

Concluding Remarks

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4–8 April 2016, ECT*, Trento

2015 Physics Nobel Prize

FOR THE DISCOVERY OF NEUTRINO OSCILLATIONS,
WHICH SHOWS THAT NEUTRINOS HAVE MASS

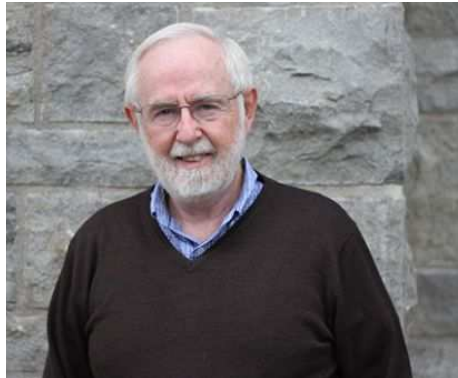
1998: Oscillations of atmospheric neutrinos observed by the Super-Kamiokande experiment

Takaaki Kajita



2002: Oscillations of solar neutrinos observed by the SNO experiment

Arthur B. McDonald

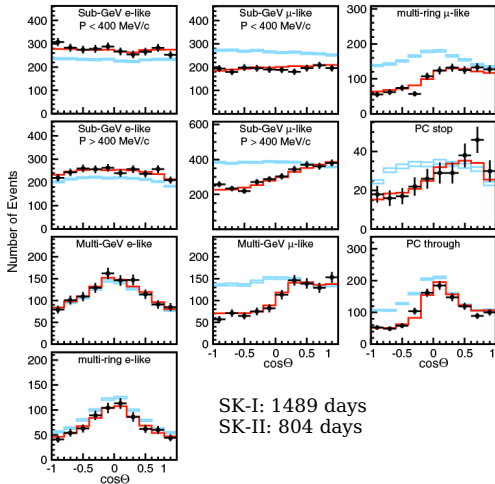


i-3 sector: θ_{i3} and Δm^2_{3i}

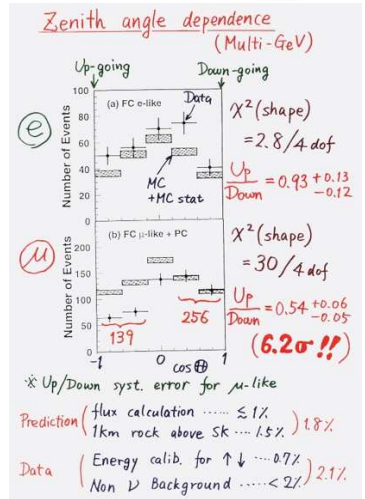
($i=1,2$)



atmospheric neutrinos:



SK-I: 1489 days
SK-II: 804 days

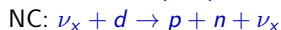


1-2 sector: θ_{12} and Δm^2_{21}

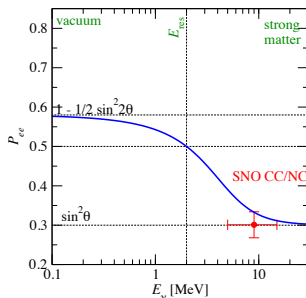


MSW conversion in the Sun

2002: SNO: CC to NC ratio of solar neutrino flux



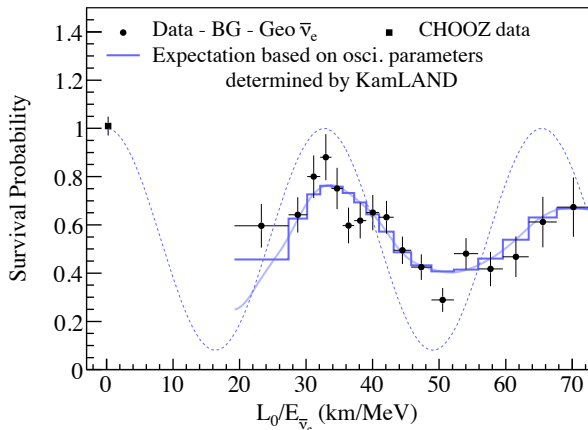
- ▶ evidence for $\nu_e \rightarrow \nu_\mu, \nu_\tau$ conversion
- ▶ **MSW effect** inside the sun
adiabatic conversion through resonance
- ▶ fixes ordering of the 1-2 mass states



$$P_{ee} = \frac{\phi_e}{\phi_e + \phi_\mu + \phi_\tau} = \frac{\phi_{CC}}{\phi_{NC}}$$

1-2 sector: θ_{12} and Δm^2_{21}

Evidence for spectral distortion: KamLAND 2004



see also Marco Drewes talk

Textbook Example: type I seesaw

introduce $N_R \sim (1, 0)$, automatically has two possible couplings:

- couples to $g_\nu \bar{L} \tilde{\Phi} \sim (1, 0)$, becomes $g_\nu v \bar{\nu}_L N_R \equiv m_D \bar{\nu}_L N_R$
- in addition: Majorana mass term for N_R : $\frac{1}{2} M_R \overline{N_R^c} N_R$

$$\mathcal{L} = \frac{1}{2} (\bar{\nu}_L, \overline{N_R^c}) \begin{pmatrix} 0 & m_D \\ m_D & M_R \end{pmatrix} \begin{pmatrix} \nu_L^c \\ N_R \end{pmatrix} + h.c.$$

$$\equiv \frac{1}{2} \bar{\Psi} \mathcal{M}_\nu \Psi^c + h.c.$$

diagonalization gives $\text{diag}(m_\nu, M)$ with (in limit $M_R \gg m_D$)

$$m_\nu = m_D^2/M_R \text{ and } M = M_R$$

MASSIVE MAJORANA NEUTRINOS!

Paths to Neutrino Mass

approach	ingredient	quantum number of messenger	\mathcal{L}	m_ν	scale
"SM" (Dirac mass)	RH ν	$N_R \sim (1, 0)$	$h \overline{N_R} \Phi L$	$h v$	$h = \mathcal{O}(10^{-12})$
"effective" (dim 5 operator)	new scale + LNV	-	$h \overline{L^c} \Phi \Phi L$	$\frac{h v^2}{\Lambda}$	$\Lambda = 10^{14} \text{ GeV}$
"direct" (type II seesaw)	Higgs triplet + LNV	$\Delta \sim (3, -2)$	$h \overline{L^c} \Delta L + \mu \Phi \Phi \Delta$	$h v_T$	$\Lambda = \frac{1}{h \mu} M_\Delta^2$
"indirect 1" (type I seesaw)	RH ν + LNV	$N_R \sim (1, 0)$	$h \overline{N_R} \Phi L + \overline{N_R} M_R N_R^c$	$\frac{(h v)^2}{M_R}$	$\Lambda = \frac{1}{h} M_R$
"indirect 2" (type III seesaw)	fermion triplets + LNV	$\Sigma \sim (3, 0)$	$h \overline{\Sigma} L \Phi + \text{Tr} \overline{\Sigma} M_\Sigma \Sigma$	$\frac{(h v)^2}{M_\Sigma}$	$\Lambda = \frac{1}{h} M_\Sigma$

plus seesaw variants (linear, double, inverse, ...)

plus radiative mechanisms

plus extra dimensions

plusplus

Common to essentially all mechanisms
 “3 Majorana neutrino paradigm”

at low energies:

$$\mathcal{L} = \frac{1}{2} \nu^T m_\nu \nu \quad \text{with} \quad m_\nu = U \text{diag}(m_1, m_2, m_3) U^T$$

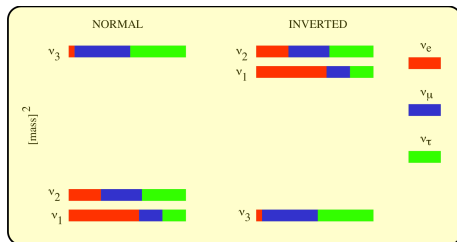
with PMNS matrix

$$U = \begin{pmatrix} c_{12} c_{13} & s_{12} c_{13} & s_{13} e^{-i\delta} \\ -s_{12} c_{23} - c_{12} s_{23} s_{13} e^{i\delta} & c_{12} c_{23} - s_{12} s_{23} s_{13} e^{i\delta} & s_{23} c_{13} \\ s_{12} s_{23} - c_{12} c_{23} s_{13} e^{i\delta} & -c_{12} s_{23} - s_{12} c_{23} s_{13} e^{i\delta} & c_{23} c_{13} \end{pmatrix} P$$

with $P = \text{diag}(e^{i\alpha}, e^{i\beta}, 1)$ (\leftrightarrow Majorana, lepton number violation)

\Rightarrow 3 angles, 3 phases, 3 masses

3-flavour oscillations

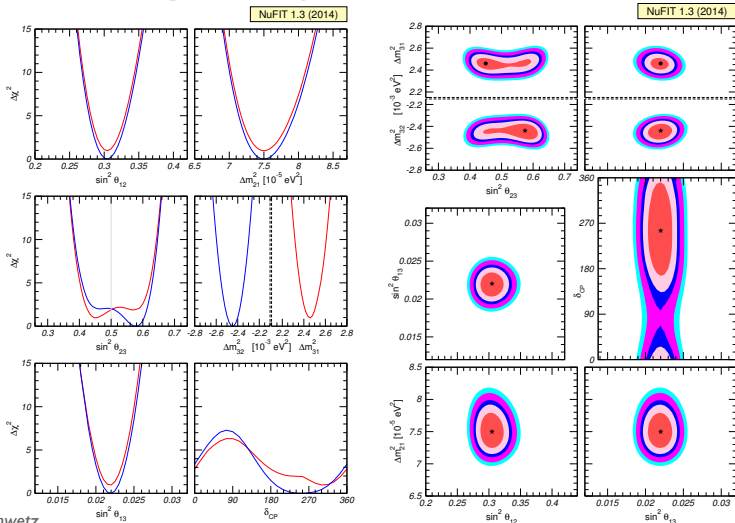


6 oscillation parameters:
 3 mixing angles,
 1 complex phase,
 2 mass-squared differences

Experiment	Dominant	Important
Solar Experiments	θ_{12}	$\Delta m_{21}^2, \theta_{13}$
Reactor LBL (KamLAND)	Δm_{21}^2	θ_{12}, θ_{13}
Reactor MBL (Daya-Bay, Reno, D-Chooz)	θ_{13}	$ \Delta m_{3\ell}^2 $
Atmospheric Experiments	θ_{23}	$ \Delta m_{3\ell}^2 , \theta_{13}, \delta$
Accelerator LBL ν_μ Disapp (Minos, T2K)	$ \Delta m_{3\ell}^2 , \theta_{23}$	
Accelerator LBL ν_e App (Minos, T2K)	δ	$\theta_{13}, \theta_{23}, \text{sign}(\Delta m_{3\ell}^2)$

Table 1. Experiments contributing to the present determination of the oscillation parameters.
 T. Schwetz

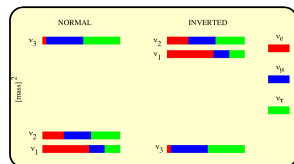
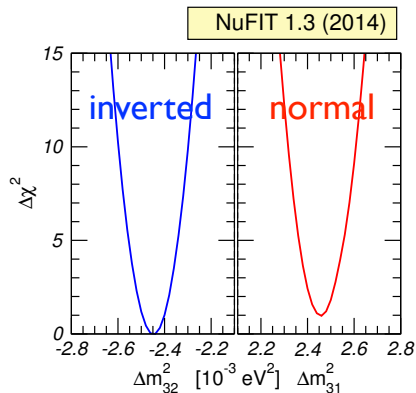
3-flavour global fit to oscillation data



T. Schwetz

see also: { Capozzi, Lisi, Marrone, Montanino, Palazzo, arXiv:1601.07777
 Forero, Tortola, Valle, PRD 90 (2014) 093006, arXiv:1405.7540

Neutrino mass ordering



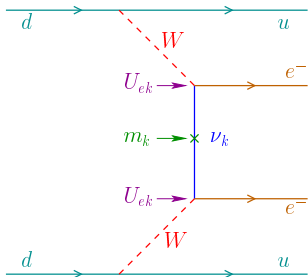
almost complete degeneracy in present data

Neutrinoless Double-Beta Decay

$$\mathcal{N}(A, Z) \rightarrow \mathcal{N}(A, Z + 2) + e^- + e^-$$

$$(T_{1/2}^{0\nu})^{-1} = G_{0\nu} |\mathcal{M}_{0\nu}|^2 |m_{\beta\beta}|^2$$

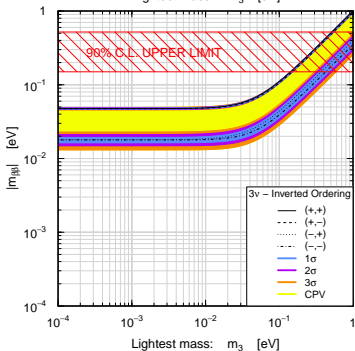
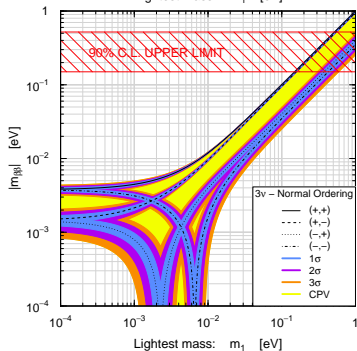
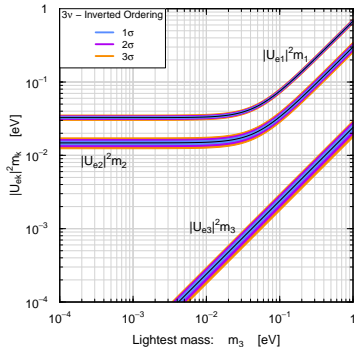
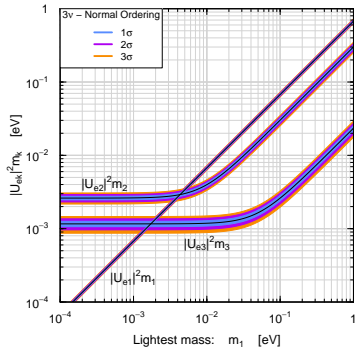
$$|m_{\beta\beta}| = \left| \sum_k U_{ek}^2 m_k \right|$$



