

# Phenomenology of Light Sterile Neutrinos

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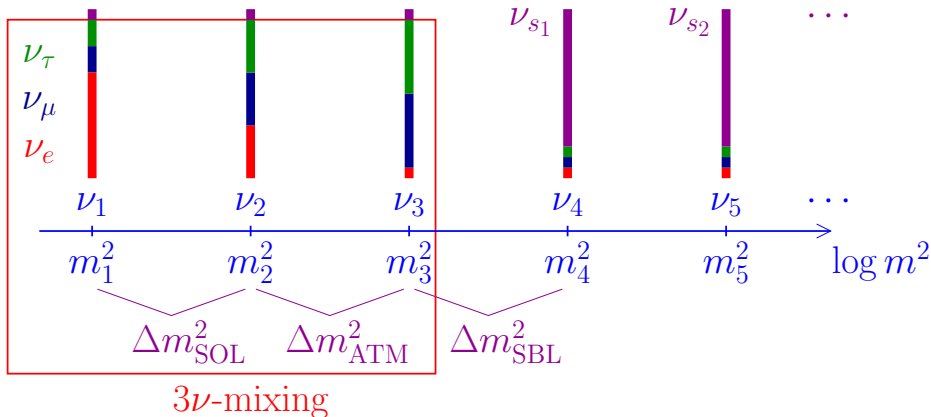
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Neutrino Unbound: <http://www.nu.to.infn.it>

NPB 2012, International Symposium on Neutrino Physics and Beyond

23-26 September 2012, Shenzhen, China

# Beyond Three-Neutrino Mixing



# Sterile Neutrinos from Physics Beyond the SM

- ▶ Neutrinos are special in the Standard Model: the only **neutral fermions**
- ▶ In extensions of SM neutrinos can mix with non-SM fermions

▶ SM:  $L_L = \begin{pmatrix} \nu_L \\ \ell_L \end{pmatrix} \quad \tilde{\Phi} = i\sigma_2 \Phi^* = \begin{pmatrix} \phi^0 \\ \phi^- \end{pmatrix} \xrightarrow[\text{Breaking}]{\text{Symmetry}} \begin{pmatrix} v/\sqrt{2} \\ 0 \end{pmatrix}$

- ▶ SM singlet  $\overline{L}_L \tilde{\Phi}$  can couple to new singlet chiral fermion field  $f_R$  related to physics beyond the SM
- ▶ Known examples: light  $\nu_R$  from see-saw, SUSY ( $\nu_R$ , axino, ...), extra dimensions (Kaluza-Klein modes), mirror world, ...
- ▶ **Dirac mass term**  $\sim \overline{L}_L \tilde{\Phi} f_R$  + **Majorana mass term**  $\sim \overline{f_R^c} f_R$
- ▶  $f_R$  is often called **Right-Handed Neutrino**:  $f_R \rightarrow \nu_R$

# Sterile Neutrinos

- ▶ Light anti- $\nu_R$  are called **sterile neutrinos**

$$\nu_R^c \rightarrow \nu_{sL} \quad (\text{left-handed})$$

- ▶ Sterile means **no standard model interactions**
- ▶ Active neutrinos ( $\nu_e, \nu_\mu, \nu_\tau$ ) can oscillate into sterile neutrinos ( $\nu_s$ )
- ▶ Observables:
  - ▶ **Disappearance** of active neutrinos (**neutral current deficit**)
  - ▶ Indirect evidence through **combined fit of data** (**current indication**)
- ▶ Short-baseline anomalies +  $3\nu$ -mixing:

$$\begin{array}{ccccc} \Delta m_{21}^2 & \ll & |\Delta m_{31}^2| & \ll & |\Delta m_{41}^2| \leq \dots \\ \nu_1 & & \nu_2 & & \nu_3 & & \nu_4 & & \dots \\ \nu_e & & \nu_\mu & & \nu_\tau & & \nu_{s1} & & \dots \end{array}$$

- ▶ In this talk I consider sterile neutrinos with mass scale  $\sim 1$  eV in light of short-baseline LSND, MiniBooNE, Reactor Anomaly, Gallium Anomaly.
  - ▶ Other possibilities (not incompatible):
    - ▶ Very light sterile neutrinos with mass scale  $\ll 1$  eV: important for solar neutrino phenomenology
      - [Das, Pulido, Picariello, PRD 79 (2009) 073010]
      - [de Holanda, Smirnov, PRD 83 (2011) 113011]
    - ▶ Heavy sterile neutrinos with mass scale  $\gg 1$  eV: could be Warm Dark Matter
      - [Kusenko, Phys. Rept. 481 (2009) 1]
- [Boyarsky, Ruchayskiy, Shaposhnikov, Ann. Rev. Nucl. Part. Sci. 59 (2009) 191]

