

# Status of the reactor antineutrino anomalies and implications for active-sterile neutrino mixing

**Carlo Giunti**

INFN, Torino, Italy

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# Mainstream Three Neutrino Mixing Paradigm

- ▶ Supported by robust, abundant, and consistent solar, atmospheric and long-baseline (accelerator and reactor) neutrino oscillation data.
- ▶ Flavor Neutrinos:  $\nu_e, \nu_\mu, \nu_\tau$  produced in Weak Interactions
- ▶ Massive Neutrinos:  $\nu_1, \nu_2, \nu_3$  propagate from Source to Detector
- ▶ Neutrino Mixing: a Flavor Neutrino is a **superposition** of Massive Neutrinos

$$\begin{pmatrix} |\nu_e\rangle \\ |\nu_\mu\rangle \\ |\nu_\tau\rangle \end{pmatrix} = \begin{pmatrix} U_{e1}^* & U_{e2}^* & U_{e3}^* \\ U_{\mu1}^* & U_{\mu2}^* & U_{\mu3}^* \\ U_{\tau1}^* & U_{\tau2}^* & U_{\tau3}^* \end{pmatrix} \begin{pmatrix} |\nu_1\rangle \\ |\nu_2\rangle \\ |\nu_3\rangle \end{pmatrix}$$

- ▶  $U$  is the  $3 \times 3$  unitary Neutrino Mixing Matrix
- ▶  $P_{\nu_\alpha \rightarrow \nu_\beta}(L) = \sum_{k,j} U_{\beta k} U_{\alpha k}^* U_{\beta j}^* U_{\alpha j} \exp\left(-i \frac{\Delta m_{kj}^2 L}{2E}\right)$  ( $\alpha, \beta = e, \mu, \tau$ )
- ▶ The oscillation probabilities depend on

$$U \text{ (osc. amplitude)} \quad \text{and} \quad \Delta m_{kj}^2 \equiv m_k^2 - m_j^2 \text{ (osc. phase)}$$

- ▶ In the mainstream  $3\nu$  mixing paradigm there are **two independent  $\Delta m^2$ 's**:

- ▶  $\Delta m_{\text{SOL}}^2 = \Delta m_{21}^2 \simeq 7.4 \times 10^{-5} \text{ eV}^2$       Solar Mass Splitting

- ▶  $\Delta m_{\text{ATM}}^2 \simeq |\Delta m_{31}^2| \simeq 2.5 \times 10^{-3} \text{ eV}^2$       Atmospheric Mass Splitting

- ▶ The **solar and atmospheric mass splittings generate oscillations that are detectable at the distances**

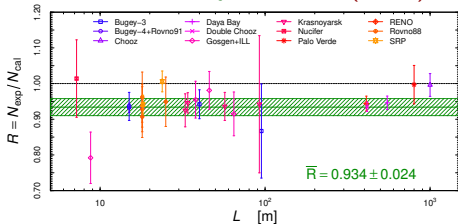
- ▶  $L_{\text{SOL}}^{\text{osc}} \gtrsim \frac{E_\nu}{\Delta m_{\text{SOL}}^2} \approx 50 \text{ km} \frac{E_\nu}{\text{MeV}}$

- ▶  $L_{\text{ATM}}^{\text{osc}} \gtrsim \frac{E_\nu}{\Delta m_{\text{ATM}}^2} \approx 1 \text{ km} \frac{E_\nu}{\text{MeV}}$

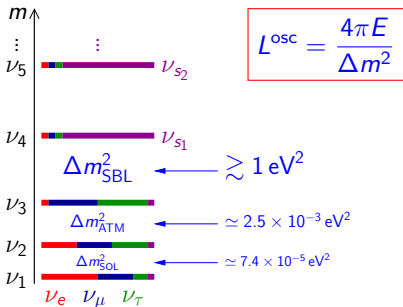
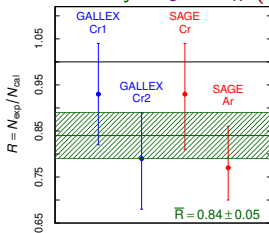
- ▶ The **solar and atmospheric mass splittings cannot explain flavor neutrino transitions at shorter distances.**