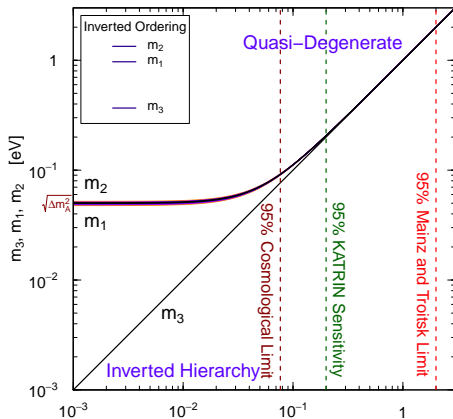
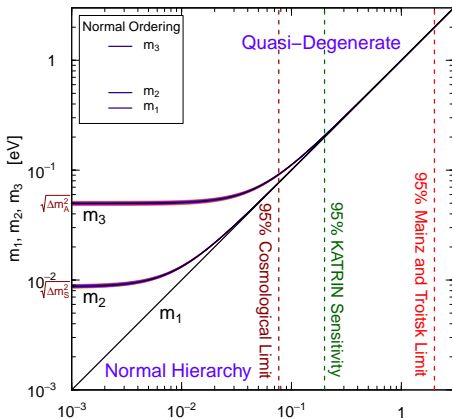
$$\Delta L = 2$$

Effective Majorana Neutrino Mass

$$m_{\beta\beta} = |U_{e1}|^2 m_1 + |U_{e2}|^2 e^{i\alpha_2} m_2 + |U_{e3}|^2 e^{i\alpha_3} m_3$$



Neutrino Masses



$$m_2^2 = m_1^2 + \Delta m_{21}^2 = m_1^2 + \Delta m_S^2$$

$$m_3^2 = m_1^2 + \Delta m_{31}^2 = m_1^2 + \Delta m_A^2$$

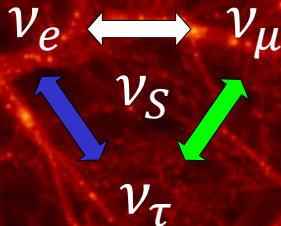
$$m_1^2 = m_3^2 - \Delta m_{31}^2 = m_3^2 + \Delta m_A^2$$

$$m_2^2 = m_1^2 + \Delta m_{21}^2 \simeq m_3^2 + \Delta m_A^2$$

Quasi-Degenerate for $m_1 \simeq m_2 \simeq m_3 \simeq m_\nu \gtrsim \sqrt{\Delta m_A^2} \simeq 5 \times 10^{-2} \text{ eV}$

95% Cosmological Limit: Planck TT + lowP + BAO [arXiv:1502.01589]

MASSIVE NEUTRINOS IN THE ERA OF PRECISION COSMOLOGY



STEEN HANNESTAD, AARHUS UNIVERSITY
ECT*, 4 APRIL 2016

- ▶ neutrinos in equilibrium in early Universe through weak interactions:

$$\nu\bar{\nu} \leftrightarrow e^+e^- \quad \bar{\nu}e \leftrightarrow \bar{\nu}e \quad \bar{\nu}N \leftrightarrow \bar{\nu}N$$

$$\nu_e n \leftrightarrow pe^- \quad \bar{\nu}_e p \leftrightarrow ne^+ \quad n \leftrightarrow pe^- \bar{\nu}_e$$

- ▶ weak interactions freeze out \implies active (ν_e, ν_μ, ν_τ) neutrino decoupling

$$\Gamma_{\text{weak}} = N\sigma v \sim G_F^2 T^5 \sim T^2/M_P \sim \sqrt{G_N T^4} \sim \sqrt{G_N \rho} \sim H$$

$$T_{\nu\text{-dec}} \sim 1 \text{ MeV}$$

$$t_{\nu\text{-dec}} \sim 1 \text{ s}$$

- ▶ relic neutrinos: $T_\nu = \left(\frac{4}{11}\right)^{\frac{1}{3}} T_\gamma \simeq 1.945 \text{ K} \implies k T_\nu \simeq 1.676 \times 10^{-4} \text{ eV}$
($T_\gamma = 2.725 \pm 0.001 \text{ K}$)

- ▶ number density: $n_f = \frac{3}{4} \frac{\zeta(3)}{\pi^2} g_f T_f^3 \implies n_{\nu_k, \bar{\nu}_k} \simeq 0.1827 T_\nu^3 \simeq 112 \text{ cm}^{-3}$

- ▶ density contribution: $\Omega_k = \frac{n_{\nu_k, \bar{\nu}_k} m_k}{\rho_c} \simeq \frac{1}{h^2} \frac{m_k}{94.1 \text{ eV}} \implies \Omega_\nu h^2 = \frac{\sum_k m_k}{94.1 \text{ eV}}$
($\rho_c = \frac{3H^2}{8\pi G_N}$)

[Gershtein, Zeldovich, JETP Lett. 4 (1966) 120; Cowsik, McClelland, PRL 29 (1972) 669]

NEUTRINO MASS AND ENERGY DENSITY FROM COSMOLOGY

NEUTRINOS AFFECT STRUCTURE FORMATION
BECAUSE THEY ARE A SOURCE OF DARK MATTER
($n \sim 100 \text{ cm}^{-3}$)

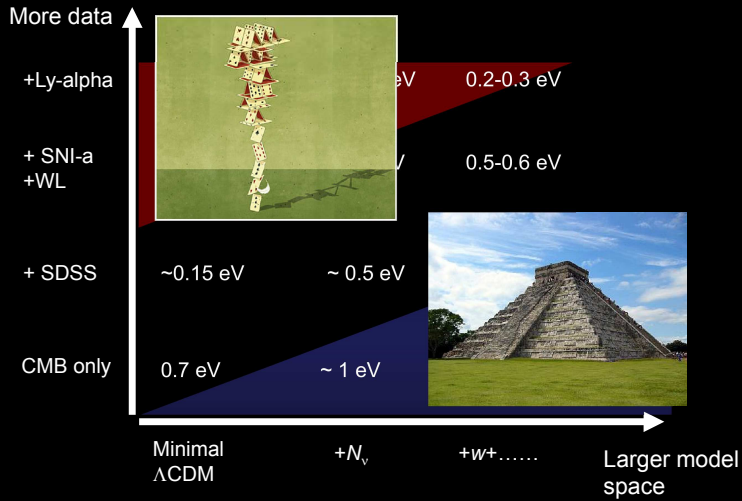
$$\Omega_\nu h^2 = \frac{\sum m_\nu}{93 \text{ eV}} \quad \text{FROM} \quad T_\nu = T_\gamma \left(\frac{4}{11} \right)^{1/3} \approx 2 \text{ K}$$

HOWEVER, eV NEUTRINOS ARE DIFFERENT FROM CDM
BECAUSE THEY FREE STREAM

$$d_{\text{FS}} \sim 1 \text{ Gpc } m_{\text{eV}}^{-1}$$

SCALES SMALLER THAN d_{FS} DAMPED AWAY, LEADS TO
SUPPRESSION OF POWER ON SMALL SCALES

THE NEUTRINO MASS FROM COSMOLOGY PLOT





Determination of neutrino mass with a sub-eV uncertainty

KATRIN - Project
Project 8

β^- -decay of Tritium



- Project

HOLMES - Project

EC in ^{163}Ho

NuMECS - Project

$Q_{Re} = 2466.7(1.5) \text{ eV}$ 😊

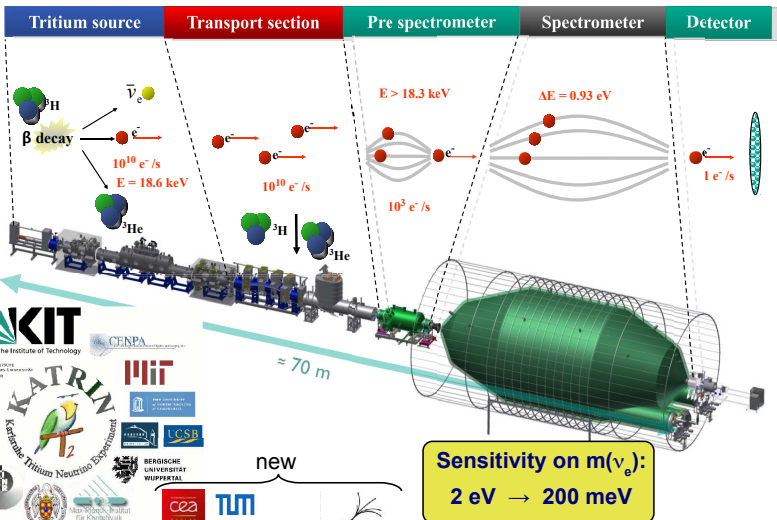
MARE- Project 😞

β^- -decay of ^{187}Re

Measurements of Q-Values are required
with a relative uncertainty $(\delta Q/m) < 10^{-11}$



The Karlsruhe Tritium Neutrino Experiment KATRIN - overview





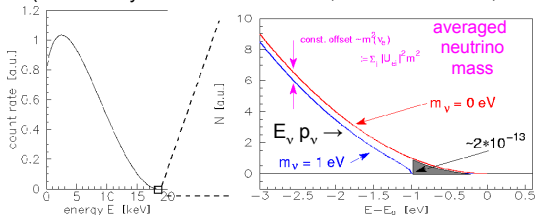
Direct determination of $m(\nu_e)$ from β decay

$$\beta: dN/dE = K F(E,Z) \underbrace{p_e}_{p_e} \underbrace{E_e}_{E_e} \underbrace{(E_0 - E_e)}_{E_\nu} \underbrace{\sum |U_{ei}|^2 \sqrt{(E_0 - E_e)^2 - m(\nu_i)^2}}_{p_\nu}$$

phase space:

with "electron neutrino mass": $m(\nu_e)^2 := \sum |U_{ei}|^2 m(\nu_i)^2$

(modified by electronic final states, recoil corrections, radiative corrections)



$m(\nu) < 2$ eV (Mainz, Troitsk)

Recent review:
G. Drexlin, V. Hannen, S. Mertens,
C. Weinheimer, *Adv. High Energy
Phys.*, 2013 (2013) 293986

Need: low endpoint energy \Rightarrow Tritium ${}^3\text{H}$ (${}^{187}\text{Re}$, ${}^{163}\text{Ho}$)
 very high energy resolution &
 very high luminosity &
 very low background \Rightarrow MAC-E-Filter
 (or bolometer for ${}^{187}\text{Re}$, ${}^{163}\text{Ho}$)

Summary: β -spectrum incl. electronic final states + ν mixing

Including electronic excited final states of excitation energy V_j with probability W_j

$$W_j = |\langle \Psi_0 | \Psi_{fj} \rangle|^2$$

$$\text{Using } \varepsilon_j = E_0 - V_j - E$$

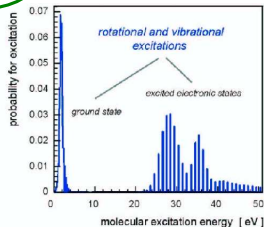
$$\frac{d^2 N}{dt dE} = A \cdot F(E, Z+1) \cdot p \cdot (E+m) \cdot \sum_j W_j \cdot \varepsilon_j \cdot \sqrt{\varepsilon_j^2 - m^2(\nu_c)} \cdot \Theta(\varepsilon_j - m(\nu_c))$$

Final states of T_2 β -decay:

(A. Saenz et al. Phys. Rev. Lett. 84 (2000) 242,
N. Doss et al., Phys. Rev. C73 (2006) 025502)

⇒ **electronic final states
are very important**

⇒ **look at
endpoint region**



Including neutrino mixing

$$\frac{d^2 N}{dt dE} = A \cdot F(E, Z+1) \cdot p \cdot (E+m) \cdot \sum_j W_j \cdot \varepsilon_j \cdot \left(\sum_i |U_{ci}|^2 \sqrt{\varepsilon_j^2 - m^2(\nu_i)} \cdot \Theta(\varepsilon_j - m(\nu_i)) \right)$$

⇒ "Electron neutrino mass"

$$m^2(\nu_c) := \sum_i |U_{ci}|^2 \cdot m^2(\nu_i)$$

⇒ **the different $m(\nu_i)$
are not important
at present precision**

NEW TESTS FOR AND BOUNDS ON NEUTRINO MASSES AND LEPTON MIXING

R.E. SHROCK

*Institute for Theoretical Physics, State University of New York at Stony Brook,
Stony Brook, NY 11794, USA*

Received 5 May 1980

We propose a new class of correlated tests for neutrino masses and lepton mixing. Two particular tests based on $(\pi, K)_{\ell 2}$ decay and nuclear β decay are discussed and applied to present data to derive bounds on these quantities.