## Effective SBL Oscillation Probabilities in 3+1 Schemes

$$P_{\nu_\alpha \rightarrow \nu_\beta} = \sin^2 2\vartheta_{\alpha\beta} \sin^2 \left( \frac{\Delta m_{41}^2 L}{4E} \right) \quad \sin^2 2\vartheta_{\alpha\beta} = 4|U_{\alpha 4}|^2 |U_{\beta 4}|^2$$

No CP Violation!

$$P_{\nu_\alpha \rightarrow \nu_\alpha} = 1 - \sin^2 2\vartheta_{\alpha\alpha} \sin^2 \left( \frac{\Delta m_{41}^2 L}{4E} \right) \quad \sin^2 2\vartheta_{\alpha\alpha} = 4|U_{\alpha 4}|^2 (1 - |U_{\alpha 4}|^2)$$

Perturbation of 3 $\nu$  Mixing

$$|U_{e4}|^2 \ll 1, \quad |U_{\mu 4}|^2 \ll 1, \quad |U_{\tau 4}|^2 \ll 1, \quad |U_{s4}|^2 \simeq 1$$

$$U = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} & U_{\mu 4} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} & U_{\tau 4} \\ U_{s1} & U_{s2} & U_{s3} & U_{s4} \end{pmatrix}$$

↑  
SBL

$$\sin^2 2\vartheta_{\alpha\alpha} \ll 1$$



$$|U_{\alpha 4}|^2 \simeq \frac{\sin^2 2\vartheta_{\alpha\alpha}}{4}$$

# Effective SBL Oscillation Probabilities in 3+2 Schemes

$$\phi_{kj} = \Delta m_{kj}^2 L / 4E$$

$$\eta = \arg[U_{e4}^* U_{\mu 4} U_{e5} U_{\mu 5}^*]$$

$$P_{\nu_{\mu} \rightarrow \nu_e}^{(-) \quad (-)} = 4|U_{e4}|^2 |U_{\mu 4}|^2 \sin^2 \phi_{41} + 4|U_{e5}|^2 |U_{\mu 5}|^2 \sin^2 \phi_{51} \\ + 8|U_{\mu 4} U_{e4} U_{\mu 5} U_{e5}| \sin \phi_{41} \sin \phi_{51} \cos(\phi_{54}^{(+)} - \eta)$$

$$P_{\nu_{\alpha} \rightarrow \nu_{\alpha}}^{(-) \quad (-)} = 1 - 4(1 - |U_{\alpha 4}|^2 - |U_{\alpha 5}|^2)(|U_{\alpha 4}|^2 \sin^2 \phi_{41} + |U_{\alpha 5}|^2 \sin^2 \phi_{51}) \\ - 4|U_{\alpha 4}|^2 |U_{\alpha 5}|^2 \sin^2 \phi_{54}$$

[Sorel, Conrad, Shaevitz, PRD 70 (2004) 073004; Maltoni, Schwetz, PRD 76 (2007) 093005; Karagiorgi et al, PRD 80 (2009) 073001; Kopp, Maltoni, Schwetz, PRL 107 (2011) 091801; Giunti, Laveder, PRD 84 (2011) 073008; Donini et al, arXiv:1205.5230; Conrad, Ignarra, Karagiorgi, Shaevitz, Spitz, arXiv:1207.4765]

- ▶ More parameters: 7 (vs 3 in 3+1)
- ▶ CP violation
- ▶ Why not 3+3?

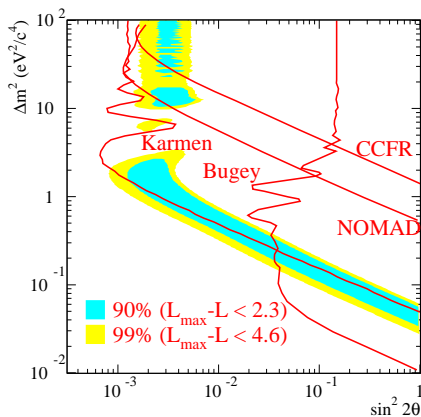
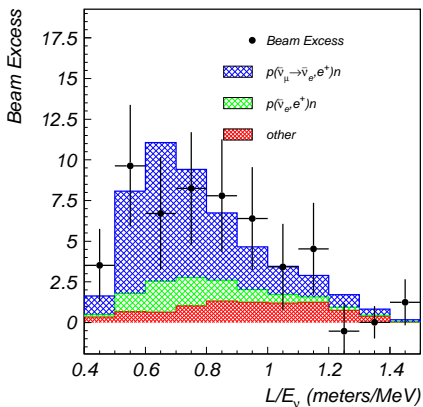
# LSND