# Short-Baseline Neutrino Oscillation Anomalies

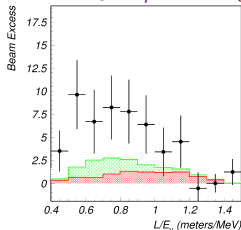
## Reactor Anomaly: $\bar{\nu}_e \rightarrow \bar{\nu}_x$ ( $\sim 3\sigma$ )



## Gallium Anomaly: $\nu_e \rightarrow \nu_x$ ( $\sim 3\sigma$ )



## LSND Anomaly: $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ ( $\sim 4\sigma$ )



Minimal perturbation of  $3\nu$  mixing: effective  $3+1$  with  $|U_{e4}|, |U_{\mu 4}|, |U_{\tau 4}| \ll 1$

# Effective 3+1 SBL Oscillation Probabilities

Appearance ( $\alpha \neq \beta$ )

$$P_{\nu_\alpha \rightarrow \nu_\beta}^{\text{SBL}(-)(-)} \simeq \sin^2 2\vartheta_{\alpha\beta} \sin^2 \left( \frac{\Delta m_{41}^2 L}{4E} \right)$$

$$\sin^2 2\vartheta_{\alpha\beta} = 4|U_{\alpha 4}|^2 |U_{\beta 4}|^2$$

Disappearance

$$P_{\nu_\alpha \rightarrow \nu_\alpha}^{\text{SBL}(-)(-)} \simeq 1 - \sin^2 2\vartheta_{\alpha\alpha} \sin^2 \left( \frac{\Delta m_{41}^2 L}{4E} \right)$$

$$\sin^2 2\vartheta_{\alpha\alpha} = 4|U_{\alpha 4}|^2 (1 - |U_{\alpha 4}|^2)$$

$$U = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} & U_{\mu 4} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} & U_{\tau 4} \\ U_{s1} & U_{s2} & U_{s3} & U_{s4} \end{pmatrix}$$

SBL

- ▶ 6 mixing angles
- ▶ 3 Dirac CP phases
- ▶ 3 Majorana CP phases

- ▶  $\Delta m_{\text{SBL}}^2 = \Delta m_{41}^2 \simeq \Delta m_{42}^2 \simeq \Delta m_{43}^2$
- ▶ CP violation is not observable in SBL experiments!
- ▶ Observable in LBL accelerator exp. sensitive to  $\Delta m_{\text{ATM}}^2$  [de Gouvea et al, arXiv:1412.1479, arXiv:1507.03986, arXiv:1605.09376; Palazzo et al, arXiv:1412.7524, arXiv:1509.03148; Kayser et al, arXiv:1508.06275, arXiv:1607.02152] and solar exp. sensitive to  $\Delta m_{\text{SOL}}^2$  [Long, Li, Giunti, arXiv:1304.2207]

## Common Parameterization of $4\nu$ Mixing

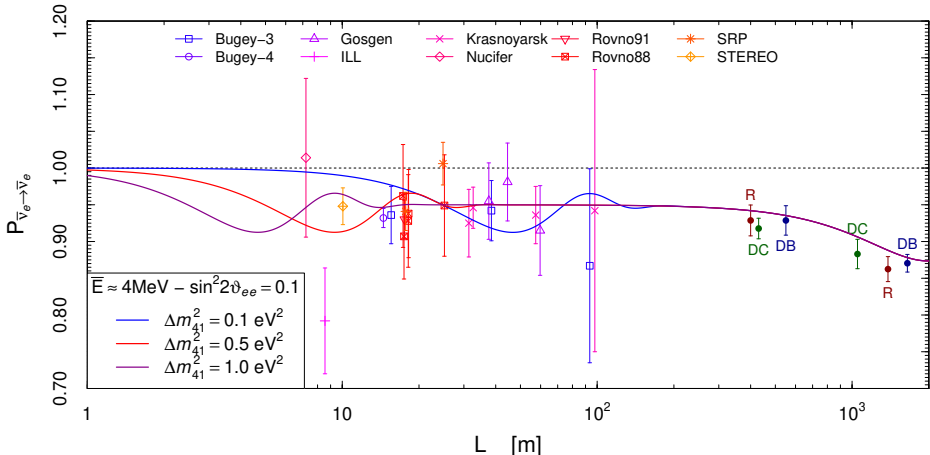
$$U = [W^{34} R^{24} W^{14} R^{23} W^{13} R^{12}] \text{diag}\left(1, e^{i\lambda_{21}}, e^{i\lambda_{31}}, e^{i\lambda_{41}}\right)$$

