

# Phenomenology of Light Sterile Neutrinos

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Neutrino Unbound: <http://www.nu.to.infn.it>

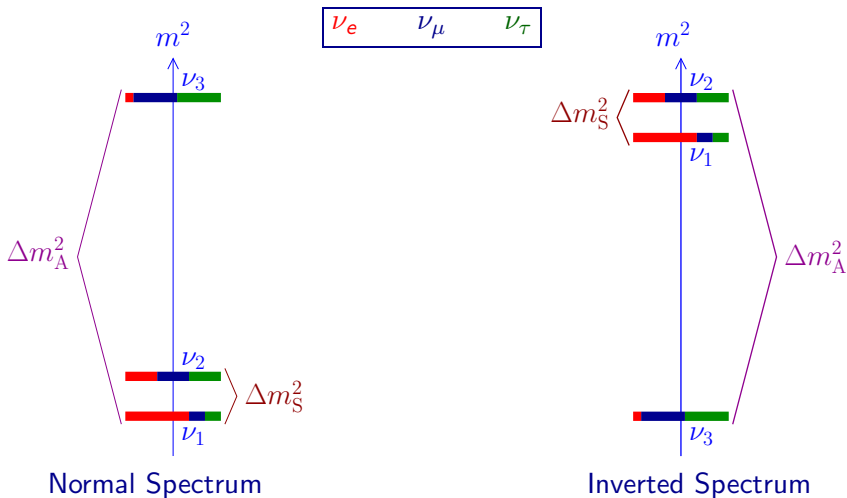


NuPhys2014: Prospects in Neutrino Physics

Queen Mary, University of London, UK

15-17 December 2014

# Three-Neutrino Mixing Paradigm



absolute mass scale  $\lesssim 1$  eV

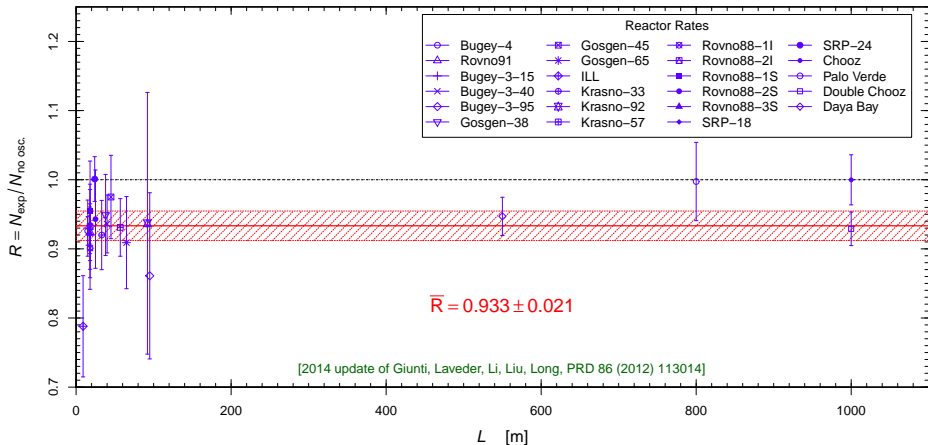
# Indications of SBL Oscillations Beyond $3\nu$

# Reactor Electron Antineutrino Anomaly

[Mention et al, PRD 83 (2011) 073006; update in White Paper, arXiv:1204.5379]

New reactor  $\bar{\nu}_e$  fluxes

[Mueller et al, PRC 83 (2011) 054615; Huber, PRC 84 (2011) 024617]



$$\bar{\nu}_e \rightarrow \bar{\nu}_e$$

$$L \simeq 10 - 100 \text{ m}$$

$$E \simeq 4 \text{ MeV}$$

$\sim 3.1\sigma$  deficit

$$\Delta m^2 \gtrsim 0.5 \text{ eV}^2$$

$$(\gg \Delta m_A^2 \gg \Delta m_S^2)$$

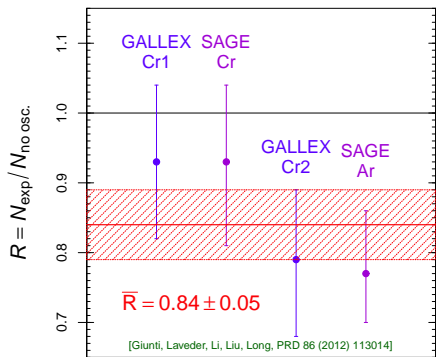
[see also: Sinev, arXiv:1103.2452; Ciuffoli, Evslin, Li, JHEP 12 (2012) 110; Zhang, Qian, Vogel, PRD 87 (2013) 073018; Kopp, Machado, Maltoni, Schwetz, JHEP 1305 (2013) 050; Ivanov et al, PRC 88 (2013) 055501]

# Gallium Anomaly

## Gallium Radioactive Source Experiments: GALLEX and SAGE

Detection Process:  $\nu_e + {}^{71}\text{Ga} \rightarrow {}^{71}\text{Ge} + e^-$