[PRL 75 (1995) 2650; PRC 54 (1996) 2685; PRL 77 (1996) 3082; PRD 64 (2001) 112007]

$$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$$

$$L \simeq 30 \text{ m}$$

$$20 \text{ MeV} \leq E \leq 200 \text{ MeV}$$



3.8 $\sigma$  excess

$$\Delta m_{\text{LSND}}^2 \gtrsim 0.2 \text{ eV}^2 \quad (\gg \Delta m_A^2 \gg \Delta m_S^2)$$



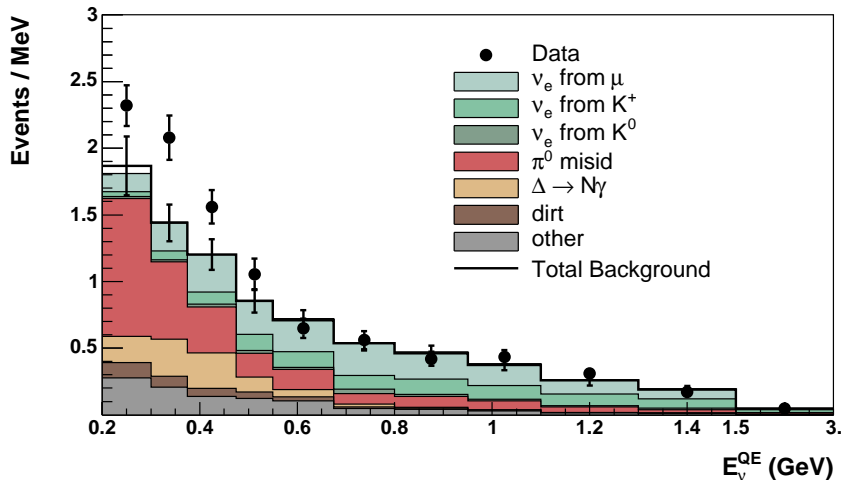
# MiniBooNE Neutrinos

[PRL 98 (2007) 231801; PRL 102 (2009) 101802]

$\nu_\mu \rightarrow \nu_e$

$L \simeq 541$  m

$200 \text{ MeV} \leq E \lesssim 3 \text{ GeV}$



- ▶ no  $\nu_\mu \rightarrow \nu_e$  signal corresponding to LSND  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  signal ( $E > 475$  MeV)
- ▶ low-energy anomaly

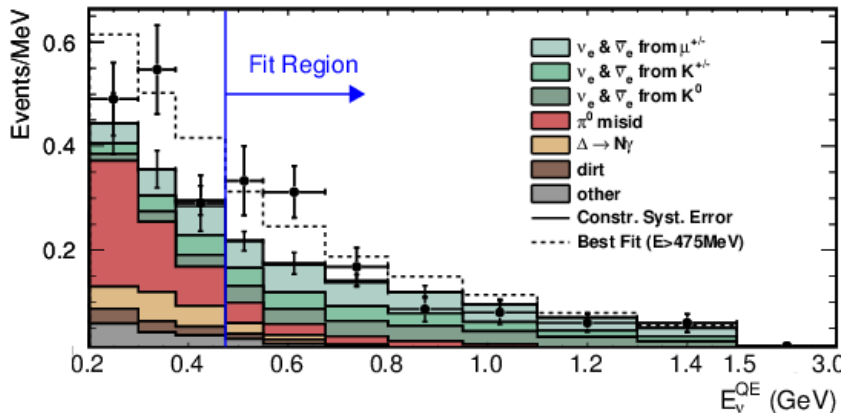
# MiniBooNE Antineutrinos - 2009-2010

[PRL 103 (2009) 111801; PRL 105 (2010) 181801]

$$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$$

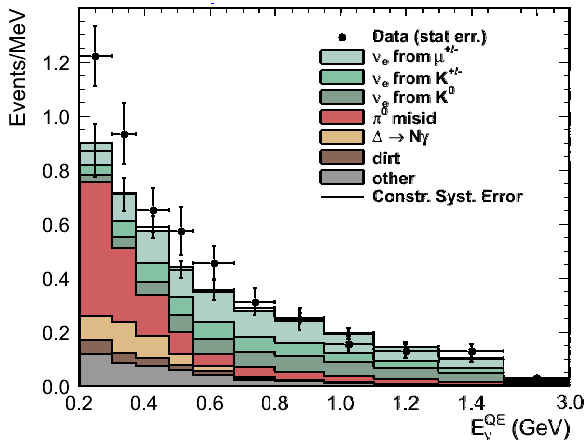
$$L \simeq 541 \text{ m}$$

$$200 \text{ MeV} \leq E \lesssim 3 \text{ GeV}$$



- ▶ agreement with LSND  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  signal ( $E > 475 \text{ MeV}$ )
- ▶ similar  $L/E$  but different  $L$  and  $E \implies$  oscillations
- ▶ CP violation?