$$= \begin{pmatrix} c_{12}c_{13}c_{14} & s_{12}c_{13}c_{14} & c_{14}s_{13}e^{-i\delta_{13}} & s_{14}e^{-i\delta_{14}} \\ \dots & \dots & \dots & c_{14}s_{24} \\ \dots & \dots & \dots & c_{14}c_{24}s_{34}e^{-i\delta_{34}} \\ \dots & \dots & \dots & c_{14}c_{24}c_{34} \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & e^{i\lambda_{21}} & 0 & 0 \\ 0 & 0 & e^{i\lambda_{31}} & 0 \\ 0 & 0 & 0 & e^{i\lambda_{41}} \end{pmatrix}$$

$$|U_{e4}|^2 = \sin^2 \vartheta_{14} \Rightarrow \sin^2 2\vartheta_{ee} = 4|U_{e4}|^2 (1 - |U_{e4}|^2) = \sin^2 2\vartheta_{14}$$

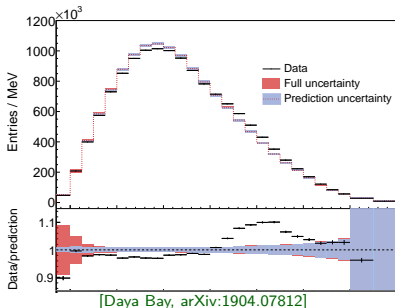
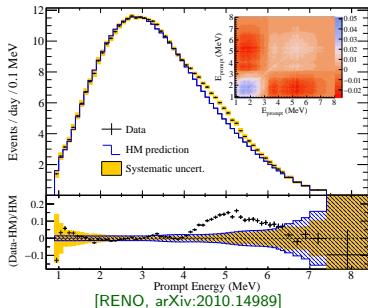
$$|U_{\mu 4}|^2 = \cos^2 \vartheta_{14} \sin^2 \vartheta_{24} \simeq \sin^2 \vartheta_{24} \Rightarrow \sin^2 2\vartheta_{\mu\mu} = 4|U_{\mu 4}|^2 (1 - |U_{\mu 4}|^2) \simeq \sin^2 2\vartheta_{24}$$

# Short-Baseline Reactor Neutrino Oscillations



- ▶  $\Delta m_{\text{SBL}}^2 \gtrsim 0.5 \text{ eV}^2 \gg \Delta m_{\text{ATM}}^2$
- ▶ SBL oscillations are **averaged** at the Daya Bay, RENO, and Double Chooz near detectors  $\implies$  **no spectral distortion**
- ▶ The reactor antineutrino anomaly is **model dependent** (depends on the theoretical reactor neutrino flux calculation; is it reliable?).

# Reactor Antineutrino 5 MeV Bump (Shoulder)



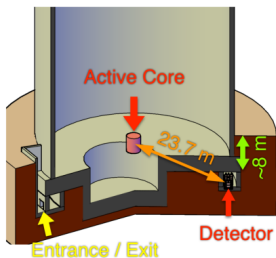
- ▶ Discovered in 2014 by RENO, Double Chooz, Daya Bay.
- ▶ **Cannot** be explained by neutrino oscillations (SBL oscillations are averaged in RENO, DC, DB).
- ▶ If it is due to a theoretical miscalculation of the spectrum, it **can have opposite effects on the anomaly:**
  - [see: Berryman, Huber, arXiv:1909.09267]
  - ▶ If it is a 4-6 MeV excess it **increases** the anomaly:  
recent HKSS flux calculation  
[Hayen, Kostensalo, Severijns, Suhonen, arXiv:1908.08302]
  - ▶ If it is a 1-4 MeV suppression it **decreases** the anomaly:  
recent EF flux calculation  
[Estienne, Fallot, et al, arXiv:1904.09358]  
new KI  $^{235}\text{U}$  flux renormalization  
[Kopeikin, Skorokhvatov, Titov, arXiv:2103.01684]