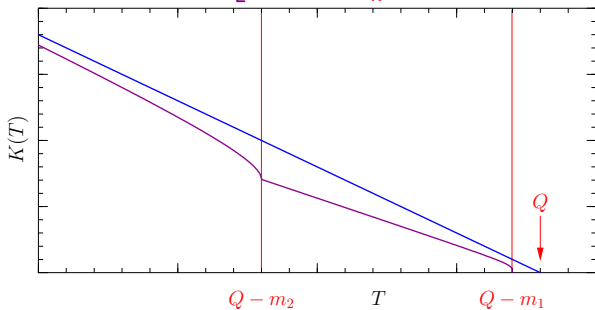
$\rightarrow (E_e)_{\max}$. An analysis of the decay ${}^3\text{H} \rightarrow {}^3\text{He} + e^- + \bar{\nu}_e$ yielded the best upper limit quoted as “ $m(\nu_e)$ ” < 35 eV (90% CL) [10]. The precise meaning is that $m(\nu_i) < 35$ eV for all LDC modes i occurring in this β decay. In fact, however, previous discussions do not seem to have recognized that, as a corollary of our beginning observation, the early falloff near $(E_e)_{\max}$ in a Kurie plot is not the only signature of massive neutrinos. Rather, a Kurie plot would in general consist of k' components due to the separate decays $(Z_1, A_1) \rightarrow (Z_1 \pm 1, A_1) + e^\pm + (\bar{\nu})_e$. Of these, a subset $i \in \{i_L\}$

every β decay can be used. The characteristic signature of the i th HSC mode is a kink in the Kurie plot at its endpoint energy

$$(E_e^{(i)})_{\max} = \{M_1^2 + m_e^2 - [M_2 + m(\nu_i)]^2\} / (2M_1),$$

where $M_{1,2}$ are the initial and final nuclear masses, together with the small incremental addition which it contributes for $E_e < (E_e^{(i)})_{\max}$. From the position of the i th kink one can determine $m(\nu_i)$. Next, one can deter-

$$\text{Neutrino Mixing} \Rightarrow K(T) = \left[(Q - T) \sum_k |U_{ek}|^2 \sqrt{(Q - T)^2 - m_k^2} \right]^{1/2}$$



Eventually it may be possible to

- ▶ determine the individual masses m_1, m_2, m_3 ;
- ▶ determine the mixings $|U_{e1}|^2, |U_{e2}|^2, |U_{e3}|^2$;
- ▶ check the unitarity relation $\sum_{k=1}^3 |U_{ek}|^2 = 1$.

Energy resolution $\Delta E \gtrsim 1 \text{ eV} \gg m_1, m_2, m_3 \implies Q - T \gg m_1, m_2, m_3$

$$\begin{aligned} K^2 &= (Q - T) \sum_{k=1}^3 |U_{ek}|^2 \sqrt{(Q - T)^2 - m_k^2} \\ &= (Q - T)^2 \sum_{k=1}^3 |U_{ek}|^2 \sqrt{1 - \frac{m_k^2}{(Q - T)^2}} \\ &\simeq (Q - T)^2 \sum_{k=1}^3 |U_{ek}|^2 \left[1 - \frac{1}{2} \frac{m_k^2}{(Q - T)^2} \right] \\ &= (Q - T)^2 \left[1 - \frac{1}{2} \frac{m_\beta^2}{(Q - T)^2} \right] \\ &\simeq (Q - T) \sqrt{(Q - T)^2 - m_\beta^2} \end{aligned}$$

EFFECTIVE MASS:

$$m_\beta^2 = \sum_{k=1}^3 |U_{ek}|^2 m_k^2$$

What happens if $\Delta E \approx m_1 \simeq m_2 \simeq m_3$ (quasi-degenerate)?

$$m_k^2 = m_1^2 + m_k^2 - m_1^2 = m_1^2 + \Delta m_{k1}^2$$

$$K^2 = (Q - T) \sum_{k=1}^3 |U_{ek}|^2 \sqrt{(Q - T)^2 - m_1^2 + \Delta m_{k1}^2}$$

$(Q - T)^2 - m_1^2 \gg \Delta m_{k1}^2 \implies$ first order mass effect:

$$K^2 \simeq (Q - T) \underbrace{\sum_{k=1}^3 |U_{ek}|^2}_1 \sqrt{(Q - T)^2 - m_1^2}$$

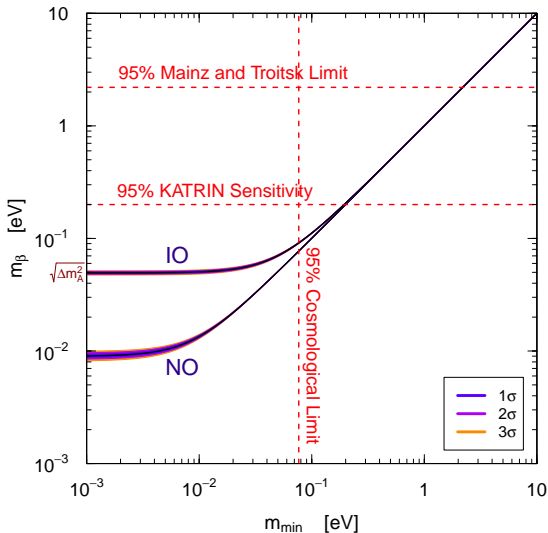
$$\simeq (Q - T) \sqrt{(Q - T)^2 - m_1^2}$$

$$m_\beta^2 = \sum_{k=1}^3 |U_{ek}|^2 m_k^2 \simeq \underbrace{\sum_{k=1}^3 |U_{ek}|^2}_1 m_1^2 = m_1^2$$

the effective mass is valid down to an energy resolution $\Delta E \approx 0.1 \text{ eV}$
where the masses are quasi-degenerate

Effective Neutrino Mass

$$m_\beta^2 = |U_{e1}|^2 m_1^2 + |U_{e2}|^2 m_2^2 + |U_{e3}|^2 m_3^2$$



- ▶ Quasi-Degenerate:

$$m_\beta^2 \simeq m_\nu^2 \sum_{k=1}^3 |U_{ek}|^2 = m_\nu^2$$

- ▶ Inverted Hierarchy:

$$m_\beta^2 \simeq (1 - s_{13}^2) \Delta m_A^2 \simeq \Delta m_A^2$$

- ▶ Normal Hierarchy:

$$m_\beta^2 \simeq s_{12}^2 c_{13}^2 \Delta m_S^2 + s_{13}^2 \Delta m_A^2 \\ \simeq 2 \times 10^{-5} + 6 \times 10^{-5} \text{ eV}^2$$

- ▶ $m_\beta \lesssim 4 \times 10^{-2} \text{ eV}$



Normal Spectrum

Project 8

Coherent radiation emitted can be collected and used to measure the energy of the electron in non-destructively.

PROJECT 8

Frequency Approach



I. I. Rabi

"Never measure anything but frequency."

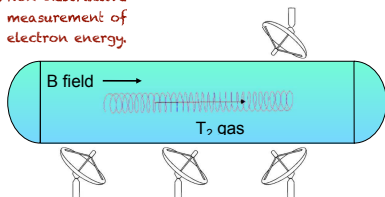


A. L. Schawlow

- Use cyclotron frequency to extract electron energy.

$$\omega(\gamma) = \frac{\omega_0}{\gamma} = \frac{eB}{K + m_e}$$

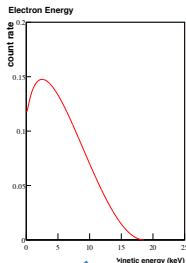
- Non-destructive measurement of electron energy.



B. Monreal and JAF, Phys. Rev D80:051301

Unique Advantages

- **Source = Detector**
(no need to separate the electrons from the tritium)
- **Frequency Measurement**
(can pin electron energies to well-known frequency standards)
- **Full Spectrum Sampling**
(full differential spectrum measured at once, large leverage for stability and statistics)

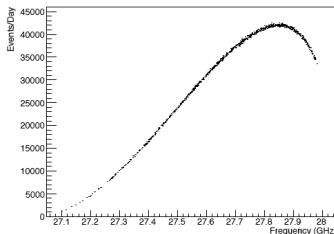


Beta spectrum



Cyclotron Frequency

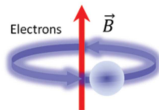
$$\omega(\gamma) = \frac{\omega_0}{\gamma} = \frac{eB}{K + m_e}$$



Beta (frequency) spectrum

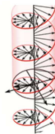
...and Challenges

- Power Emitted**
 Less than 1 fW of power radiated (depends on antenna geometry) is challenging.
- Confinement Period**
 One needs time to make sufficiently accurate measurement ($> 10 \mu\text{s}$).
 Employ magnetic bottle for trapping.
- Full Spectrum**
 The full spectrum is available.
 Fortunately, linearity of frequency space helps separate regions of interest.



$$\omega(\gamma) = \frac{\omega_0}{\gamma} = \frac{eB}{K + m_e}$$

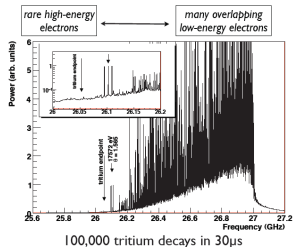
Relativistic cyclotron frequency



$$P_{\text{tot}}(\beta_{\parallel}, \beta) = \frac{1}{4\pi\epsilon_0} \frac{2e^2\omega_0^2}{3c} \frac{\beta_{\parallel}^2}{1 - \beta^2}$$

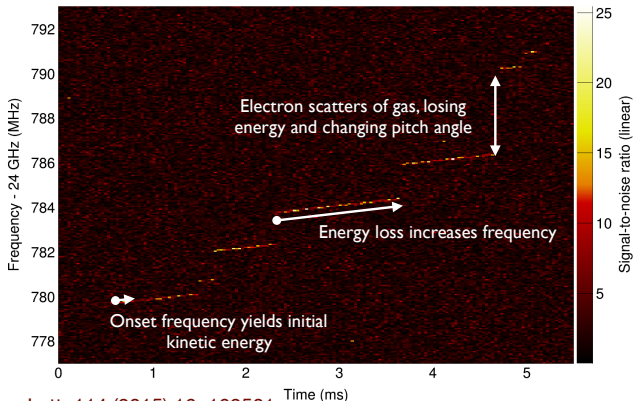
(Free) Radiative Power Emitted

Simulation of electron motion in magnetic bottle



Simulation of beta (frequency) spectrum

Project 8's "Event Zero"



Phys. Rev. Lett. 114 (2015) 16, 162501

Exhibits all predicted characteristics:

- Onset frequency
- Energy loss due to cyclotron radiation
- Quantum jumps due to inelastic scattering

A Phased Approach

Given the novelty of the project, we are pursuing a phased approach toward neutrino mass measurements:

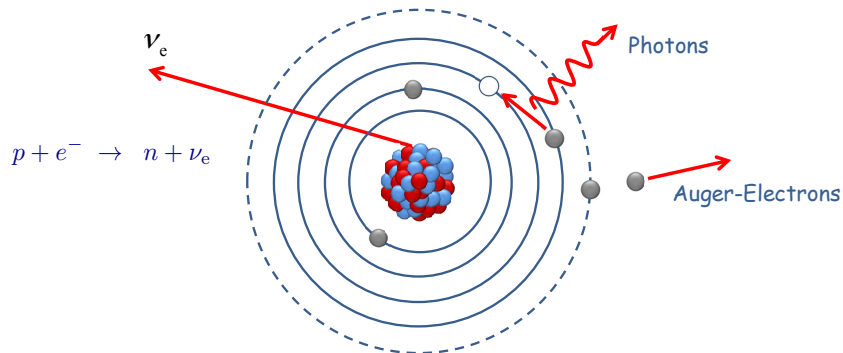
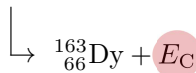
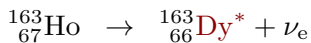
	Timeline	Scientific Goal	Source	R&D Milestone
Phase I	2010-2014	Proof of principle; Kr spectrum	^{83m}Kr	Single electron detection COMPLETED!
Phase II	2015-2017	T-He mass difference	T_2	Tritium spectrum; calibration and error studies
Phase III	2016-2020	2 eV scale	T_2	
Phase IV	2018+	0.04 eV scale	T	High rate sensitivity

We have completed Phase I, we are preparing for Phase II

Electron Capture: ^{163}Ho

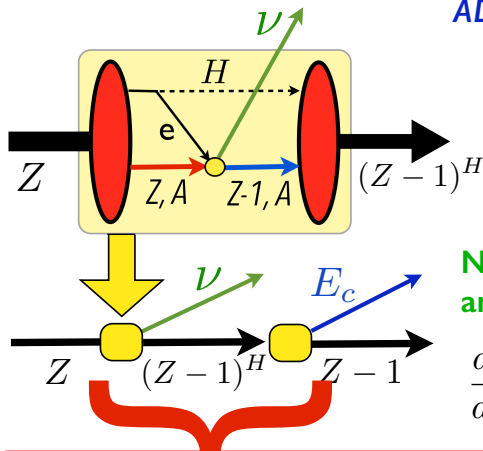
EChO

A. De Rujula, M. Lusignoli,
Phys. Lett. B **118** (1982) 429



“Effective” calorimetric theory,

ADR & Lusignoli (1982)



$$Q = M[\text{det.,before}] - M[\text{det.,after}]$$

(Chem. pure detector)

$$Q = E_\nu + E_c$$

No matter what H was and how it de-excited !