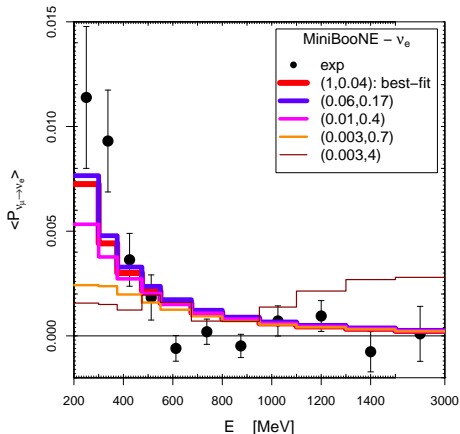
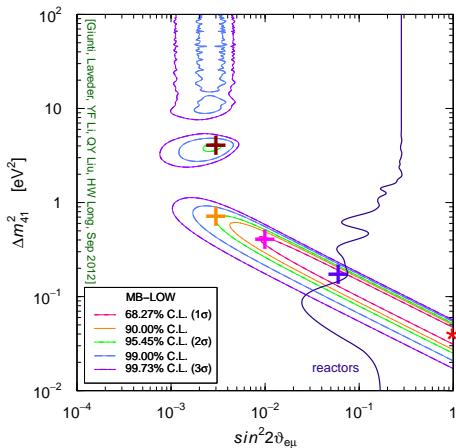
# MiniBooNE $\bar{\nu}$ - Neutrino 2012 - 6 June



	1st half			2nd half		
	data	mc	excess	data	mc	excess
200-475	119	100.5±14.3	18.5 (1.3s)	138	100.0±14.1	38 (2.7s)
475-1250	120	99.1±14.0	20.9 (1.5s)	101	103.1±14.4	-2.2 (-0.2s)

agreement with LSND signal is sadly vanishing

# MiniBooNE $\nu$ and $\bar{\nu}$ - arXiv:1207.4809



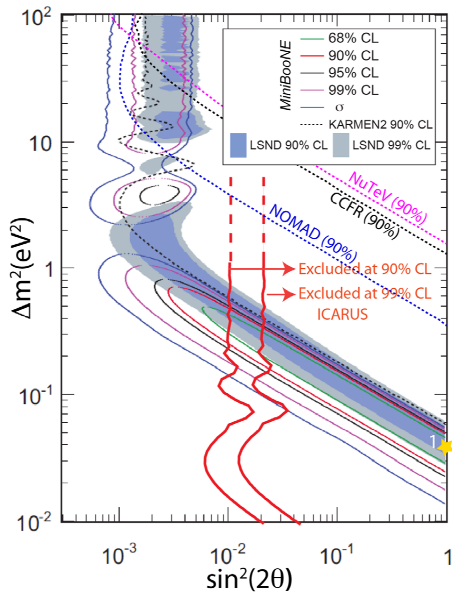
- ▶ Fit of low-energy excess is marginal
- ▶ It requires  $\Delta m_{41}^2 \lesssim 0.4 \text{eV}^2$
- ▶ Neutrino energy reconstruction problem?

[Martini, Ericson, Chanfray, arXiv:1202.4745]

# ICARUS

[arXiv:1209.0122]

- ▶  $\nu_\mu \rightarrow \nu_e$
- ▶  $L = 730 \text{ km}$  (CNGS)
- ▶  $10 < E < 30 \text{ GeV}$
- ▶  $3 \times 10^{-3} < \frac{E}{L} < 9 \times 10^{-3} \text{ eV}^2$
- ▶ 2 observed  $\nu_e$  events
- ▶ 3.7 background  $\nu_e$  events



# Reactor Electron Antineutrino Anomaly

[Mention et al, PRD 83 (2011) 073006]

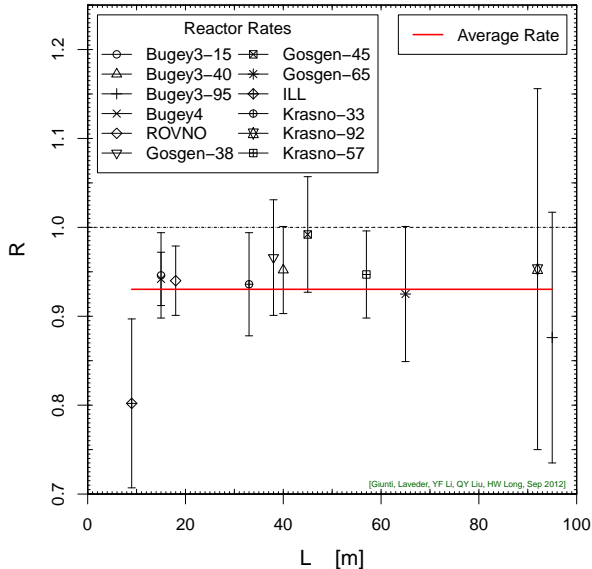
[update in White Paper, arXiv:1204.5379]

new reactor  $\bar{\nu}_e$  fluxes

[Mueller et al, PRC 83 (2011) 054615]