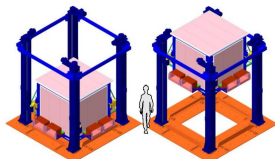
# Model Indep. Measurements of Reactor $\nu$ Osc.

Ratios of spectra at different distances

## NEOS

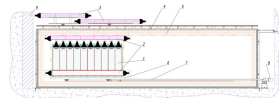


## DANSS

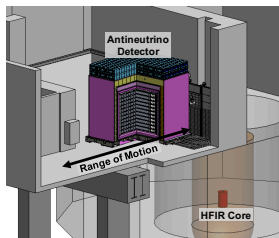


DANSS on a lifting platform

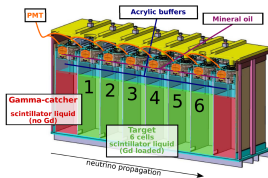
## Neutrino-4



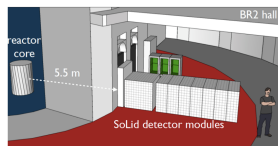
## PROSPECT



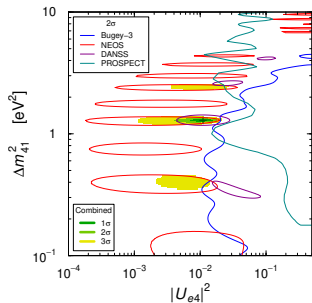
## STEREO



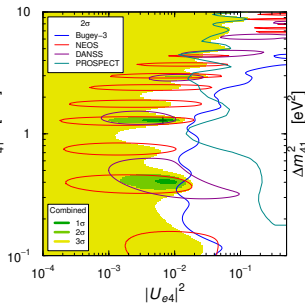
## SoLid



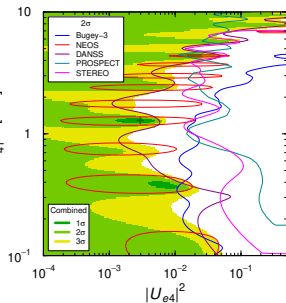
2018



2019



2020



- ▶ **2018:** remarkable agreement of the DANSS and NEOS best-fit regions at  $\Delta m_{41}^2 \approx 1.3$  eV<sup>2</sup>  $\implies$  model independent indication in favor of SBL oscillations. [Gariazzo, Giunti, Laveder, Li, arXiv:1801.06467]

[Dentler, Hernandez-Cabezudo, Kopp, Machado, Maltoni, Martinez-Soler, Schwetz, arXiv:1803.10661]

- ▶ **2019:** decreased agreement between NEOS and DANSS allowed regions. [CG, Y.F. Li, Y.Y. Zhang, arXiv:1912.12956]

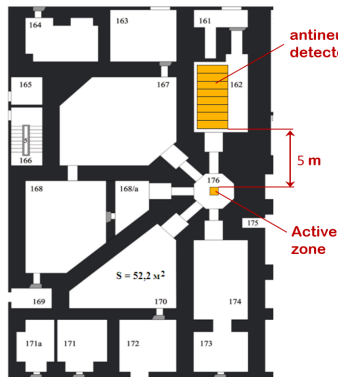
- ▶ **2020:** No 2 $\sigma$  DANSS allowed regions (exclusion curve).  
No compelling indication of oscillations.