$$\frac{dW}{dE_c} = - \frac{dW}{dE_\nu} \Big|_{E_\nu = Q - E_c}$$

$$\frac{dW}{dE_c} \propto \frac{(Q - E_c)}{E_\nu} \sqrt{(Q - E_c)^2 - m_\nu^2} \sum_H \frac{\varphi_H^2(0) \Gamma_H}{(E_c - E_H)^2 + \Gamma_H^2/4}$$

For Electron Capture (in Holmium 163):

1) Electron at nucleus \rightarrow $s_{1/2}$ and $p_{1/2}$

2) Electron binding energy $<$ Q-value \approx 2.8 [keV]

$$E(1s_{1/2}, K, \text{Ho}) = 55.6 \text{ keV}$$

$$E(2s_{1/2}, L1, \text{Ho}) = 9.4 \text{ keV}$$

$$E(2p_{1/2}, L2, \text{Ho}) = 8.9 \text{ keV}$$

$$E(2p_{3/2}, L3, \text{Ho}) = 8.1 \text{ keV}$$

$$E(3s_{1/2}, M1, \text{Ho}) = 2.0 \text{ keV}$$

$$E(3p_{1/2}, M2, \text{Ho}) = 1.8 \text{ keV}$$

$$E(4s_{1/2}, N1, \text{Ho}) = 0.4 \text{ keV}$$

$$E(4p_{1/2}, N2, \text{Ho}) = 0.3 \text{ keV}$$

$$E(5s_{1/2}, O1, \text{Ho}) = 0.05 \text{ keV}$$

Deexcitation Spectrum (X-rays, Auger- electrons by a Calorimeter) of excited Dy^* (Atom)

$$\frac{d\Gamma}{dE_c} \propto (Q-E_c) \sqrt{(Q-E_c)^2 - m_\nu^2} \sum_{ff'} \lambda_0 B_{ff'} \frac{\Gamma_{f'}}{2\pi} \frac{1}{(E_c - E_{f'})^2 + \Gamma_{f'}/4}$$

$$B_{f,f'} \approx |\langle \text{Dy}^*_{f'} | \mathbf{a}_f | \mathbf{G} \rangle|^2 |\psi_f(\mathbf{R})|^2 / |\psi_{3s1/2}(\mathbf{R})|^2$$

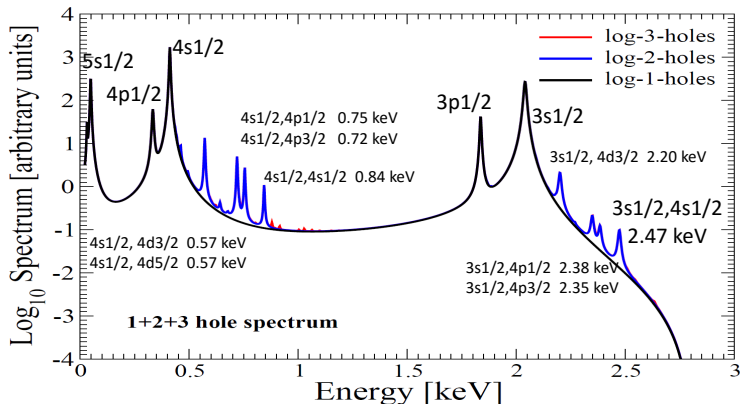
$$\psi_A(r) = \frac{1}{r} \begin{pmatrix} P_A \\ Q_A \end{pmatrix}$$

$$\lambda_0 \propto \mathbf{G}_{\text{weak}}^2 \xi$$

$$\langle A|B' \rangle = \int_{0,\infty} (P_A(r) \cdot P_{B'}(r) + Q_A(r) \cdot Q_{B'}(r)) \cdot dr = \text{overlap}(A, B')$$

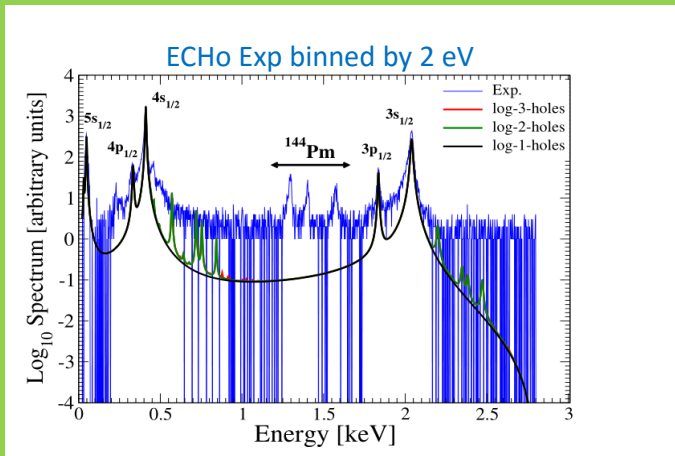
Amand Faessler, University of Tuebingen

One-, two- and three-hole state deexcitation in Dy*



Comparison
with the
EChO data.

Background
must be
included into
theoretical
treatment.



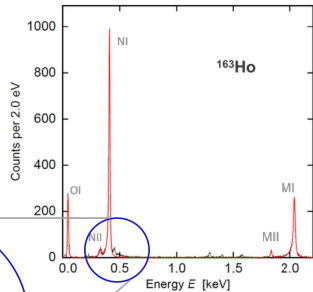
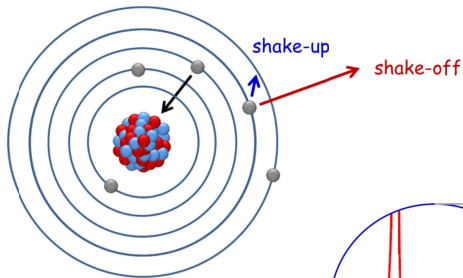
Amand Faessler, University of Tuebingen

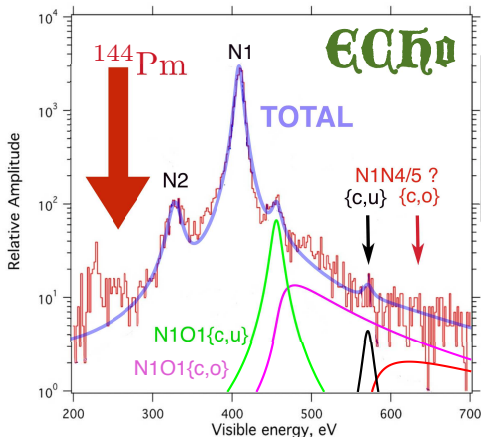
Spectral Shape: Higher Order Processes

EChO

R.G.H. Robertson, *Phys. Rev. C* **91**, 035504 (2015)
 A. Faessler, *et al.*, *J. Phys. G* **42**, 015108 (2015)
 A. Faessler, *et al.*, *Phys. Rev. C* **91**, 045505 (2015)
 A. Faessler, *et al.*, *Phys. Rev. C* **91**, 064302 (2015)
 A. De Rujula, *et al.*, arXiv:1601.04990v1 [hep-ph]

two-hole processes





Maurizio Lusignoli + ADR
 (à la 1967 Intemann & Pollock)

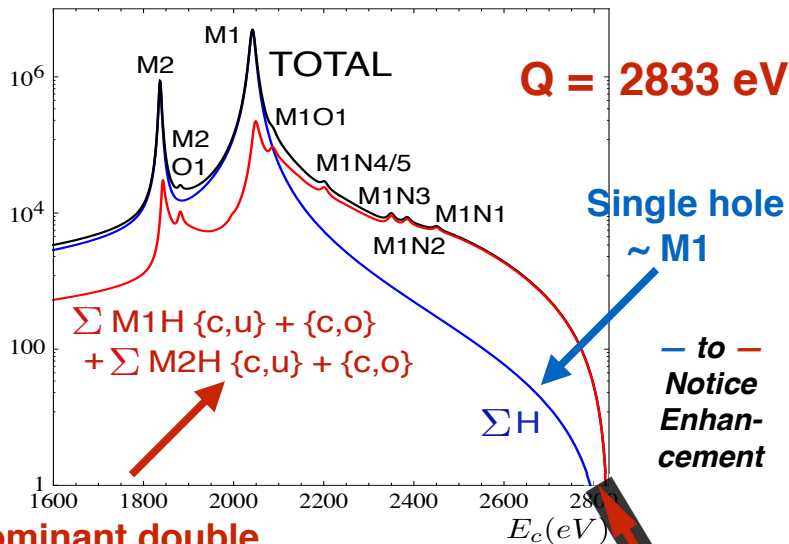
{ , }

$\mathcal{O}(2)$ Massage

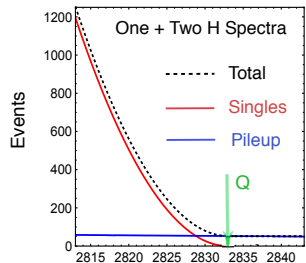
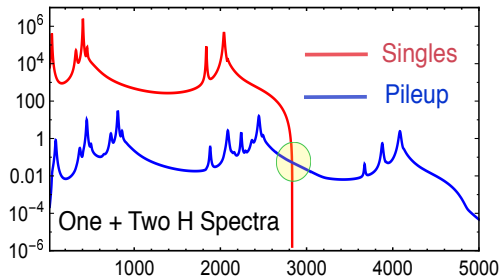
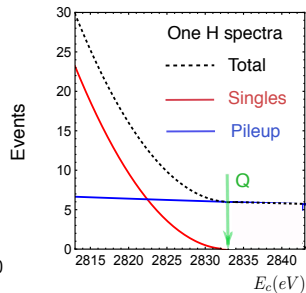
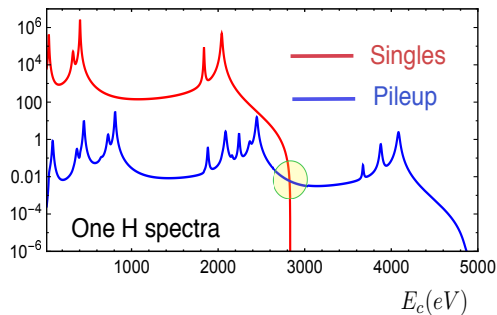
$\{c,u\}$ 1 e captured; 1 e up to unoccupied level

$\{c,o\}$ 1 e captured; 1 e off to the continuum

 **Electron ShakeOff previously FORGOTTEN!!**



$$E_\nu p_\nu = (Q - E_c) \sqrt{(Q - E_c)^2 - m_\nu^2}$$



x ~ 6 IMPROVEMENT

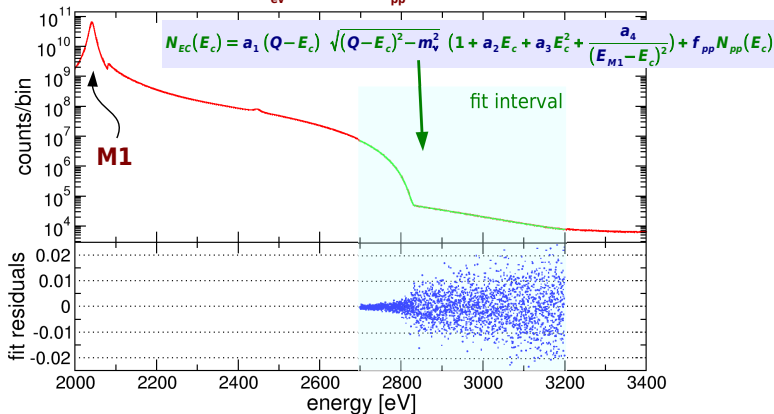
- ▶ Different theoretical opinions about the size of the shake-off effect.
- ▶ We all hope that it is as large as calculated by Alvaro and Maurizio.
- ▶ Plausible statement by Alvaro (as I remember): theoretical calculations are important for the development of the experiments, but will not be crucial for the mass measurements.
- ▶ This is because the spectrum near the end point can be fitted by the sum of a smooth function and a Breit-Wigner tail.