[Huber, PRC 84 (2011) 024617]

$$\bar{R} = 0.930 \pm 0.024$$



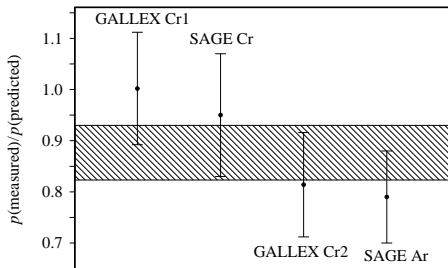
# Gallium Anomaly

## Gallium Radioactive Source Experiments

Tests of the solar neutrino detectors GALLEX (Cr1, Cr2) and SAGE (Cr, Ar)

Detection Process:  $\nu_e + {}^{71}\text{Ga} \rightarrow {}^{71}\text{Ge} + e^-$

$\nu_e$  Sources:  $e^- + {}^{51}\text{Cr} \rightarrow {}^{51}\text{V} + \nu_e$        $e^- + {}^{37}\text{Ar} \rightarrow {}^{37}\text{Cl} + \nu_e$



$$E \sim 0.7 \text{ MeV}$$

$$\langle L \rangle_{\text{GALLEX}} = 1.9 \text{ m}$$

$$\langle L \rangle_{\text{SAGE}} = 0.6 \text{ m}$$

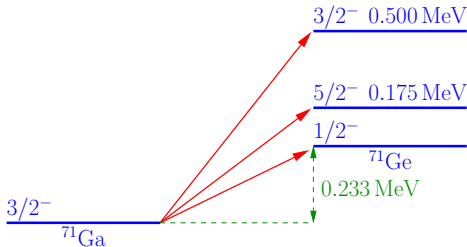
$$\bar{R}_B = 0.86 \pm 0.05$$

[SAGE, PRC 73 (2006) 045805, nucl-ex/0512041]

- ▶ Deficit could be due to overestimate of

$$\sigma(\nu_e + {}^{71}\text{Ga} \rightarrow {}^{71}\text{Ge} + e^-)$$

- ▶ Calculation: Bahcall, PRC 56 (1997) 3391



- ▶  $\sigma_{\text{G.S.}}$  from  $T_{1/2}({}^{71}\text{Ge}) = 11.43 \pm 0.03$  days [Hampel, Remsberg, PRC 31 (1985) 666]

$$\sigma_{\text{G.S.}}({}^{51}\text{Cr}) = 55.3 \times 10^{-46} \text{ cm}^2 (1 \pm 0.004)_{3\sigma}$$

- ▶  $\sigma({}^{51}\text{Cr}) = \sigma_{\text{G.S.}}({}^{51}\text{Cr}) \left( 1 + 0.669 \frac{\text{BGT}_{175}}{\text{BGT}_{\text{G.S.}}} + 0.220 \frac{\text{BGT}_{500}}{\text{BGT}_{\text{G.S.}}} \right)$

- ▶ Contribution of Excited States only 5%!



Krofcheck et al.  
PRL 55 (1985) 1051



$$\frac{\text{BGT}_{175}}{\text{BGT}_{\text{G.S.}}}$$

$$< 0.056$$

$$\frac{\text{BGT}_{500}}{\text{BGT}_{\text{G.S.}}}$$

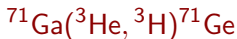
$$0.126 \pm 0.023$$

Haxton  
PLB 431 (1998) 110

Shell Model

$$0.19 \pm 0.18$$

Frekers et al.  
PLB 706 (2011) 134



$$0.039 \pm 0.030$$

$$0.202 \pm 0.016$$

► Haxton:

[Haxton, PLB 431 (1998) 110]

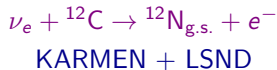
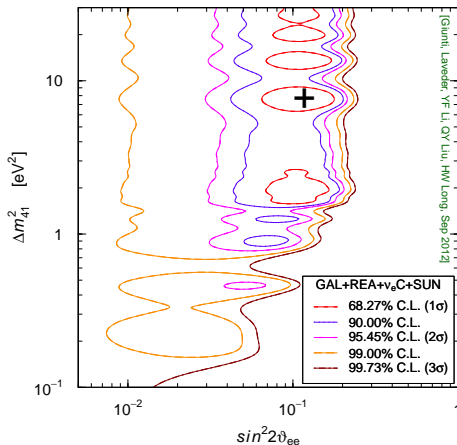
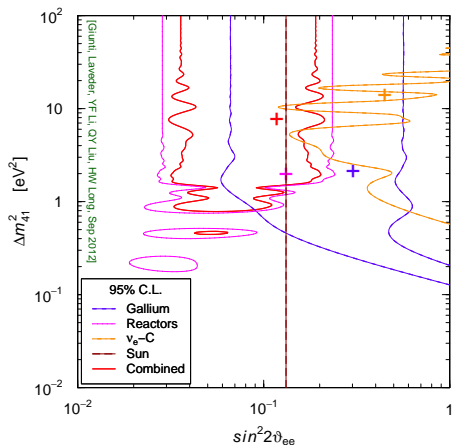
“a sophisticated shell model calculation is performed ... for the transition to the first excited state in  ${}^{71}\text{Ge}$ . The calculation predicts **destructive interference** between the  $(p, n)$  spin and spin-tensor matrix elements”