In practice these reactor experiments exclude large values of  $|U_{e4}|^2$  for

$$0.1 \lesssim \Delta m_{41}^2 \lesssim 10 \text{ eV}^2$$

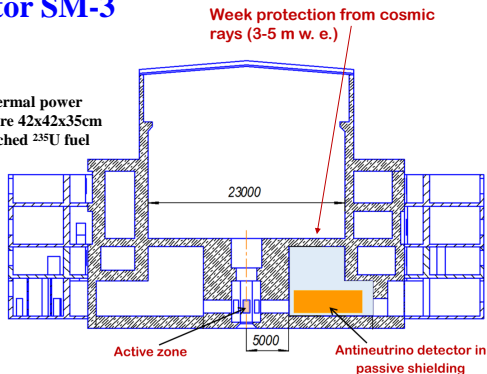
# Neutrino-4

[arXiv:1708.00421, arXiv:1809.10561, arXiv:2003.03199, arXiv:2005.05301, arXiv:2006.13639]



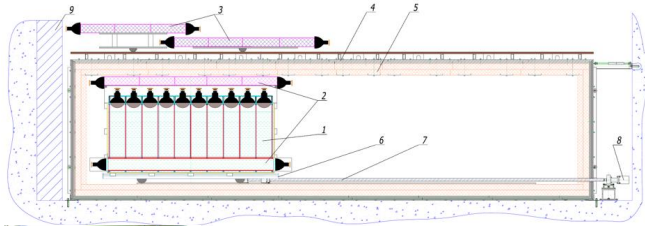
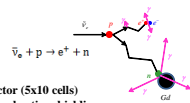
## Reactor SM-3

100 MW thermal power  
Compact core 42x42x35cm  
Highly enriched  $^{235}\text{U}$  fuel



Due to some peculiar characteristics of its construction, reactor SM-3 provides the most favorable conditions to search for neutrino oscillations at short distances. However, SM-3 reactor, as well as other research reactors, is located on the Earth's surface, hence, cosmic background is the major difficulty in considered experiment.

## Movable and spectrum sensitive antineutrino detector at SM-3 reactor



1. detector (5x10 cells)
2. internal active shielding
3. external active shielding
4. steel and lead
5. borated polyethylene
6. moveable platform
7. feed screw
8. step motor
9. shielding