Statistical sensitivity: shake-off processes



MC simulation with the *optimistic* spectrum in arXiv:1601.04990

$$Q = 2833 \text{ eV}, N_{\text{ev}} = 3 \times 10^{13}, f_{\text{pp}} = 3.0 \times 10^{-4}, \Delta E = 1.0 \text{ eV}$$



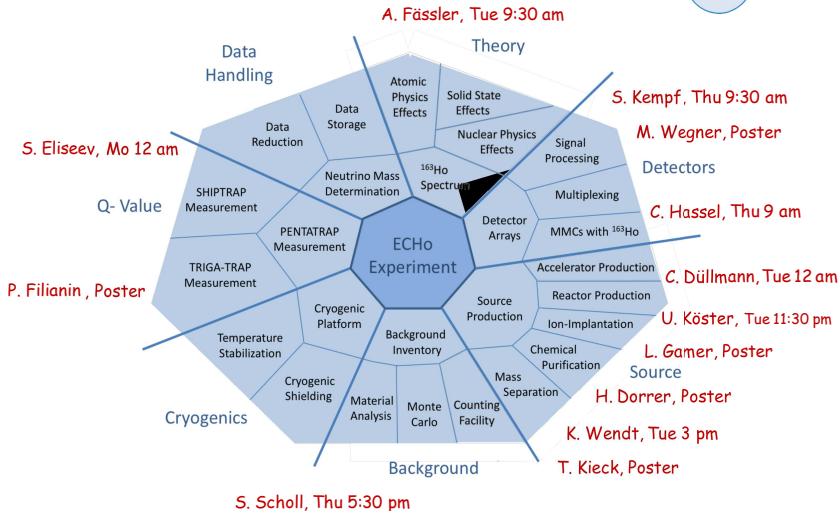
statistical sensitivity $\Sigma(m_\nu) \approx 0.64 \pm 0.03 \text{ eV}$

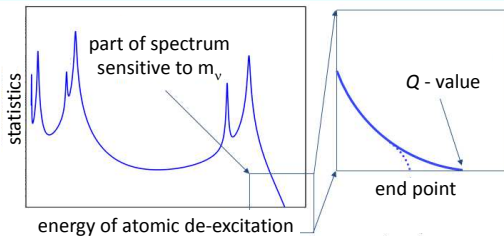
A. Nucciotti, ECT*, Trento (Italy), April 4th-8th, 2016

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improvement by a factor $\approx 40^{1/4} \simeq 2.5$

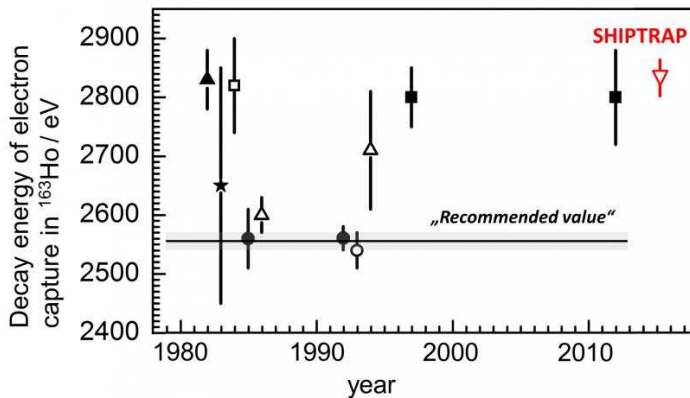
Overview ECHo





2

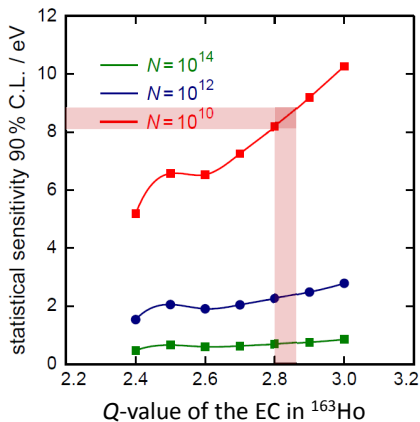
2
4
 $Q_{\text{microcalorimetry}}$
 $\Delta Q (\delta Q \sim 1\text{eV})$
 $Q_{\text{Penning trap}}$
 $\delta m_\nu^{\text{sys}}$



$$Q_{Ho} = 2833(30_{\text{stat}})(15_{\text{sys}}) \text{ eV}$$

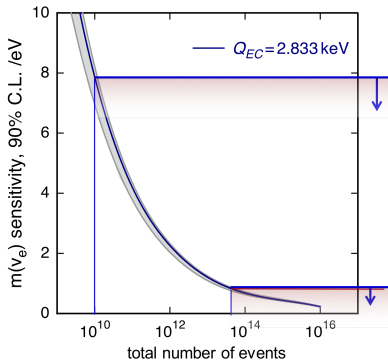


statistical sensitivity to neutrino mass



Expected Sensitivity for $\Delta E_{\text{FWHM}} = 3 \text{ eV}$ and $f_{\text{pu}} = 10^{-5}$

EChO



EChO-1k

2 x 50 pixel x 10 Bq

4 months $\rightarrow 10^{10}$ events

sub 10 eV resolution

EChO-1M

50 x 2000 pixel x 10 Bq

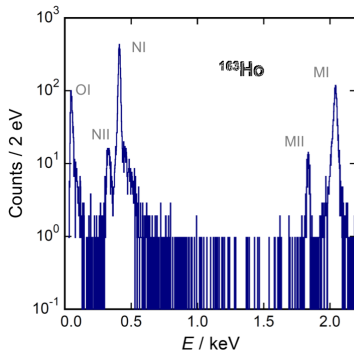
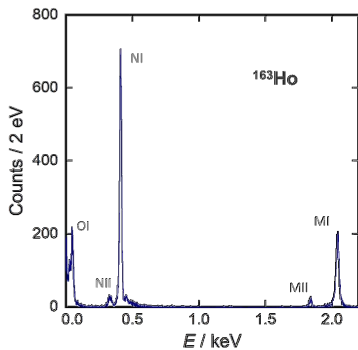
24 months $\rightarrow 6 \times 10^{13}$ events

sub 1 eV resolution

Latest Results: **First Spectrum**

EChO

1 pixel about 2 days

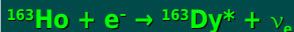


activity per pixel $A \sim 0.2$ Bq
 energy resolution $\Delta E_{FWHM} \sim 5$ eV

→ no evidence of radioactive contamination
 in the source



Electron capture end-point experiment / 1

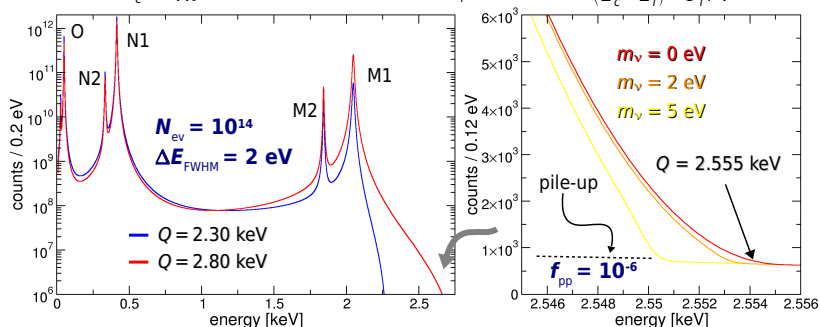


electron capture from shell $\geq M1$

A. De Rújula and M. Lusignoli, Phys. Lett. B 118 (1982) 429

- calorimetric measurement of Dy atomic de-excitations (mostly non-radiative)
- $Q = 2.8 \text{ keV}$ (recent measurement with Penning trap)
 - ▶ rate at end-point and ν mass sensitivity depend on $Q = E_{M1}$
- $\tau_{\nu} \approx 4570 \text{ years}$ \rightarrow few active nuclei are needed (2×10^{11} ^{163}Ho nuclei \leftrightarrow 1Bq)

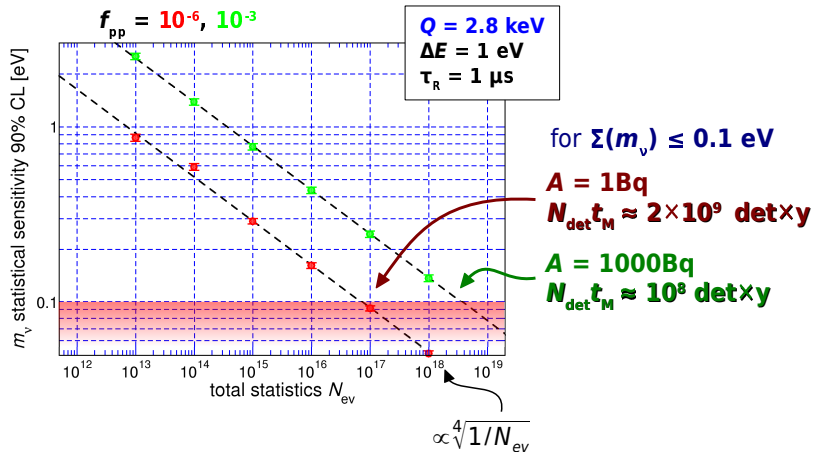
$$\frac{d\lambda_{EC}}{dE_c} = \frac{G_\beta^2}{4\pi^2} (Q - E_c) \sqrt{(Q - E_c)^2 - m_\nu^2} \times \sum_i n_i C_i \beta_i^2 B_i \frac{\Gamma_i}{2\pi} \frac{1}{(E_c - E_i)^2 + \Gamma_i^2/4}$$



A. Nucciotti, ECT*, Trento (Italy), April 4th-8th, 2016

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Statistical sensitivity: Montecarlo simulations



M. Galeazzi et al., arXiv:1202.4763v2

A. Nucciotti, Eur. Phys. J. C (2014) 74:3161

A. Nucciotti, ECT*, Trento (Italy), April 4th-8th, 2016

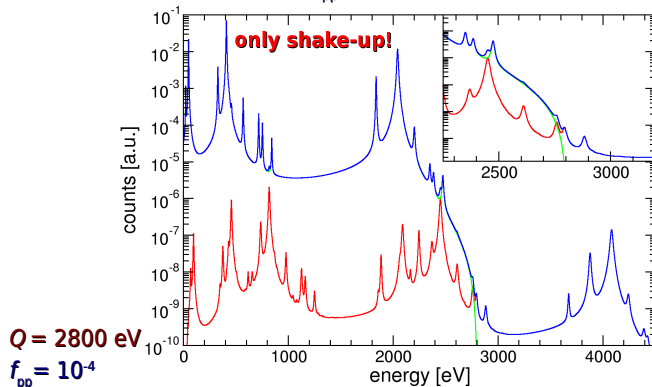
7



Electron capture end-point experiment / 3

- shake-up/shake-off → double hole excitations
 - ▶ n -hole excitations possible but less probable
 - ▶ authors do not fully agree on energies and probabilities
- even more complex pile-up spectrum
 - ▶ it may be worth keeping f_{pp} smaller than 10^{-4}

A.De Rújula, arXiv:1305.4857
 R.G.H.Robertson, arXiv:1411.2906
 A.Faessler et al., PRC 91 (2015) 45505



HOLMES (ERC-Advanced Grant n. 340321)

HOLMES

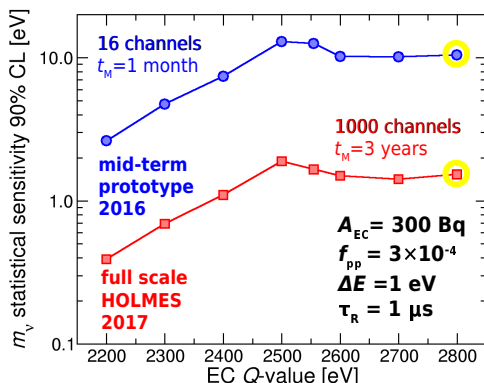


goal

- neutrino mass measurement: m_ν statistical sensitivity as low as 0.4 eV
- prove technique potential and scalability:
 - ▶ assess EC spectral shape
 - ▶ assess systematic errors

baseline

- TES with implanted ^{163}Ho
 - ▶ 6.5×10^{13} nuclei per pixel
 - 300 dec/sec
 - ▶ $\Delta E \approx 1\text{eV}$ and $\tau_R \approx 1\mu\text{s}$
- **1000 channel** array
 - ▶ 6.5×10^{16} ^{163}Ho nuclei
 - $\approx 18\mu\text{g}$
 - ▶ 3×10^{13} events in **3 years**



→ Project Started on February 1st 2014

B. Alpert et al., Eur. Phys. J. C, (2015) 75:112
<http://artico.mib.infn.it/holmes>

A. Nucciotti, ECT*, Trento (Italy), April 4th-8th, 2016

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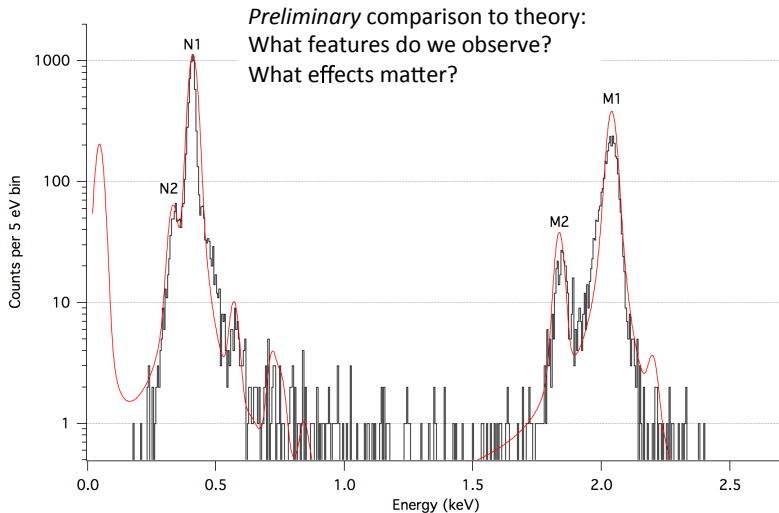
Project goals

Develop experimental methods to enable calorimetric ECS for neutrino mass measurement

- Make ^{163}Ho with high isotopic and chemical purity
- Develop optimized sensors
- Develop methods to incorporate EC-decaying isotopes into sensors
- Demonstrate high-resolution ECS at single-pixel scale

Different methods by independent groups → good science!