► Does Haxton argument apply also to  $({}^3\text{He}, {}^3\text{H})$  measurements?

►  $2.7\sigma$  discrepancy of  $\text{BGT}_{500}/\text{BGT}_{\text{G.S.}}$  measurements!

► Anyhow, new  ${}^{71}\text{Ga}({}^3\text{He}, {}^3\text{H}){}^{71}\text{Ge}$  data **support** Gallium Anomaly!

# Global $\nu_e$ and $\bar{\nu}_e$ Disappearance



[Conrad, Shaevitz, PRD 85 (2012) 013017]

[Giunti, Laveder, PLB 706 (2011) 200]

solar  $\nu_e$  + KamLAND  $\bar{\nu}_e$  +  $\vartheta_{13}$

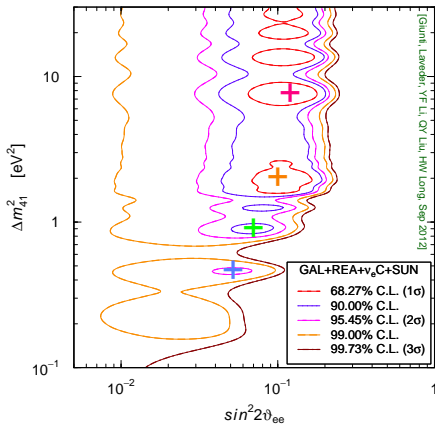
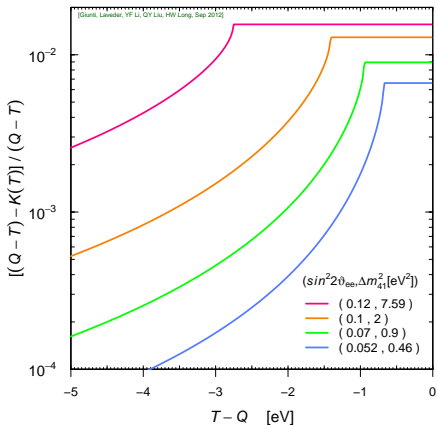
[Giunti, Li, PRD 80 (2009) 113007]

[Palazzo, PRD 83 (2011) 113013]

[Palazzo, PRD 85 (2012) 077301]

[Giunti, Laveder, YF Li, QY Liu, HW Long, Sep 2012]

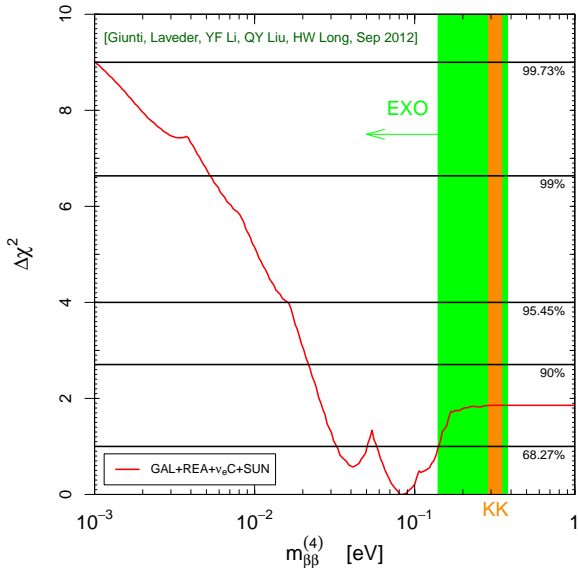
# Testable Implications: $\beta$ Decay



relative deviation of Kurie plot

$$\frac{(Q - T) - K(T)}{Q - T}$$

# Testable Implications: $(\beta\beta)_{0\nu}$ Decay



$$m_{\beta\beta} = \left| \sum_k U_{ek}^2 m_k \right|$$

$$m_{\beta\beta}^{(4)} = |U_{e4}|^2 \sqrt{\Delta m_{41}^2}$$

caveat:  
possible cancellation  
with  $m_{\beta\beta}^{(3\nu-IH)}$

[Rodejohann, arXiv:1206.2560]