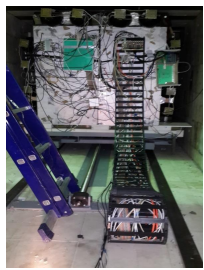
Passive shielding - 60 tons

Neutrino channel outside and inside



Detector prototype

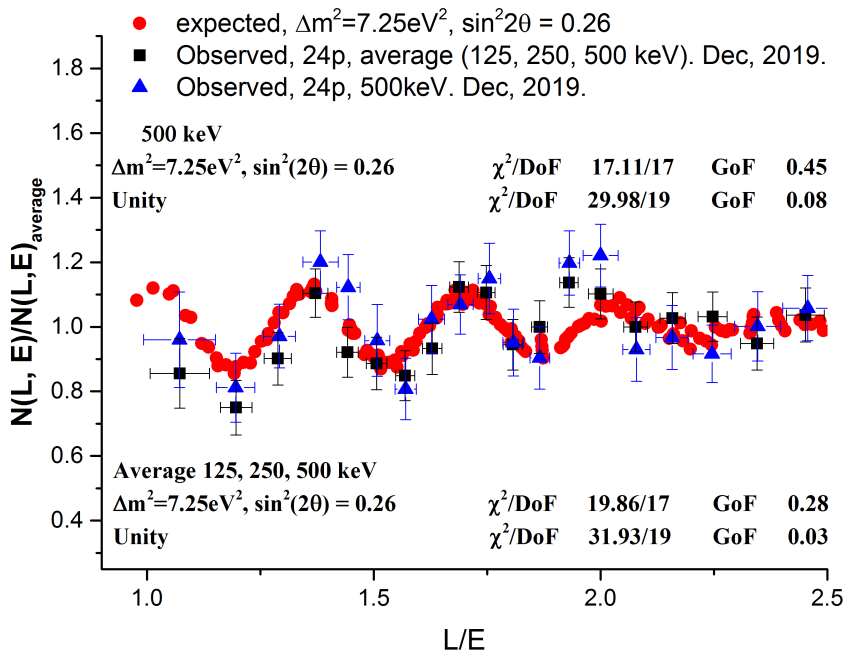
Full-scale detector

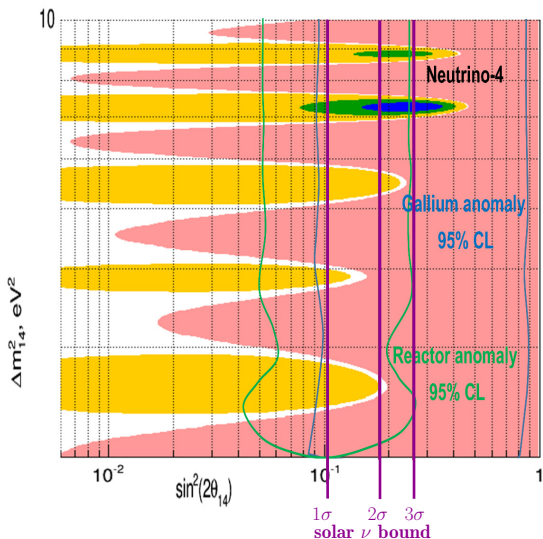


Liquid scintillator detector  
50 sections 0.235x0.235x0.85m<sup>3</sup>

Range of measurements is 6 - 12 meters

[A. Serebrov, 17 September 2020]





- ▶ Neutrino-4 best fit:

$$\sin^2 2\vartheta_{ee} = 0.26$$

$$\Delta m_{41}^2 = 7.25 \text{eV}^2$$

- ▶ Very large mixing!
- ▶ Not a small perturbation of  $3\nu$  mixing.
- ▶ Tension with solar neutrino bound.

[Palazzo, arXiv:1105.1705, arXiv:1201.4280]

[Giunti, Laveder, Li, Liu, Long, arXiv:1210.5715]

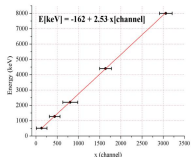
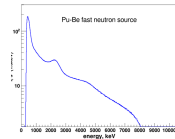
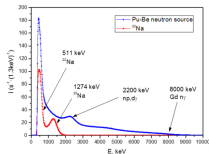
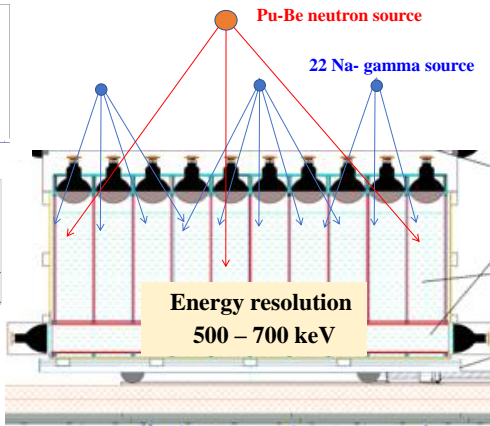
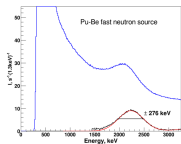
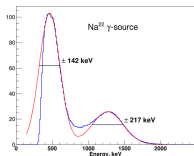
[Gariazzo, Giunti, Laveder, Li, arXiv:1703.00860]

# Oscillations of Last Neutrino-4 Results

[arXiv:2005.05301]

version	date	$(\Delta m_{41}^2)_{\text{bf}}$	$(\sin^2 2\vartheta_{ee})_{\text{bf}}$	statistical significance
v1	9 May 2020	$7.25 \pm 1.0$	$0.26 \pm 0.09$	$2.8\sigma$
v2	18 Jun 2020	$7.25 \pm 1.0$	$0.26 \pm 0.09$	$2.8\sigma$
v3	31 Jul 2020	$7.25 \pm 1.09$	$0.26 \pm 0.09$	$2.9\sigma$
v4	16 Aug 2020	$7.25 \pm 1.09$	$0.26 \pm 0.09$	$2.9\sigma$
v5	14 Feb 2021	$7.2 \pm 1.13$	$0.29 \pm 0.12$	$2.4\sigma$
v6	21 Feb 2021	$7.2 \pm 1.13$	$0.26 \pm 0.08$	$3.2\sigma$
v7	5 Apr 2021	$7.3 \pm 1.17$	$0.36 \pm 0.12$	$2.9\sigma$

