_{e1} = c_{12}c_{13}c_{14} \quad U_{e2} = s_{12}c_{13}c_{14} \quad U_{e3} = s_{13}c_{14} \quad U_{e4} = s_{14}$$

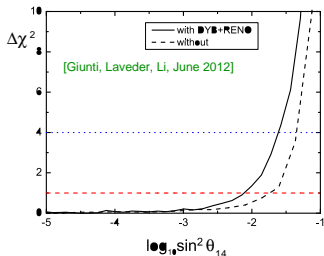
$$U_{s1} = -c_{12}c_{13}s_{14} \quad U_{s2} = -s_{12}c_{13}s_{14} \quad U_{s3} = -s_{13}s_{14} \quad U_{s4} = c_{14}$$

$$P_{\nu_e \rightarrow \nu_e} = c_{13}^4 c_{14}^4 P_{\nu_e \rightarrow \nu_e}^{2\nu} + s_{13}^4 c_{14}^4 + s_{14}^4$$

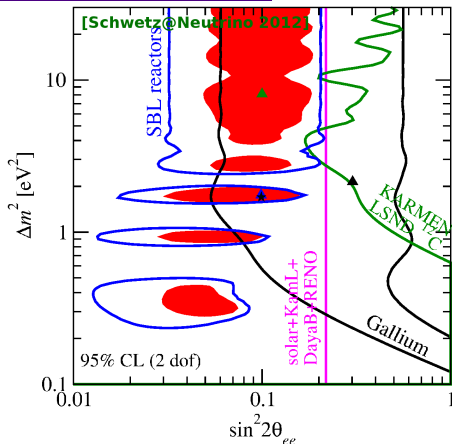
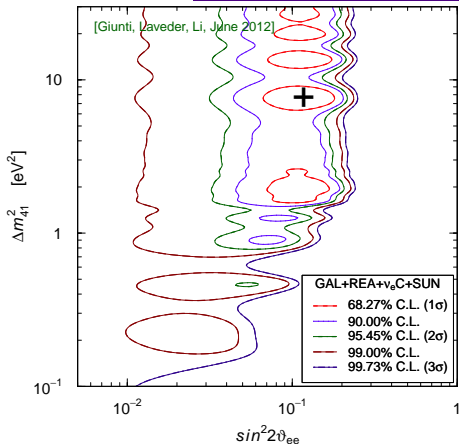
$$P_{\nu_e \rightarrow \nu_s} = c_{14}^2 s_{14}^2 (c_{13}^4 P_{\nu_e \rightarrow \nu_s}^{2\nu} + s_{13}^4 + 1)$$

$$V = c_{13}^2 c_{14}^2 V_{CC} - c_{13}^2 s_{14}^2 V_{NC} = (|U_{e1}|^2 + |U_{e2}|^2) V_{CC} - (|U_{s1}|^2 + |U_{s2}|^2) V_{NC}$$

Fit with $U_{\mu 4}$ and $U_{\tau 4}$ free:



Global ν_e and $\bar{\nu}_e$ Disappearance

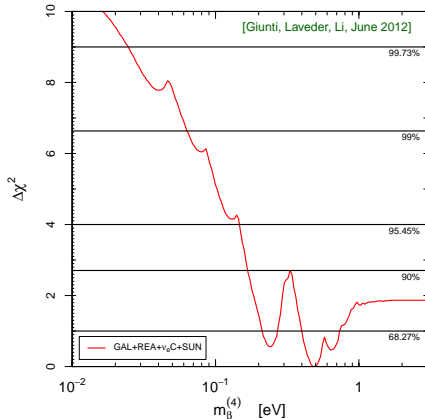


No Osc.	χ_{\min}^2	57.1
	NDF	53
	GoF	32.6 %
3+1	χ_{\min}^2	46.0
	NDF	51
	GoF	67 %
	Δm_{41}^2 [eV ²]	7.59
	$\sin^2 2\theta_{ee}$	0.12

No Osc.	χ_{\min}^2	318.4
	NDF	331
	GoF	68%
3+1	χ_{\min}^2	306.0
	NDF	329
	GoF	80%
	Δm_{41}^2 [eV ²]	1.71
	$\sin^2 2\theta_{ee}$	0.099

Testable Implications

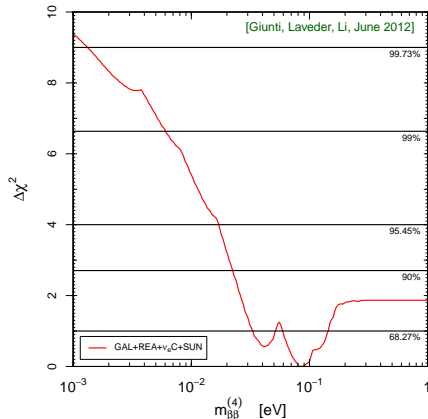
β Decay



$$m_\beta = \sqrt{\sum_k |U_{ek}|^2 m_k^2}$$

$$m_\beta^{(4)} = |U_{e4}| \sqrt{\Delta m_{41}^2}$$

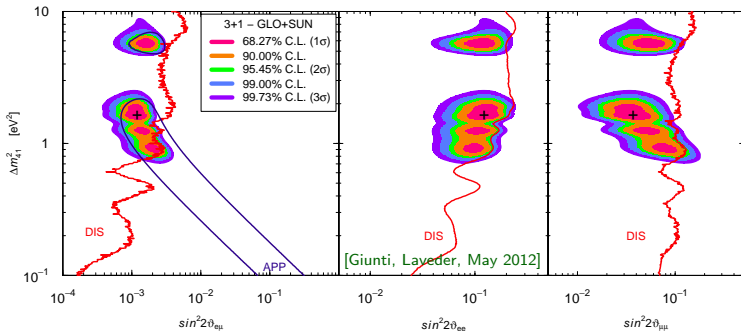
$(\beta\beta)_{0\nu}$ Decay



$$m_{\beta\beta} = \left| \sum_k U_{ek}^2 m_k \right|$$

$$m_{\beta\beta}^{(4)} = |U_{e4}|^2 \sqrt{\Delta m_{41}^2}$$

Global 3+1 Fit



- ▶ MiniBooNE 2011 data ($E > 475$ MeV)
- ▶ More time is needed to fit MiniBooNE 2012 data

Conclusions

- ▶ Short-Baseline $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$:
 - ▶ MiniBooNE 2011 antineutrino data were more similar to neutrino data than those of 2010 (LSND signal diminished and low-energy anomaly appeared)
 - ▶ MiniBooNE 2012 antineutrino data are even more similar to neutrino data
 - ▶ Probably there is no CP violation \implies no need of 3+2
 - ▶ The decrease of MiniBooNE-LSND agreement is discouraging
 - ▶ Better experiments are needed to clarify situation
- ▶ Short-Baseline ν_e and $\bar{\nu}_e$ Disappearance:
 - ▶ Reactor $\bar{\nu}_e$ anomaly is alive and exciting
 - ▶ Gallium ν_e anomaly has been strengthened by new cross-section measurements
 - ▶ Many promising projects to test short-baseline ν_e and $\bar{\nu}_e$ disappearance in a few years with reactors and radioactive sources
 - ▶ Independent tests through effect of m_4 in β -decay and $(\beta\beta)_{0\nu}$ -decay