$\nu_e$  Sources:  $e^- + {}^{51}\text{Cr} \rightarrow {}^{51}\text{V} + \nu_e$        $e^- + {}^{37}\text{Ar} \rightarrow {}^{37}\text{Cl} + \nu_e$



$\bar{\nu}_e \rightarrow \bar{\nu}_e$        $E \sim 0.7 \text{ MeV}$

$\langle L \rangle_{\text{GALLEX}} = 1.9 \text{ m}$

$\langle L \rangle_{\text{SAGE}} = 0.6 \text{ m}$

$\sim 2.9\sigma$  anomaly

$\Delta m^2 \gtrsim 1 \text{ eV}^2$  ( $\gg \Delta m_A^2 \gg \Delta m_S^2$ )

[SAGE, PRC 73 (2006) 045805; PRC 80 (2009) 015807]

[Laveder et al, Nucl.Phys.Proc.Suppl. 168 (2007) 344;  
MPLA 22 (2007) 2499; PRD 78 (2008) 073009;  
PRC 83 (2011) 065504]

[Mention et al, PRD 83 (2011) 073006]

- ▶  ${}^3\text{He} + {}^{71}\text{Ga} \rightarrow {}^{71}\text{Ge} + {}^3\text{H}$  cross section measurement [Frekers et al., PLB 706 (2011) 134]
- ▶  $E_{\text{th}}(\nu_e + {}^{71}\text{Ga} \rightarrow {}^{71}\text{Ge} + e^-) = 233.5 \pm 1.2 \text{ keV}$  [Frekers et al., PLB 722 (2013) 233]

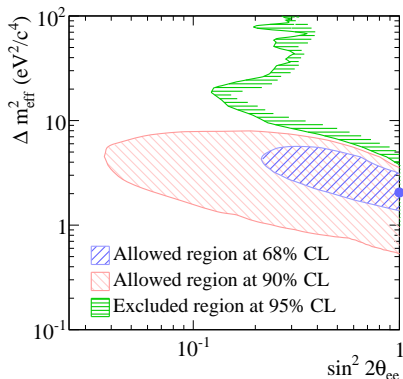
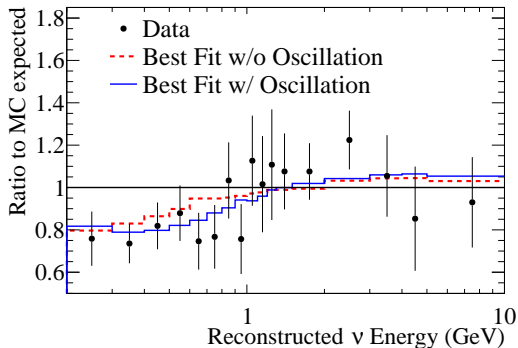
# T2K Near Detector $\nu_e$ Disappearance

[arXiv:1410.8811]

$\nu_e \rightarrow \nu_e$

$L \simeq 280$  m

$E \sim 500$  MeV



No Oscillations:  $\chi^2_{\min}/\text{NDF} = 45.86/51$

Oscillations:  $\chi^2_{\min}/\text{NDF} = 42.16/49$

$\Delta\chi^2/\text{NDF} = 3.7/2$

$\sim 1.4\sigma$  deviation

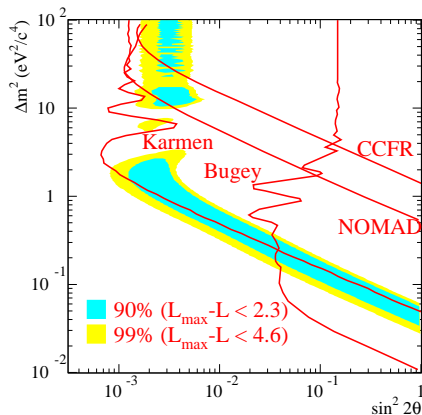
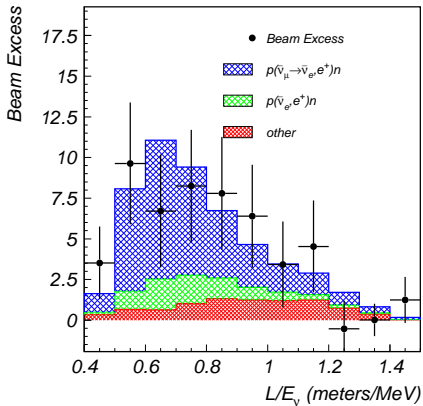
# LSND

[PRL 75 (1995) 2650; PRC 54 (1996) 2685; PRL 77 (1996) 3082; PRD 64 (2001) 112007]

$$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$$

$$L \simeq 30 \text{ m}$$

$$20 \text{ MeV} \leq E \leq 200 \text{ MeV}$$



3.8 $\sigma$  excess

$$\Delta m^2 \gtrsim 0.2 \text{ eV}^2 \quad (\gg \Delta m_A^2 \gg \Delta m_S^2)$$