# Global 3+1 Fit: Disappearance Constraints

- ▶  $\nu_e$  disappearance experiments:

$$\sin^2 2\vartheta_{ee} = 4|U_{e4}|^2 (1 - |U_{e4}|^2) \simeq 4|U_{e4}|^2$$

- ▶  $\nu_\mu$  disappearance experiments:

$$\sin^2 2\vartheta_{\mu\mu} = 4|U_{\mu4}|^2 (1 - |U_{\mu4}|^2) \simeq 4|U_{\mu4}|^2$$

- ▶  $\nu_\mu \rightarrow \nu_e$  experiments:

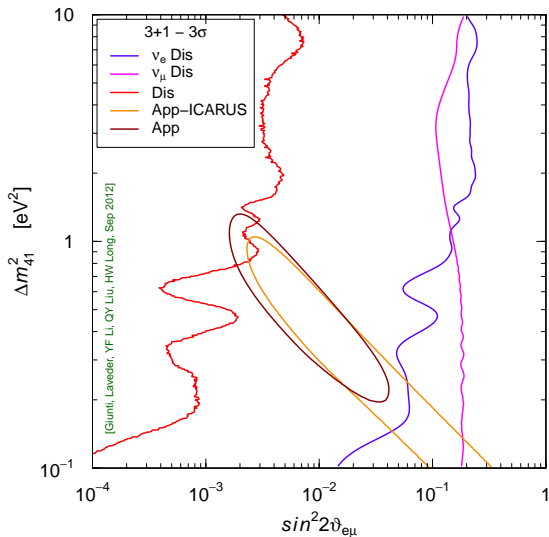
$$\sin^2 2\vartheta_{e\mu} = 4|U_{e4}|^2|U_{\mu4}|^2 \simeq \frac{1}{4} \sin^2 2\vartheta_{ee} \sin^2 2\vartheta_{\mu\mu}$$

- ▶ Upper bounds on  $\sin^2 2\vartheta_{ee}$  and  $\sin^2 2\vartheta_{\mu\mu} \implies$  strong limit on  $\sin^2 2\vartheta_{e\mu}$

[Okada, Yasuda, Int. J. Mod. Phys. A12 (1997) 3669-3694]

[Bilenky, Giunti, Grimus, Eur. Phys. J. C1 (1998) 247]

# 3+1



▶ GoF = 9.3%

▶ PGoF = 0.002%

▶ 3+1 & 3+2 & 3+N:  
App-Dis tension

▶ Tension reduced in  
3+1+NSI

[Akhmedov, Schwetz, JHEP 10 (2010) 115]

▶ No tension in  
3+1+CPTV

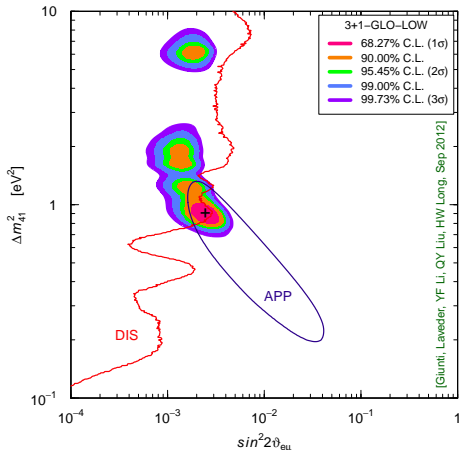
[Barger et al, PLB 576 (2003) 303]

[Giunti, Laveder, PRD 83 (2011) 053006]

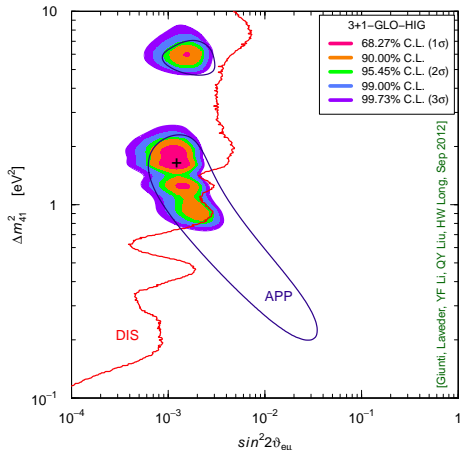
## 3+2

- ▶  $3+2$  is preferred to  $3+1$  only if there is CP-violating difference of  $\nu_\mu \rightarrow \nu_e$  and  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  transitions
- ▶ 2010 MiniBooNE antineutrino data indicated neutrino-antineutrino difference
- ▶ in 2010 it was reasonable and useful to consider  $3+2$
- ▶ neutrino-antineutrino difference almost disappeared with 2012 MiniBooNE antineutrino data
- ▶ in 2012  $3+2$  is reduced to  $3+1$  by Okkam razor shaving

# 3+1 Global Fit



No Osc. GoF = 0.021%  
3+1 GoF = 9.9%  
PGoF = 0.01%



No Osc. GoF = 0.87%  
3+1 GoF = 32%  
PGoF = 0.7%



# Cosmology

- ▶  $N_s$  = number of thermalized sterile neutrinos (not necessarily integer)
- ▶ CMB and LSS in  $\Lambda$ CDM:  $N_s = 1.3 \pm 0.9$   $m_s < 0.66$  eV (95% C.L.)