# Energy calibration of the full-scale detector

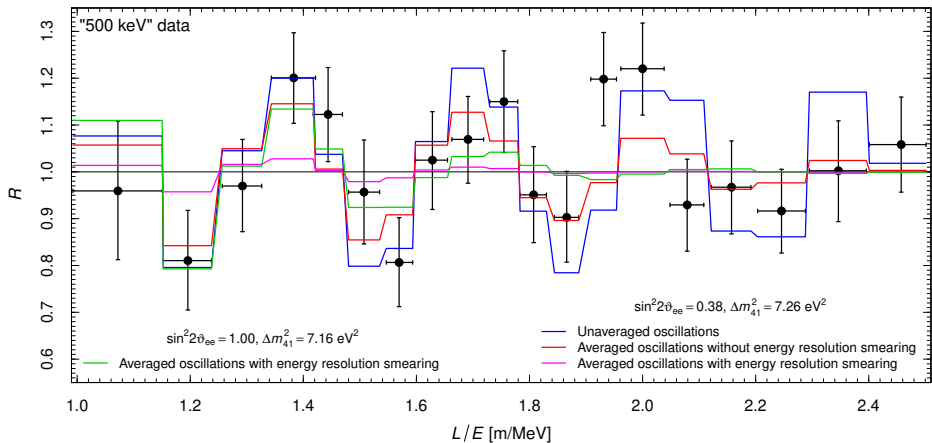


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- ▶ We approximate the energy resolution with the function

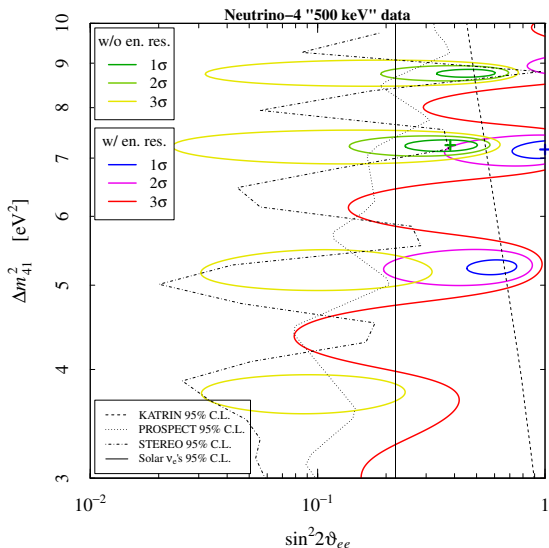
$$R(E_p, E'_p) = \frac{1}{\sqrt{2\pi}\sigma_{E_p}} \exp\left(-\frac{(E_p - E'_p)^2}{2\sigma_{E_p}^2}\right) \quad \text{with} \quad \sigma_{E_p} = 0.19 \sqrt{\frac{E_p}{\text{MeV}}} \text{ MeV}$$





$$\left\langle \sin^2 \left( \frac{\Delta m_{41}^2 L}{4E} \right) \right\rangle_{ik} = \frac{\int_{L_k^{\min}}^{L_k^{\max}} dL L^{-2} \int_{E_i^{\min}}^{E_i^{\max}} dE'_p \int dE_p R(E_p, E'_p) \sin^2 \left( \frac{\Delta m_{41}^2 L}{4E} \right) \phi_{\bar{\nu}_e}(E) \sigma_{\bar{\nu}_e p}(E)}{\int_{L_k^{\min}}^{L_k^{\max}} dL L^{-2} \int_{E_i^{\min}}^{E_i^{\max}} dE'_p \int dE_p R(E_p, E'_p) \phi_{\bar{\nu}_e}(E) \sigma_{\bar{\nu}_e p}(E)}$$

[CG, Li, Ternes, Zhang, arXiv:2101.06785]