# MiniBooNE

$L \simeq 541 \text{ m}$

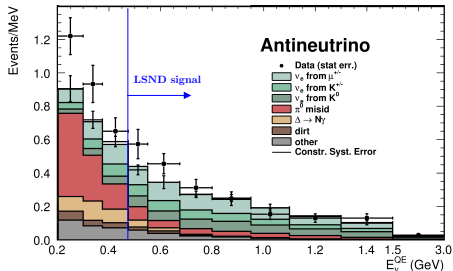
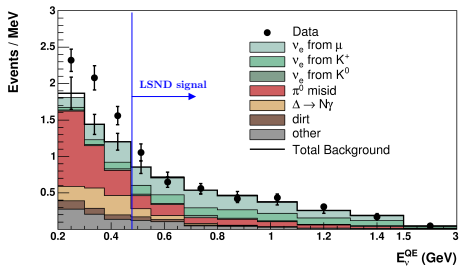
$200 \text{ MeV} \leq E \lesssim 3 \text{ GeV}$

$\nu_\mu \rightarrow \nu_e$

[PRL 102 (2009) 101802]

$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$

[PRL 110 (2013) 161801]

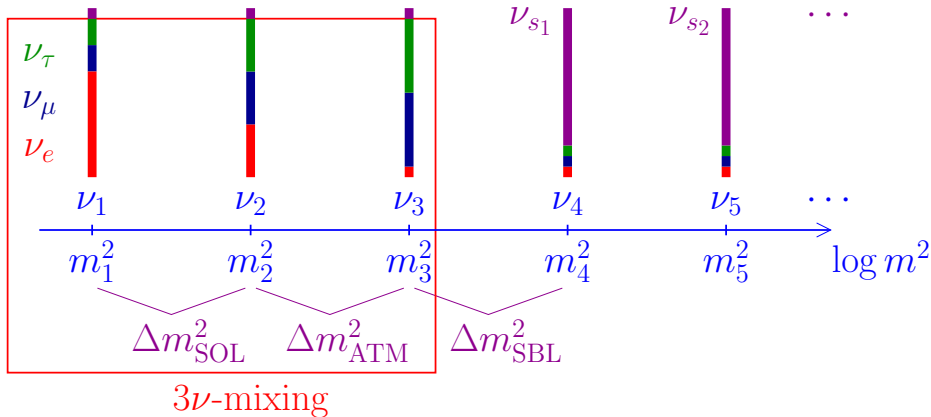


- ▶ Purpose: check LSND signal.
- ▶ Different  $L$  and  $E$ .
- ▶ Similar  $L/E$  (oscillations).
- ▶ LSND signal:  $E > 475 \text{ MeV}$ .

- ▶ Agreement with LSND signal?
- ▶ CP violation?
- ▶ Low-energy anomaly!



# Beyond Three-Neutrino Mixing: Sterile Neutrinos



Terminology: a eV-scale sterile neutrino  
means: a eV-scale massive neutrino which is mainly sterile

# Light Sterile Neutrinos

- ▶ New particles beyond the standard model!
- ▶ Sterile means **no standard model interactions**  
[Pontecorvo, Sov. Phys. JETP 26 (1968) 984]
- ▶ Active neutrinos ( $\nu_e, \nu_\mu, \nu_\tau$ ) can oscillate into light sterile neutrinos ( $\nu_s$ )
- ▶ Observables:
  - ▶ **Disappearance** of active neutrinos (neutral current deficit)
  - ▶ Indirect evidence through **combined fit of data** (current indication)
- ▶ Short-baseline anomalies +  $3\nu$ -mixing:

$$\begin{array}{ccccc} \Delta m_{21}^2 & \ll & |\Delta m_{31}^2| & \ll & |\Delta m_{41}^2| \leq \dots \\ \nu_1 & & \nu_2 & & \nu_3 & & \nu_4 & & \dots \\ \nu_e & & \nu_\mu & & \nu_\tau & & \nu_{s1} & & \dots \end{array}$$

# Effective SBL Oscillation Probabilities in 3+1 Schemes

$$P_{\nu_\alpha \rightarrow \nu_\beta}^{\text{SBL}(-)(-)} \simeq \sin^2 2\vartheta_{\alpha\beta} \sin^2 \left( \frac{\Delta m_{41}^2 L}{4E} \right)$$


$$\sin^2 2\vartheta_{\alpha\beta} = 4|U_{\alpha 4}|^2 |U_{\beta 4}|^2$$

$$P_{\nu_\alpha \rightarrow \nu_\alpha}^{\text{SBL}(-)(-)} \simeq 1 - \sin^2 2\vartheta_{\alpha\alpha} \sin^2 \left( \frac{\Delta m_{41}^2 L}{4E} \right)$$