[Hamann, Hannestad, Raffelt, Tamborra, Wong, PRL 105 (2010) 181301]

$$N_s = 1.61 \pm 0.92 \quad m_s < 0.70 \text{ eV} \quad (95\% \text{ C.L.})$$

[Giusarma, Corsi, Archidiacono, de Putter, Melchiorri, Mena, Pandolfi, PRD 83 (2011) 115023]

- ▶ BBN: 
$$\begin{cases} N_s = 0.22 \pm 0.59 & \text{[Cyburt, Fields, Olive, Skillman, AP 23 (2005) 313]} \\ N_s = 0.64^{+0.40}_{-0.35} & \text{[Izotov, Thuan, ApJL 710 (2010) L67]} \\ N_s \leq 1 \text{ at } 95\% \text{ C.L.} & \text{[Mangano, Serpico, PLB 701 (2011) 296]} \end{cases}$$

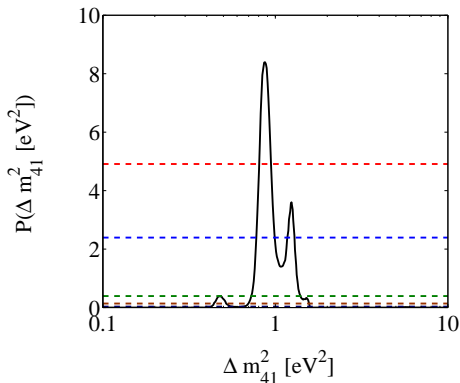
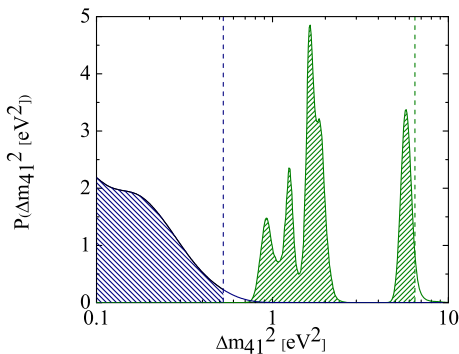
- ▶ CMB+LSS+BBN:  $N_s = 0.85^{+0.39}_{-0.56}$  (95% C.L.)

[Hamann, Hannestad, Raffelt, Wong, JCAP 1109 (2011) 034]

- ▶ Standard  $\Lambda$ CDM: 3+1 allowed, 3+2 disfavored

# Combined Oscillation and Cosmology Fit

[Archidiacono, Fornengo, Giunti, Melchiorri, arXiv:1207.6515]



- ▶ Mass Hierarchy:  $m_4 \gg m_3, m_2, m_1 \implies m_4 \simeq \sqrt{\Delta m_{41}^2}$
- ▶ Cosmology:  $m_4 < 0.73 \text{ eV}^2$  (95% Bayesian CL)
- ▶ Oscillation + Cosmology:  $0.85 < m_4 < 1.18 \text{ eV}^2$  (95% Bayesian CL)

# Conclusions

- ▶ Short-baseline neutrino oscillation anomalies  $\implies$  sterile neutrinos
- ▶ After 2010 excitement Short-Baseline  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  Signal is not feeling well:
  - ▶ MiniBooNE 2012 antineutrino data are similar to neutrino data (LSND signal diminished and low-energy anomaly appeared)
  - ▶ Probably there is no CP violation  $\implies$  no need of 3+2
  - ▶ The decrease of MiniBooNE-LSND agreement is discouraging
  - ▶ Better experiments are needed to clarify situation  
ICARUS/Nessie@CERN [Stanco, Gibin, NOW2012]
- ▶ Short-Baseline  $\nu_e$  and  $\bar{\nu}_e$  Disappearance is in good health:
  - ▶ Reactor  $\bar{\nu}_e$  anomaly is alive and exciting
  - ▶ Gallium  $\nu_e$  anomaly strengthened by new cross-section measurements
  - ▶ Many promising projects to test short-baseline  $\nu_e$  and  $\bar{\nu}_e$  disappearance in a few years with reactors, radioactive sources and accelerators  
[Ianni, Link, Gaffiot, NOW2012; Ranucci, NPB2012]
  - ▶ Independent tests through effects of  $m_4$  in  $\beta$ -decay and  $(\beta\beta)_{0\nu}$ -decay