- Contribute data to aid theoretical understanding of EC spectra



Red line: 35 eV FWHM Gaussian convolved with calculation from *Faessler et al., Phys. Rev. C. 2015*

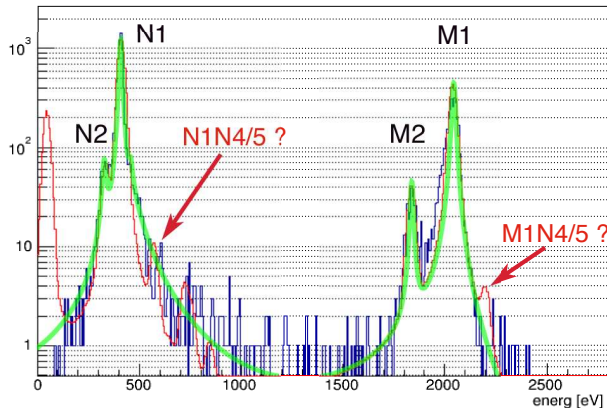
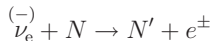


FIG. 2. Blue: the calorimetric spectrum measured by Nu-MECS [8]. Red: the theoretical prediction of Faessler et al. [13]. Green: the same description as in Fig. (1b).

Neutrino beta capture

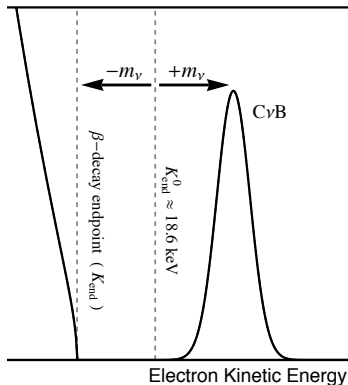
- Capture on beta-decaying nuclei



- *zero threshold*

- **excess electrons**

- $\sim 2 m_\nu$ beyond beta decay endpoint



S. Weinberg, Phys.Rev. 128 (1962) 1457–1473

Lusignoli: need to cite Irvine and Humphreys (1983)

Neutrino history: Dirac

Decoupling: $T \gg m$

Today: $T \ll m$

$$\nu_L = \nu_{hL} \quad n_\nu(z) \longrightarrow \nu_{hL} \quad n_0 \quad L = 1 \quad \text{Detected!}$$

$$\nu_R = \nu_{hR} \quad 0$$

$$\bar{\nu}_L = \bar{\nu}_{hL} \quad 0$$

$$\bar{\nu}_R = \bar{\nu}_{hR} \quad n_\nu(z) \longrightarrow \bar{\nu}_{hR} \quad n_0 \quad L = -1$$

**Propagation:
Helicity conserved**

$$n_\nu(z) = n_0(1+z)^3.$$

$$n_0 \approx 56 \text{ cm}^{-3}$$

Duda, Gelmini, Nussinov, Phys.Rev. D64 (2001) 122001

Neutrino history: Majorana

Decoupling: $T \gg m$

Today: $T \ll m$

$$\begin{array}{lcl}
 \nu_L = \nu_{hL} & n_\nu(z) \longrightarrow & \nu_{hL} \quad n_0 \quad \cancel{L} \quad \text{Detected!} \\
 \nu_R = \nu_{hR} & n_\nu(z) \longrightarrow & \nu_{hR} \quad n_0 \quad \cancel{L} \quad \text{Detected!}
 \end{array}$$

$$N_L = N_{hL} \quad 0$$

$$N_R = N_{hR} \quad 0$$

Propagation:
Helicity conserved

Duda, Gelmini, Nussinov, Phys.Rev. D64 (2001) 122001

Macroscopic difference Dirac/Majorana!

$$\Gamma_{C\nu B} = \bar{\sigma}_0 [n(\nu_{h_R}) + n(\nu_{h_L})] N_{\text{Tri}}$$

$$\Gamma_{C\nu B}^{\text{D}} = \bar{\sigma}_0 n_0 N_{\text{Tri}} \approx 4.1 \text{ yr}^{-1}$$

$$\begin{aligned} n(\nu_{h_L}) &= n_0 \\ n(\nu_{h_R}) &= 0 \end{aligned}$$

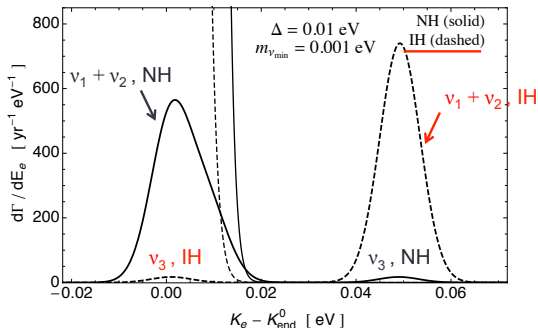
$$\Gamma_{C\nu B}^{\text{M}} = 2\bar{\sigma}_0 n_0 N_{\text{Tri}} \approx 8.1 \text{ yr}^{-1}$$

$$\begin{aligned} n(\nu_{h_L}) &= n_0 \\ n(\nu_{h_R}) &= n_0 \end{aligned}$$

(rates for 100 g of ${}^3\text{H}$)

see also Lisanti, Safdi and Tully, PRD90 (2014) no.7, 073006

- Even for optimistic Δ , ν_1 and ν_2 can not be resolved
- Inverted hierarchy more promising



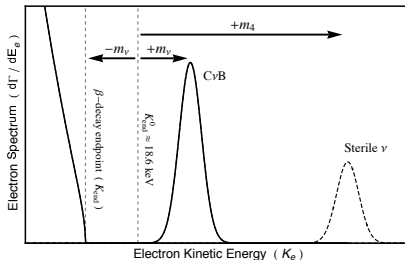
Detectable at beta capture experiment!

- Clustering compensates small mixing:

$$\frac{\Gamma_{\nu_4}}{\Gamma_{\text{C}\nu\text{B}}^{\text{M}}} \approx 0.45 \left(\frac{|U_{e4}|^2}{3 \times 10^{-2}} \right) \left(\frac{f_{\text{clus}}}{50} \right) \left(\frac{\Delta N_{\text{eff}}}{0.3} \right) \quad f_{\text{clus}} = n_s/n_0 \leq 50$$

- Background-free!**

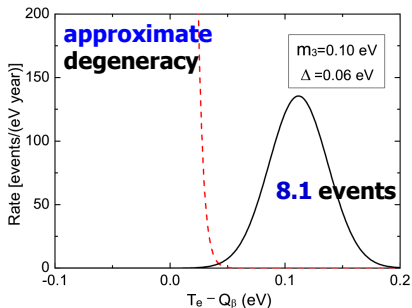
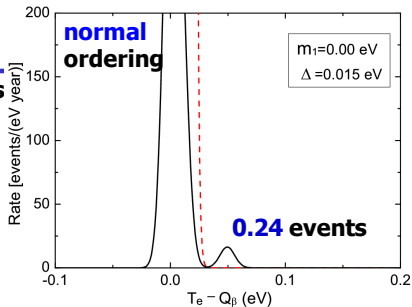
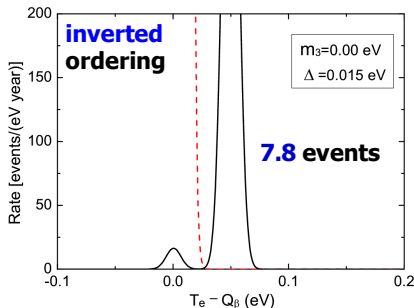
$$\Delta \ll m_4 - m_1$$



Illustration

- ◆ Target mass: **100 g** tritium atoms
- ◆ Input $\theta(13)$: 8.8 degrees
- ◆ Number of events per year: **~ 8** (Li, Xing, Luo 2011).

The gravitational clustering effect may help enhance the signal rates (Ringwald, Wong 2004).



Discovery potential of experiments

The number of signal events is given by

$$S = \frac{\lambda_{\nu(\bar{\nu})}}{\lambda_{\beta(EC)}} \frac{\log 2}{T_{1/2}} N_A n_{\text{mol}} t$$

Assume we want to record a total number of $S = 10$ signal events. We need:

- for an experiment with NCB, 135 g y of ^3H
- for an experiment with ANEC, depending on the Q-value, 23.2 (307, 1274) kg y of ^{163}Ho
- with present estimate of shake-off, 30.6 kg y

M. L., M. Vignati (2011)

New

A. De Rújula, M.L. (2016)

If the relic neutrino density is $\langle n_{\nu} \rangle$

The title 'PTOLEMY Approach' is centered in a white, sans-serif font over a horizontal banner. The banner features a colorful, abstract background of various sized spheres in shades of blue, green, orange, and red, set against a light blue sky with faint stars. On the right side of the banner, there is a small, square inset image of a man with a long white beard, wearing a yellow and orange robe, pointing upwards with his right hand. This is a traditional representation of the astronomer Ptolemy.

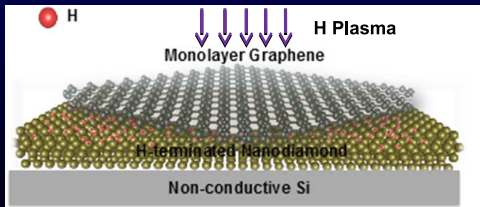
PTOLEMY Approach

- R&D program to reduce molecular smearing at the tritium source
- New geometries for TES calorimeters for 0.05-0.15 eV energy resolution at the tritium endpoint
- Design of a high mass tritium source EM geometry using a Crossed-Field MAC-E filter and time-dependent triggering with Project 8 technologies

Hydrogenation of Graphene



- ❖ Investigate the influence of different diamond platforms to support graphene
- ❖ Tune the electronic properties of CVD graphene in terms of Fang Zhao
 - Different functional terminating groups on diamond samples
 - Graphene hydrogenation process (Change the hybridization of carbon atom from sp^2 to sp^3 , thus removing the conducting π band and opening a band gap)

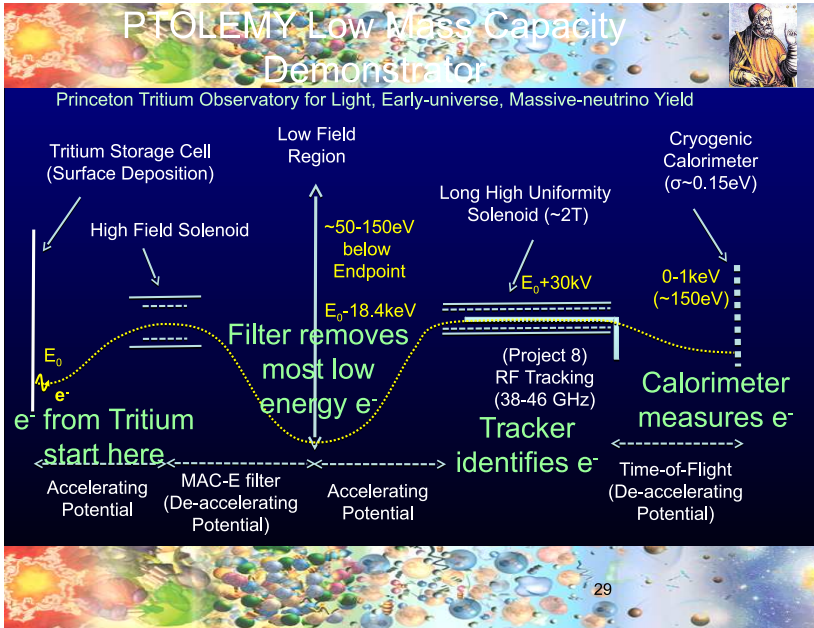


Why interesting?

C-H sp^3 bond expected to be less than 3eV

He^3 recoils into the continuum (minimal molecular broadening)

CRADA with SRNL for first tritiated-graphene sample signed by DOE and will be delivered to PPPL in March for analysis

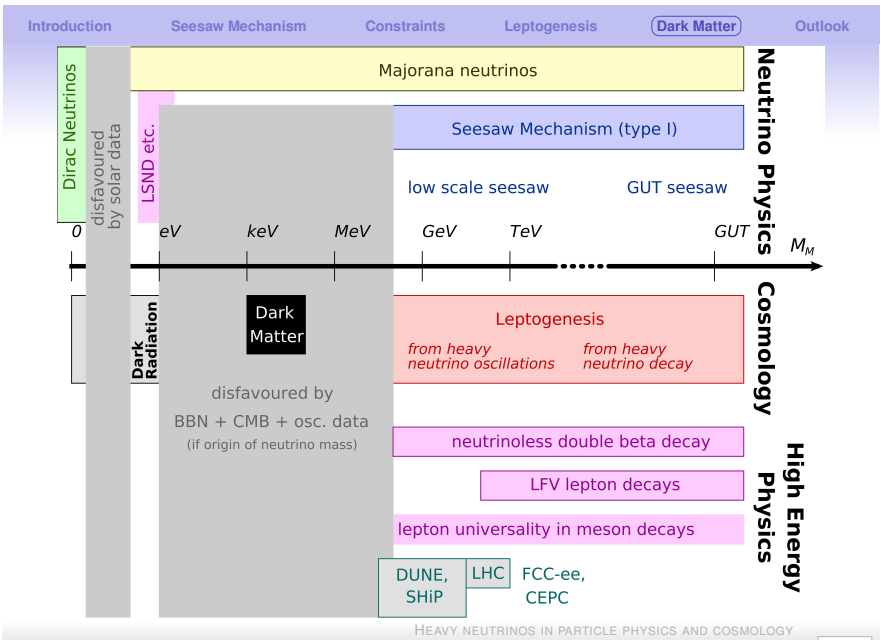


The title slide features a vibrant, abstract background of colorful spheres and particles. The text "PTOLEMY Physics" is centered in a large, white, serif font. In the top right corner, there is a small, square portrait of the astronomer Ptolemy, depicted with a beard and wearing a red and yellow robe, pointing upwards with his right hand.