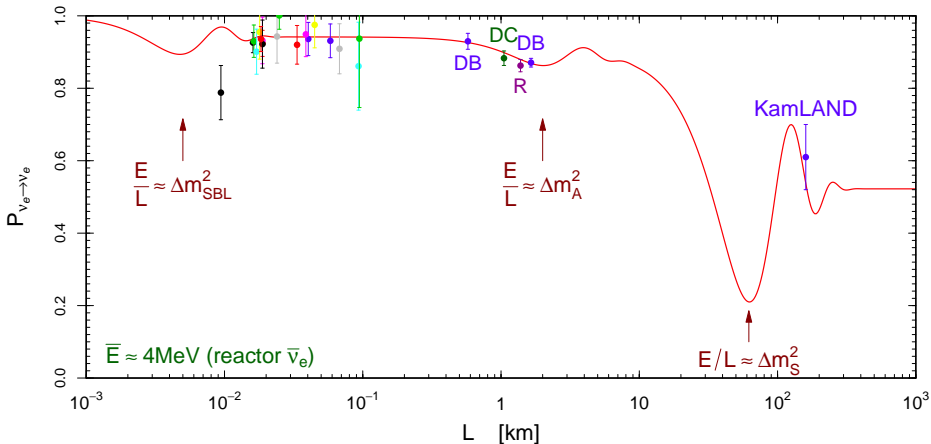
$$\sin^2 2\vartheta_{\alpha\alpha} = 4|U_{\alpha 4}|^2 (1 - |U_{\alpha 4}|^2)$$

Perturbation of  $3\nu$  Mixing:  $|U_{e4}|^2 \ll 1$ ,  $|U_{\mu 4}|^2 \ll 1$ ,  $|U_{\tau 4}|^2 \ll 1$ ,  $|U_{s4}|^2 \simeq 1$

$$U = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} & U_{\mu 4} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} & U_{\tau 4} \\ U_{s1} & U_{s2} & U_{s3} & U_{s4} \end{pmatrix}$$


  
 SBL

- ▶ 6 mixing angles
- ▶ 3 Dirac CP phases
- ▶ 3 Majorana CP phases
- ▶ But CP violation is not observable in current SBL experiments!
- ▶ May be observable in future high-precision solar exp. sensitive to  $\Delta m_{21}^2$  [Long, Li, Giunti, PRD 87, 113004 (2013) 113004] and accelerator exp. sensitive to  $\Delta m_{31}^2$  [de Gouvea, Kelly, Kobach, arXiv:1412.1479]



$$P_{\nu_e \rightarrow \nu_e}^{(-)(-)\text{LBL}} \simeq 1 - \frac{1}{2} \sin^2 2\vartheta_{14} - \cos^4 \vartheta_{14} \sin^2 2\vartheta_{13} \sin^2 \left( \frac{\Delta m_{31}^2 L}{4E} \right)$$

## 3+1: Appearance vs Disappearance

- ▶  $\nu_e$  disappearance experiments:

$$\sin^2 2\vartheta_{ee} = 4|U_{e4}|^2 (1 - |U_{e4}|^2) \simeq 4|U_{e4}|^2$$

- ▶  $\nu_\mu$  disappearance experiments:

$$\sin^2 2\vartheta_{\mu\mu} = 4|U_{\mu4}|^2 (1 - |U_{\mu4}|^2) \simeq 4|U_{\mu4}|^2$$

- ▶  $\nu_\mu \rightarrow \nu_e$  experiments:

$$\sin^2 2\vartheta_{e\mu} = 4|U_{e4}|^2 |U_{\mu4}|^2 \simeq \frac{1}{4} \sin^2 2\vartheta_{ee} \sin^2 2\vartheta_{\mu\mu}$$

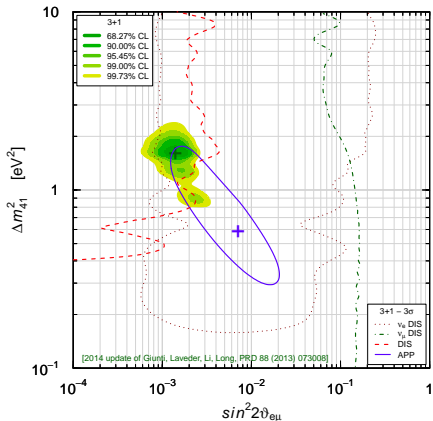
- ▶ Upper bounds on  $\sin^2 2\vartheta_{ee}$  and  $\sin^2 2\vartheta_{\mu\mu} \implies$  strong limit on  $\sin^2 2\vartheta_{e\mu}$

[Okada, Yasuda, IJMPA 12 (1997) 3669; Bilenky, Giunti, Grimus, EPJC 1 (1998) 247]

- ▶ Similar constraint in  $3+2, 3+3, \dots, 3+N_s$  !

# Global 3+1 Fit

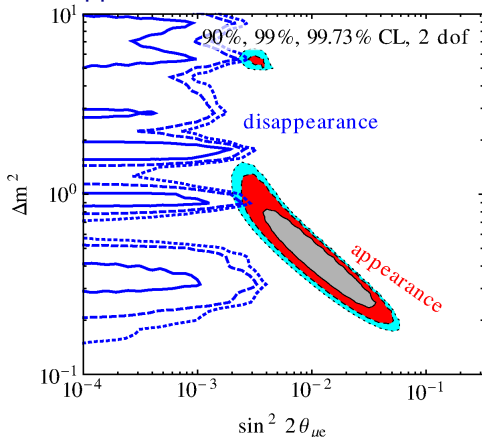
Our Fit



GoF = 5%

PGoF = 0.1%

Kopp, Machado, Maltoni, Schwetz

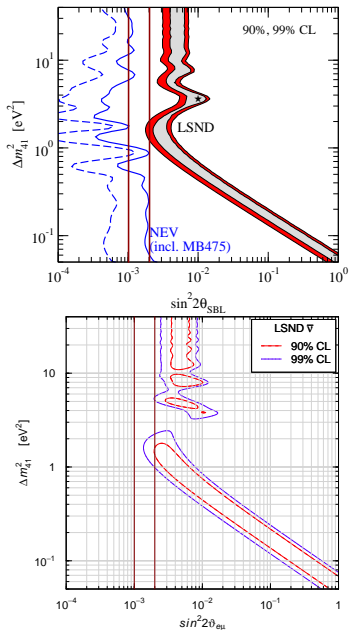


GoF = 19%

PGoF = 0.01%

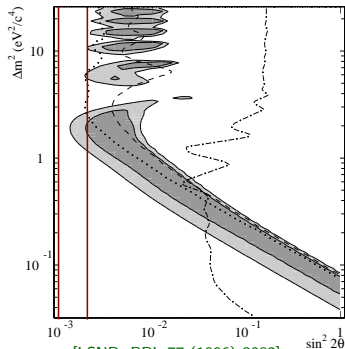
[Kopp, Machado, Maltoni, Schwetz, JHEP 1305 (2013) 050]

# Different LSND Treatments



← Kopp, Machado, Maltoni, Schwetz

[from Maltoni, Schwetz, PRD 76 (2007) 093005]



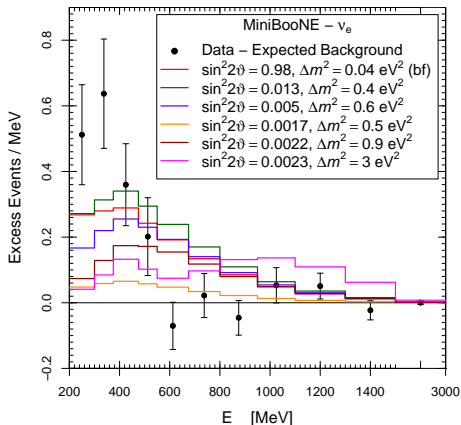
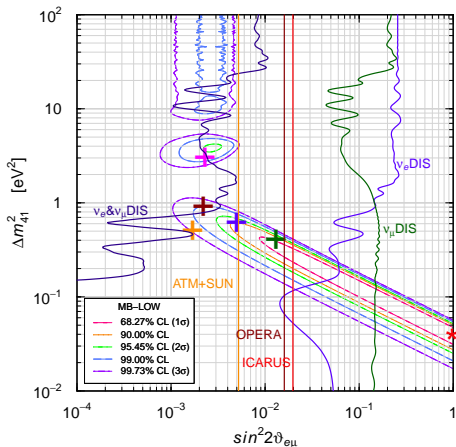
only  $\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu$  decay at rest data

difficult (impossible?) to determine best analysis because of lack of information

← Our Fit

[improvement of Giunti, Laveder, PRD 82 (2010) 093016]

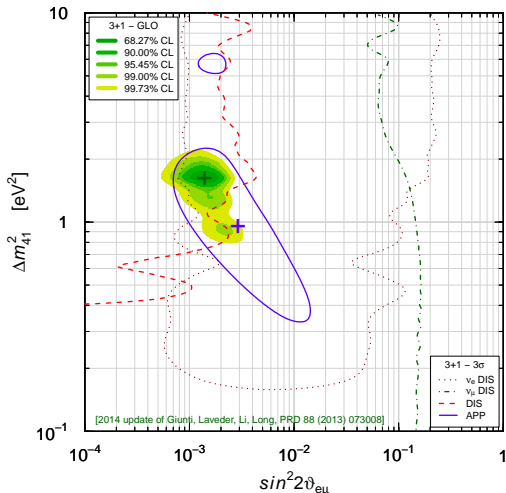
# MiniBooNE Low-Energy Excess?