PTOLEMY Physics

- R&D program may lead to advancement in the precision on the neutrino mass
 - First results expected in 2016
- Spectrum analysis can contribute to search for sterile neutrino “thresholds” down to low mixing angles
 - Initial systematics analysis included in white paper (Mertens et al.)
- Graphene-only source has unique sensitivity to MeV-scale dark matter
 - New paper in preparation
- Relic neutrino direct detection
 - Goal by 2017 : design for a 100g tritium capacity with as compact a source and filter geometry as possible from simulation

Heavy Sterile Neutrinos

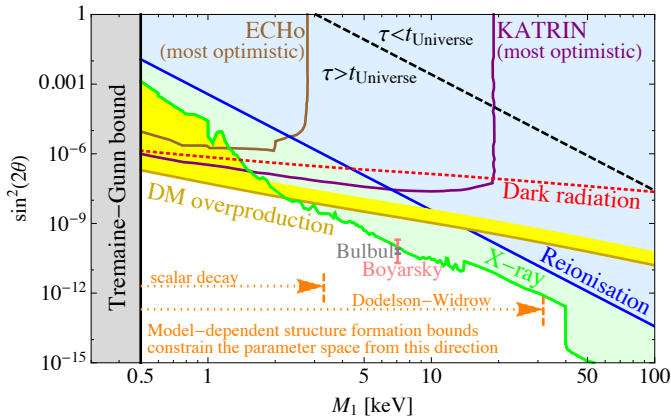


HEAVY NEUTRINOS IN PARTICLE PHYSICS AND COSMOLOGY

Production mechanisms for sterile ν Dark Matter: A Kaleidoscope of models on the market

└ Where we are and where we're heading to – Synopsis & Outlook

Synopsis of current and future bounds

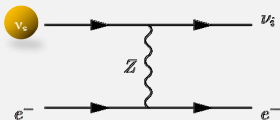


courtesy of A. Merle

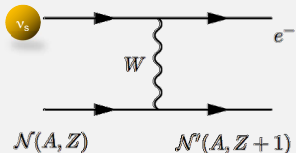
Experimental searches for ν_s -DM

Direct detection

- neutrino conversion

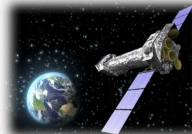


- neutrino capture



Indirect detection

XMM-Newton
Chandra
Suzaku
Astro-H
Micro-X
eRosita



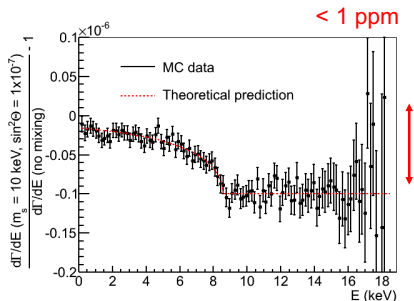
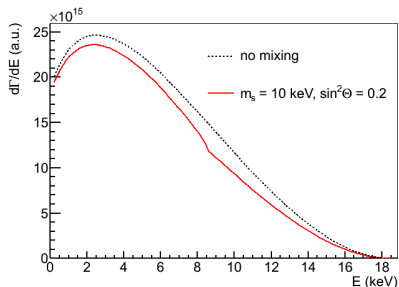
Production



KATRIN
Troitsk
ECHO
NuMecs
Holmes
Ptolemy

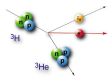


KATRIN Signature



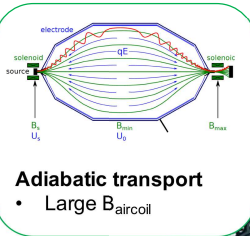
- We need large statistics
- And extremely low systematic uncertainties

Pre-Measurement



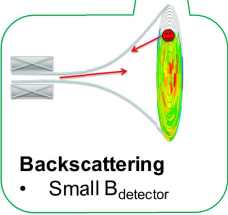
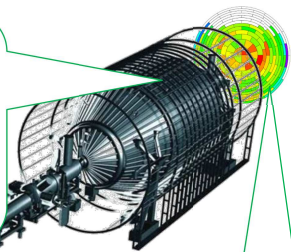
Reduce count rate

- Less T_2
- Small B_{source}

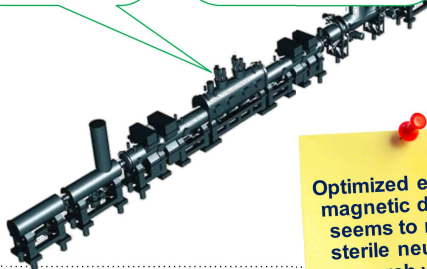


Adiabatic transport

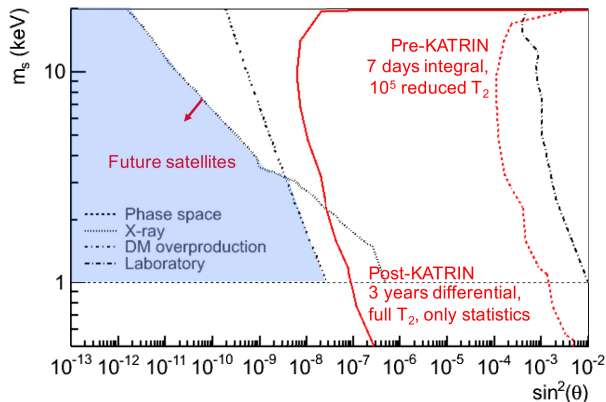
- Large $B_{aircoil}$



Optimized electro-magnetic design seems to make sterile neutrino search with KATRIN possible



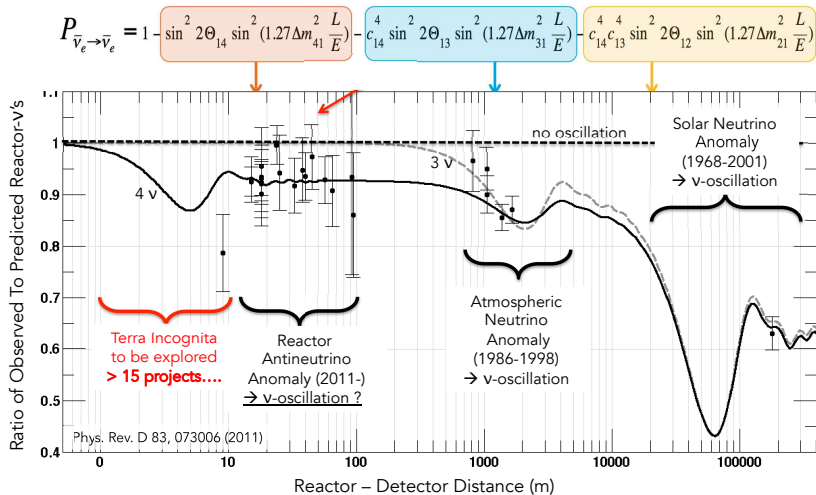
Targeted sensitivity



Light Sterile Neutrinos



The Reactor Anomaly (RAA)



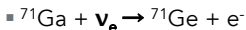
Th. Lasserre - Trento - 07/04/2016



The Gallium Anomaly (GA)



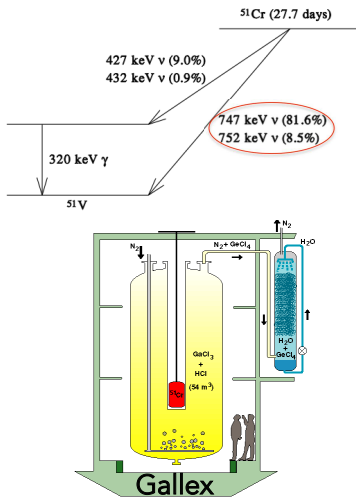
- Test of solar neutrino radiochemical detectors GALLEX and SAGE



- 4 calibration runs with 20-60 PBq Electron Capture ν_e emitters

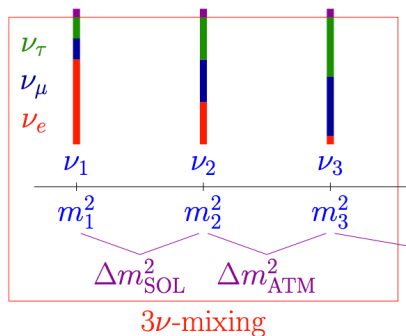
- Gallex, $\langle L \rangle = 1.9$ m
 - ${}^{51}\text{Cr}$, 750 keV
- Sage, $\langle L \rangle = 0.6$ m
 - ${}^{51}\text{Cr}$ & ${}^{37}\text{Ar}$ (810 keV)

- Deficit observed
 - 3σ anomaly

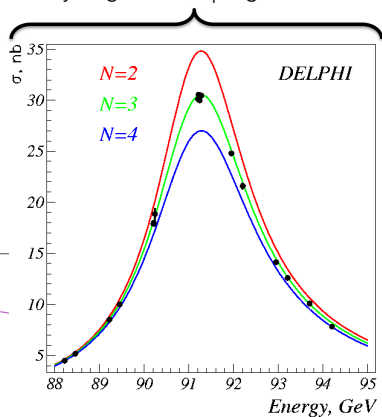




Three Active Neutrinos



Only 3 light n's coupling to Z boson



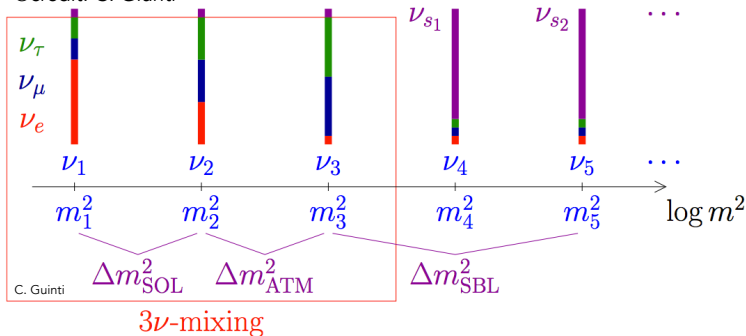


Adding Sterile Neutrinos



No SM interactions.
Mixing with active ν 's

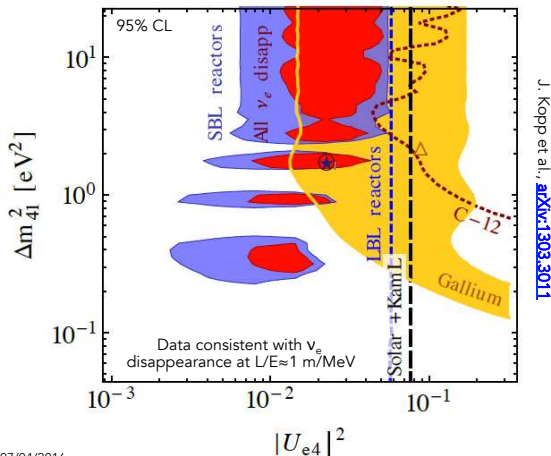
@credit: C. Giunti





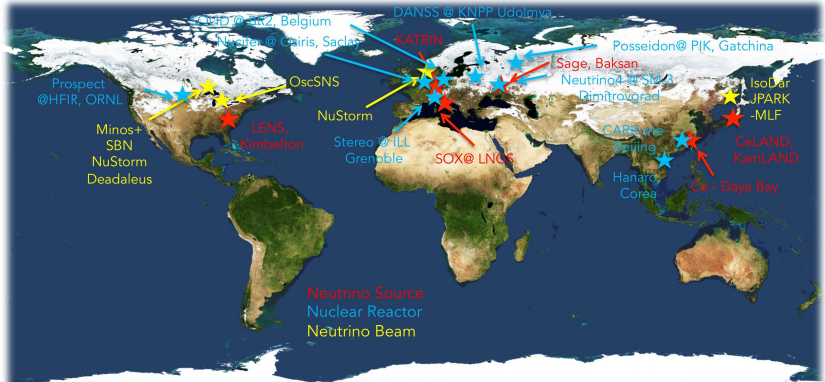
$\bar{\nu}_e$ disappearance (3+1)

$$P_{ee} = 1 - \sin^2 2\theta_{ee} \sin^2 \frac{\Delta m_{41}^2}{4E} \quad \& \quad \sin^2 2\theta_{ee} = |U_{e4}|^2 (1 - |U_{e4}|^2)$$





Searches for eV Sterile- ν



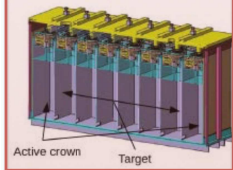
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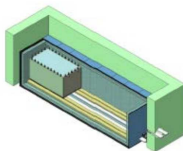
A selection of Ongoing Efforts



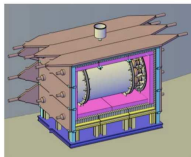
STEREO: Gd-LS detector at 10m from ILL, France



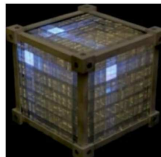
Neutrino-4: Gd-LS detector at 6-12m from SM-3, Russia



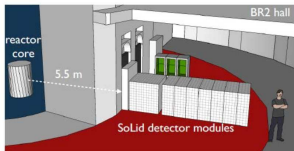
NEOS: Gd-LS detector at ~30m from Hanbit, Korea



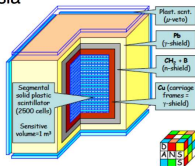
NuLAT: Li-loaded plastic scintillator cubes



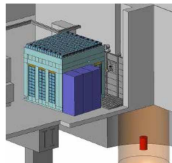
SoLid/CHANDLER: segmented composite scintillator cubes at 5.5m from BR2, Belgium