- ▶ No fit of low-energy excess for realistic  $\sin^2 2\vartheta_{e\mu} \lesssim 5 \times 10^{-3}$
- ▶ APP-DIS PGoF = 0.1%
- ▶ Neutrino energy reconstruction problem? [Martini, Ericson, Chanfray, PRD 87 (2013) 013009]
- ▶ Pragmatic Approach: discard the Low-Energy Excess because it is very likely not due to oscillations



# Pragmatic 3+1 Fit



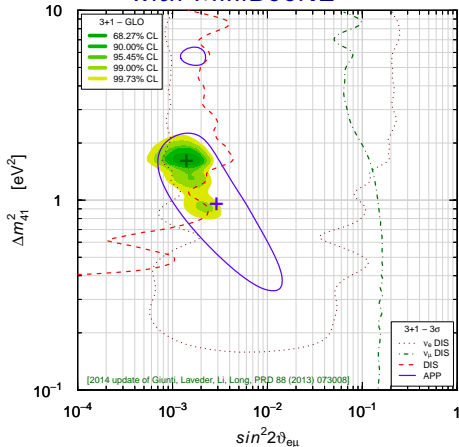
MiniBooNE  $E > 475$  MeV  
 GoF = 26%      PGoF = 7%

- ▶ APP  $\nu_\mu \rightarrow \nu_e$  &  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ :  
 LSND ( $\nu_s$ ), MiniBooNE (?),  
 OPERA ( ~~$\nu_s$~~ ), ICARUS ( ~~$\nu_s$~~ ),  
 KARMEN ( ~~$\nu_s$~~ ),  
 NOMAD ( ~~$\nu_s$~~ ), BNL-E776 ( ~~$\nu_s$~~ )
- ▶ DIS  $\nu_e$  &  $\bar{\nu}_e$ : Reactors ( $\nu_s$ ),  
 Gallium ( $\nu_s$ ),  $\nu_e$ C ( ~~$\nu_s$~~ ),  
 Solar ( ~~$\nu_s$~~ )
- ▶ DIS  $\nu_\mu$  &  $\bar{\nu}_\mu$ : CDHSW ( ~~$\nu_s$~~ ),  
 MINOS ( ~~$\nu_s$~~ ),  
 Atmospheric ( ~~$\nu_s$~~ ),  
 MiniBooNE/SciBooNE ( ~~$\nu_s$~~ )

No Osc. disfavored at  $6.3\sigma$   
 $\Delta\chi^2/\text{NDF} = 47.7/3$

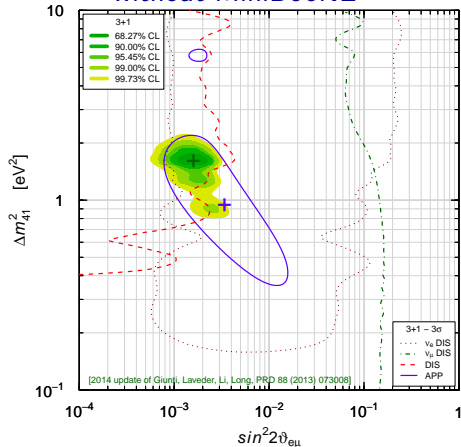
# MiniBooNE Impact in Pragmatic 3+1 Fit?

with MiniBooNE



GoF = 26%      PGoF = 7%  
 No Osc. disfavored at  $6.3\sigma$   
 $\Delta\chi^2/\text{NDF} = 47.7/3$

without MiniBooNE



GoF = 16%      PGoF = 5%  
 No Osc. disfavored at  $6.4\sigma$   
 $\Delta\chi^2/\text{NDF} = 48.1/3$

Without LSND: No Osc. disfavored only at  $2.6\sigma$  ( $\Delta\chi^2/\text{NDF} = 11.4/3$ )

# Effective SBL Oscillation Probabilities in 3+2 Schemes

$$\phi_{kj} = \Delta m_{kj}^2 L / 4E$$

$$\eta = \arg[U_{e4}^* U_{\mu 4} U_{e5} U_{\mu 5}^*]$$

$$P_{\nu_{\mu} \rightarrow \nu_e}^{(-) \quad (-)} = 4|U_{e4}|^2 |U_{\mu 4}|^2 \sin^2 \phi_{41} + 4|U_{e5}|^2 |U_{\mu 5}|^2 \sin^2 \phi_{51} \\ + 8|U_{\mu 4} U_{e4} U_{\mu 5} U_{e5}| \sin \phi_{41} \sin \phi_{51} \cos(\phi_{54} \overset{(+)}{-} \eta)$$

$$P_{\nu_{\alpha} \rightarrow \nu_{\alpha}}^{(-) \quad (-)} = 1 - 4(1 - |U_{\alpha 4}|^2 - |U_{\alpha 5}|^2)(|U_{\alpha 4}|^2 \sin^2 \phi_{41} + |U_{\alpha 5}|^2 \sin^2 \phi_{51}) \\ - 4|U_{\alpha 4}|^2 |U_{\alpha 5}|^2 \sin^2 \phi_{54}$$

[Sorel, Conrad, Shaevitz, PRD 70 (2004) 073004; Maltoni, Schwetz, PRD 76 (2007) 093005; Karagiorgi et al, PRD 80 (2009) 073001; Kopp, Maltoni, Schwetz, PRL 107 (2011) 091801; Giunti, Laveder, PRD 84 (2011) 073008; Donini et al, JHEP 07 (2012) 161; Archidiacono et al, PRD 86 (2012) 065028; Conrad et al, AHEP 2013 (2013) 163897; Archidiacono et al, PRD 87 (2013) 125034; Kopp, Machado, Maltoni, Schwetz, JHEP 1305 (2013) 050; Giunti, Laveder, Y.F. Li, H.W. Long, PRD 88 (2013) 073008; Girardi, Meroni, Petcov, JHEP 1311 (2013) 146]

► Good: CP violation

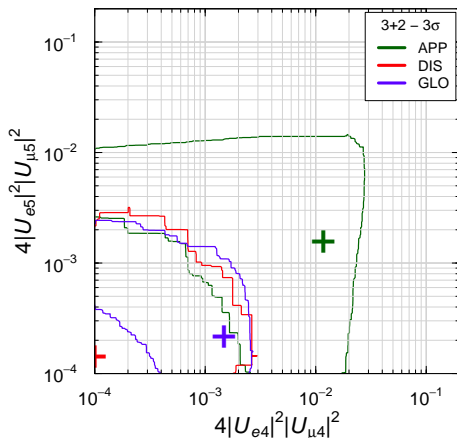
► Bad: Two massive sterile neutrinos at the eV scale!

4 more parameters:  $\underbrace{\Delta m_{41}^2, |U_{e4}|^2, |U_{\mu 4}|^2, \Delta m_{51}^2, |U_{e5}|^2, |U_{\mu 5}|^2, \eta}_{3+1}$

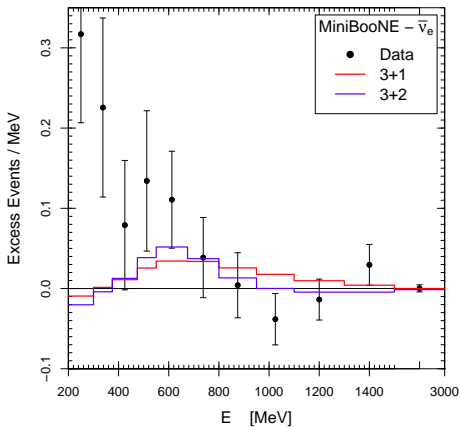
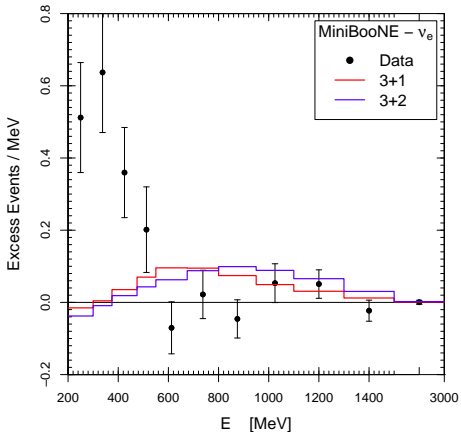
Global Fits	Our Fit		KMMS	
	3+1	3+2	3+1	3+2
GoF	5%	7%	19%	23%
PGoF	0.1%	0.04%	0.01%	0.003%

- ▶ Our Fit: 2014 update of Giunti, Laveder, Li, Long, PRD 88 (2013) 073008
- ▶ KMMS: Kopp, Machado, Maltoni, Schwetz, JHEP 1305 (2013) 050

APP-DIS 3+2 Tension:



# 3+2 cannot fit MiniBooNE Low-Energy Excess

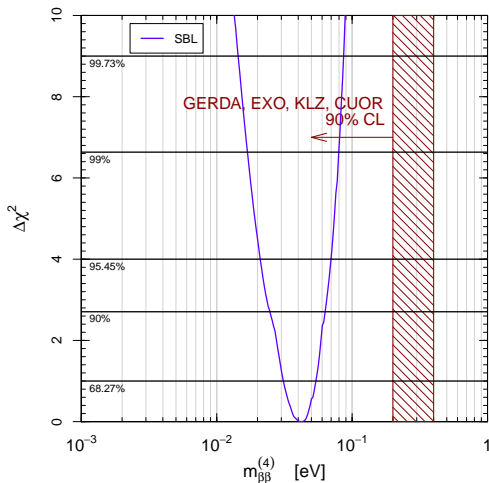


- ▶ Note difference between 3+2  $\nu_e$  and  $\bar{\nu}_e$  histograms due to CP violation
- ▶ 3+2 can fit slightly better the small  $\bar{\nu}_e$  excess at about 600 MeV
- ▶ 3+2 fit of low-energy excess as bad as 3+1
- ▶ Claims that 3+2 can fit low-energy excess do not take into account constraints from other data