DANSS: Segmented plastic scintillator at ~10m from KNPP, Russia



PROSPECT: Segmented ⁶Li liquid scintillator at 7-12m from HFIR, US



@Credit: K. Heeger

CeSOX @ BOREXINO

Antineutrino Emitter: ^{144}Ce - ^{144}Pr

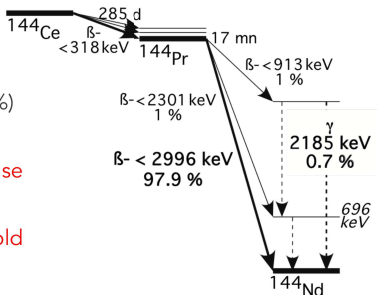
(ITEP N°90 1994, PRL 107, 201801, 2011)



- $\bar{\nu}_e$ detection: $\bar{\nu}_e + p \rightarrow e^+ + n$
 - large IBD cross section $\rightarrow 5 \text{ PBq}$
 - (e^+, n) coincidence \rightarrow mitigate backgrounds



- ^{144}Ce - ^{144}Pr
 - Abundant fission product (5%)
 - ^{144}Ce : long-lived & low- Q_β
time to produce, transport, use
 - ^{144}Pr : short-lived & high- Q_β
 $\bar{\nu}_e$ -emitter above IBD threshold



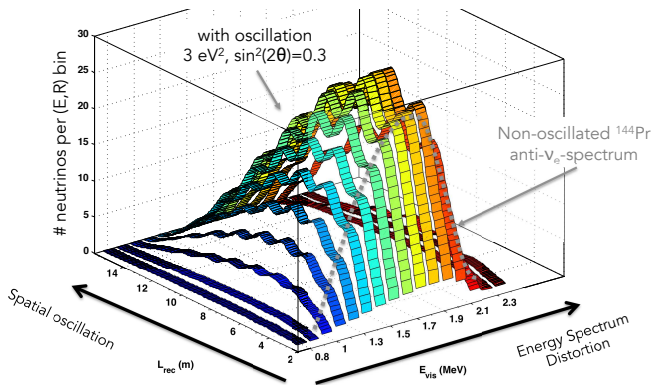
CeSOX @ BOREXINO



Expected Signal: 30/d (3.7 PBq)



$$\frac{d^5 N_{\bar{\nu}_e}}{dt dE d^3 \mathcal{V}_{\text{det}}} = \mathcal{A}_0 e^{-t \lambda_{\text{Ce}}} \eta_p \varepsilon \frac{1}{4\pi L^2} \sigma_{\text{IBD}}(E) S_{\text{Ce}}(E) \times \mathcal{P}(L, E)$$

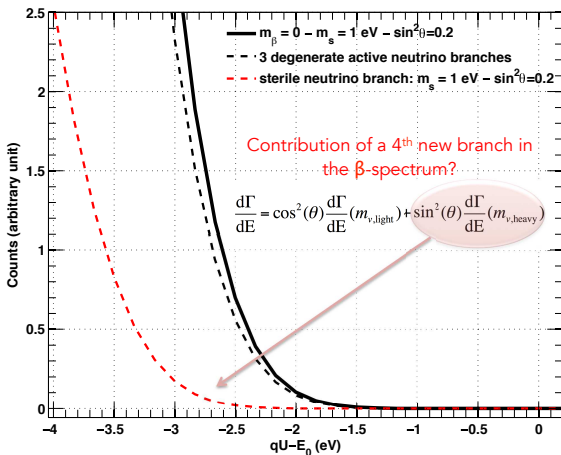


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Light Sterile Neutrino in KATRIN

Integral Tritium β -decay spectrum near endpoint $E_0=18.575$ keV



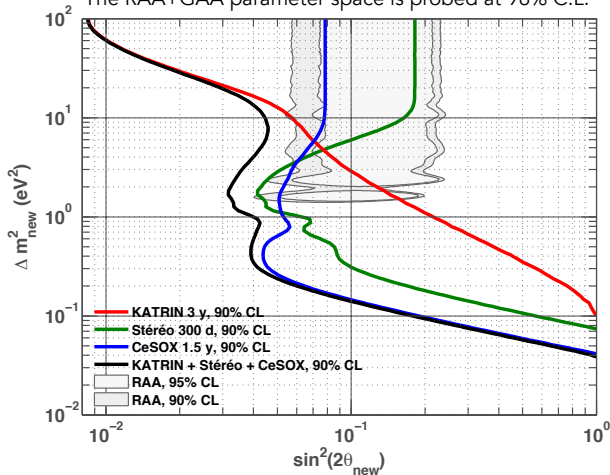
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KATRIN + Stéréo + CeSOX



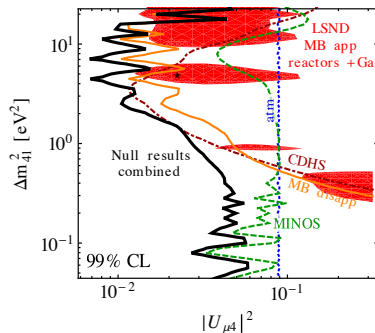
The RAA+GAA parameter space is probed at 98% C.L.



Hints from appearance experiments (LSND)

$$\sin^2 2\theta_{\mu e} \approx \frac{1}{4} \sin^2 2\theta_{ee} \sin^2 2\theta_{\mu\mu}$$

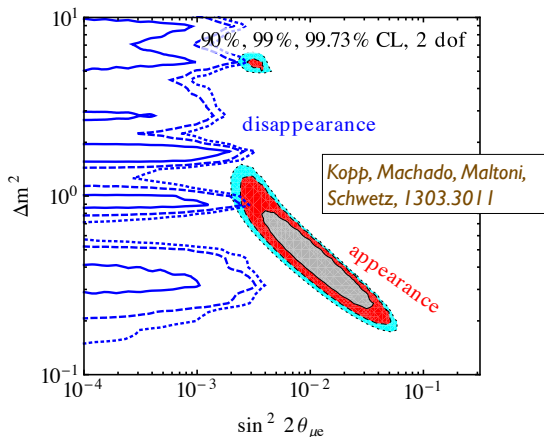
necessarily predict signal
in ν_{μ} disappearance -
but not seen



Kopp, Machado, Maltoni, Schwetz, 1303.3011

Strong tension in global data

- consistency of appearance and disappearance data with p -value 10^{-4}



expect somewhat increased tension due to recent data from MINOS, SK-atm, ICARUS, OPERA (potentially also IceCube)

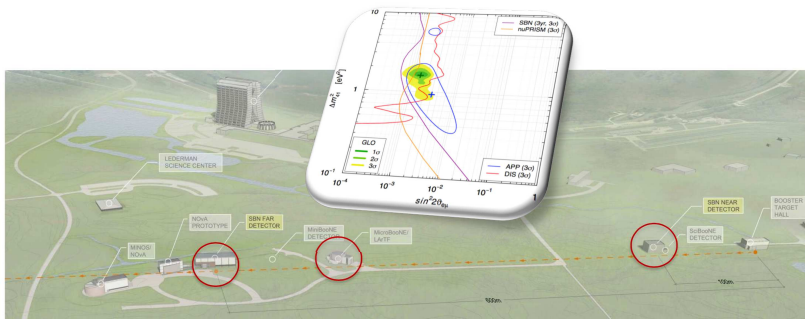
C. Giunti et al find somewhat better fit: p -value 10^{-3} 1308.5288

eV-scale sterile neutrinos

- *situation is ambiguous*
see also talk by C. Giunti
- *need to clarify experimentally*
talk by T. Lasserre



The Fermilab SBN program



ICARUS
Fewer ν_μ ?
More ν_e ?

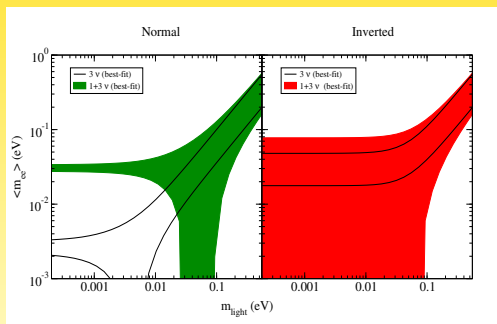
MicroBooNE
Fewer ν_μ ?
More ν_e ?

SBND **Produce**
 ν_μ ν_μ
 $\sim 1\% \nu_e$ $\sim 1\% \nu_e$

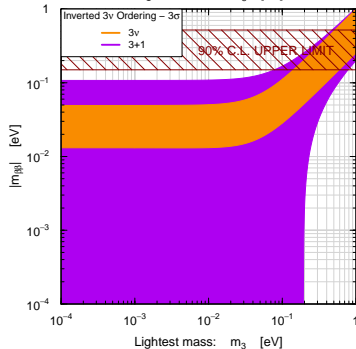
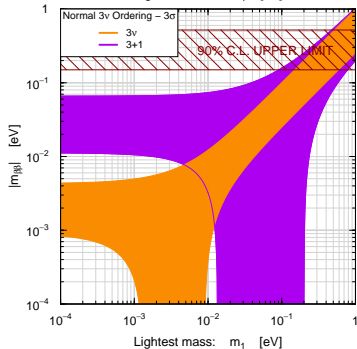
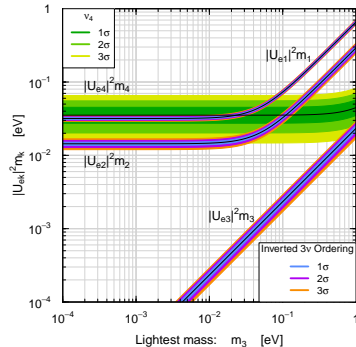
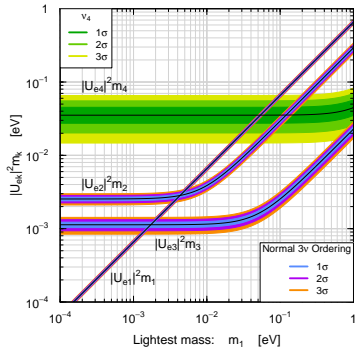


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Messing up 3 Majorana neutrino paradigm?

light sterile neutrinos, with $\sqrt{\Delta m_{st}^2} \sin^2 \theta_{st} \simeq |m_{ee}|_{IH}^{3\nu}$ Barry, W.R., Zhang; Giunti *et al.*; Girardi, Meroni, Petcov

$$m_{\beta\beta} = |U_{e1}|^2 m_1 + |U_{e2}|^2 e^{i\alpha_{21}} m_2 + |U_{e3}|^2 e^{i\alpha_{31}} m_3 + |U_{e4}|^2 e^{i\alpha_{41}} m_4$$



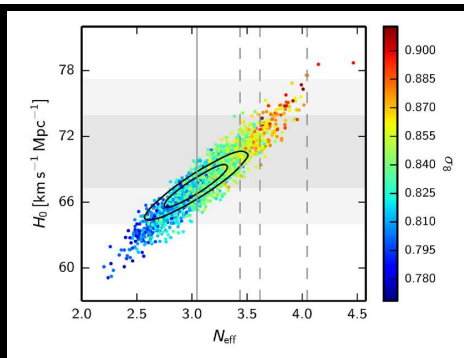
GOING BEYOND THE MASS

$$\Omega = \frac{\rho}{\rho_c} = \sum m_{\nu,i} n_{\nu,i} \quad n_{\nu} = \frac{3}{4} \left(\frac{T_{\nu}}{T_{\gamma}} \right)^3 n_{\gamma}$$

Normally $T_{\nu} = \left(\frac{4}{11}\right)^{1/3} T_{\gamma}$, but could be different. Normally the relativistic energy density in neutrinos is quantified through the relation

$$N_{eff} = \frac{\rho_{\nu,rel}}{\rho_{\nu 0}} \quad \rho_{\nu 0} = \frac{7}{8} \left(\frac{T_{\nu}}{T_{\gamma}} \right)^4 \rho_{\gamma}$$

N_{eff} is a measure of any type of "dark radiation"



THE CONCLUSION SEEMS TO BE THAT THERE IS NO EVIDENCE FOR ANY PHYSICS BEYOND THE STANDARD MODEL

BUT BE AWARE THAT IN EXTENDED MODELS THIS CAN BE VERY DIFFERENT!

$$N_{\text{eff}}^{\text{SM}} = 3.046$$

[Mangano, Miele, Pastor, Pinto, Pisanti, Serpico, NPB 729 (2005) 221]

Bottom line: Sterile neutrinos in the mass range preferred by SBL data can be accommodated by cosmology, but **ONLY** if they are not fully thermalised

How can this be achieved?

A large neutrino lepton asymmetry

(see e.g. STH, Tamborra, Tram 1204.5861, Saviano et al. arXiv:1302.1200)

New, non-standard interactions in the sterile sector

(e.g. STH, Hansen, Tram, 1310.5926, Dasgupta & Kopp 1310.6337, Bringmann, Hasenkamp & Kersten 1312.4947, Archidiacono, STH, Hansen, Tram 1404.5915 Chu, Dasgupta & Kopp 1505.02795)

Parameters of our universe chosen

\ni ν Physics 

$\Delta m_{ij}^2, \theta_{ij}, \delta?$

$E(\text{CRs}), h(\text{atms}); \rho(\text{atms}), \tau(\mu), \tau(\pi^\pm)$

$R_\odot, \rho_\odot, R_\otimes, \rho_\otimes \ni$ Reactors 

EC measurements of e -neutrino "mass" ??

Microcalorimeters, etc !!

\ni *Hope for $m(\nu_e)$ experiments*

Holmium From Latin "Holmia": Stockholm.