# No need of 3+2

- ▶ 3+2 should be preferred to 3+1 if
  - ▶ there is consistent evidence of two peaks of the probability corresponding to two  $\Delta m^2$ 's
  - ▶ there is CP-violating difference of  $\nu_\mu \rightarrow \nu_e$  and  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  transitions
- ▶ MiniBooNE low-energy peak not consistent with disappearance constraints
- ▶ final  $\nu_e + 2010 \bar{\nu}_e$  MiniBooNE data indicated  $\nu_e - \bar{\nu}_e$  difference
  - ⇓
  - reasonable and useful to consider 3+2
- ▶  $\nu_e - \bar{\nu}_e$  difference almost disappeared with 2012 final MiniBooNE  $\bar{\nu}_e$  data
- ▶ PGoF of 3+2 is even worse than that of 3+1!
- ▶ 3+2 has more tension with cosmological data than 3+1
- ▶ Conclusion: forget 3+2! (at least until new data require it)

# Neutrinoless Double- $\beta$ Decay



[Giunti, Laveder, Li, Long, 2014]

Pragmatic 3+1 Fit

$$|m_{\beta\beta}| = \left| \sum_{k=1}^4 U_{ek}^2 m_k \right|$$

$$m_{\beta\beta}^{(4)} = |U_{e4}|^2 \sqrt{\Delta m_{41}^2}$$

caveat:  
 possible cancellation  
 with  $m_{\beta\beta}^{(3\nu-IH)}$

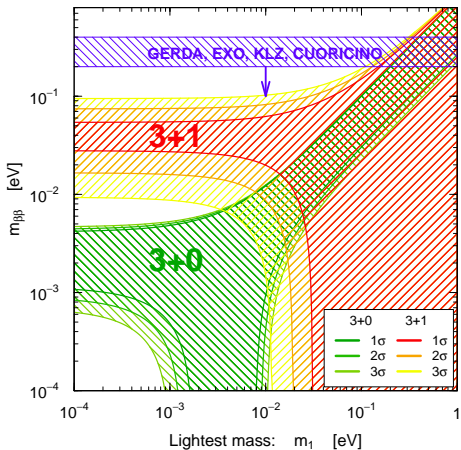
[Barry et al, JHEP 07 (2011) 091]

[Li, Liu, PLB 706 (2012) 406]

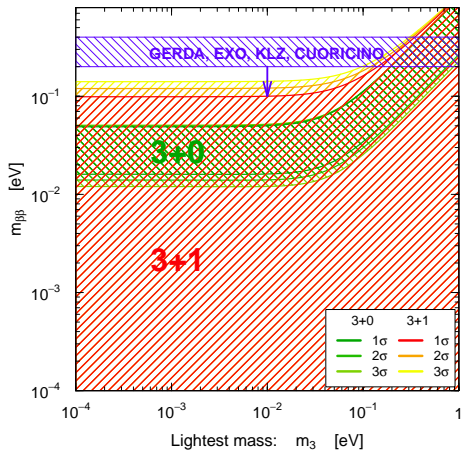
[Rodejohann, JPG 39 (2012) 124008]

[Girardi, Meroni, Petcov, JHEP 1311 (2013) 146]

## Normal $3\nu$ Spectrum



## Inverted $3\nu$ Spectrum



[Giunti, Laveder, Li, Long, 2014]



# Conclusions

- ▶ Short-Baseline  $\nu_e$  and  $\bar{\nu}_e$  Disappearance:
  - ▶ Experimental data agree on Reactor  $\bar{\nu}_e$  and Gallium  $\nu_e$  anomalies.
  - ▶ Problem: systematic uncertainties.
  - ▶ Many promising projects to test unambiguously short-baseline  $\nu_e$  and  $\bar{\nu}_e$  disappearance in a few years with reactors and radioactive sources.
  - ▶ Independent tests through effect of  $m_4$  in  $\beta$ -decay and  $\beta\beta_{0\nu}$ -decay.
- ▶ Short-Baseline  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  LSND Signal:
  - ▶ Not seen by other SBL  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  experiments.
  - ▶ MiniBooNE experiment has been inconclusive.
  - ▶ Experiments with near detector are needed to check LSND signal!
  - ▶ If  $|U_{e4}| > 0$  why not  $|U_{\mu 4}| > 0$ ?  $\implies \sin^2 2\vartheta_{e\mu} = 4|U_{e4}|^2|U_{\mu 4}|^2 > 0$
- ▶ Pragmatic 3+1 Fit is fine: moderate APP-DIS tension.
- ▶ 3+2 is not needed: same APP-DIS tension as 3+1 and no evidence of CP violation.