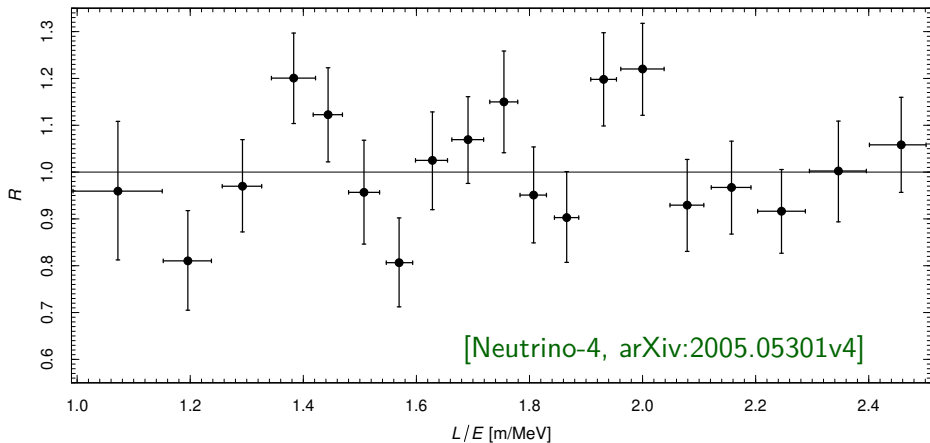
$$\chi^2 = \sum_{j=1}^{19} \left( \frac{R_j^{\text{the}} - R_j^{\text{exp}}}{\Delta R_j^{\text{exp}}} \right)^2$$

	without en. res.	with en. res.
$\chi^2_{\min}$	14.9	18.2
GoF	60%	37%
$(\sin^2 2\vartheta_{ee})_{\text{bf}}$	0.38	1.0
$(\Delta m_{41}^2)_{\text{bf}}$	7.2	7.2
$\Delta\chi^2_{\text{NO}}$	13.1	9.8
$p$ -value	0.0014	0.0075
$\sigma$ -value	3.2	2.7

[CG, Li, Ternes, Zhang, arXiv:2101.06785]

- ▶ Disconcerting comment in [arXiv:2005.05301v7](https://arxiv.org/abs/2005.05301v7): The simultaneous usage of energy interval  $\Delta E = 500$  keV and energy resolution  $\sigma = 250$  keV is incorrect, because it includes into the analysis the resolution of the detector twice as it was done in the work [Giunti, Li, Ternes, Zhang, [arXiv:2101.06785](https://arxiv.org/abs/2101.06785)].
- ▶ The Neutrino-4 collaboration thinks that energy binning takes into account the energy resolution.
- ▶ It is obvious that an event with an unknown true energy in an unknown energy bin can be counted in another bin because of the energy resolution.
- ▶ This effect is obviously not taken into account by the binning.
- ▶ This effect can be neglected if the energy resolution is much smaller than the bin width.
- ▶ This effect cannot be neglected in the Neutrino-4 experiment, where the the bin width is only twice of the energy resolution.

## Neutrino-4: Oscillations or Fluctuations?



# Wilks Theorem (1938)

## THE LARGE-SAMPLE DISTRIBUTION OF THE LIKELIHOOD RATIO FOR TESTING COMPOSITE HYPOTHESES<sup>1</sup>

BY S. S. WILKS

Let  $P_{\Omega}(O_n)$  be the least upper bound of  $P$  for the simple hypotheses in  $\Omega$ , and  $P_{\omega}(O_n)$  the least upper bound of  $P$  for those in  $\omega$ . Then

$$(2) \quad \lambda = \frac{P_{\omega}(O_n)}{P_{\Omega}(O_n)}$$

which optimum estimates of the  $\theta$ 's exist. That is, we shall assume the existence of functions  $\bar{\theta}_i(x_1, \dots, x_n)$  (maximum likelihood estimates of the  $\theta_i$ ) such that their distribution is

$$(3) \quad \frac{|c_{ij}|^{\frac{1}{2}}}{(2\pi)^{h/2}} e^{-\frac{1}{2} \sum_{i,j=1}^h c_{ij} z_i z_j} (1 + \phi) dz_1 \dots dz_h$$

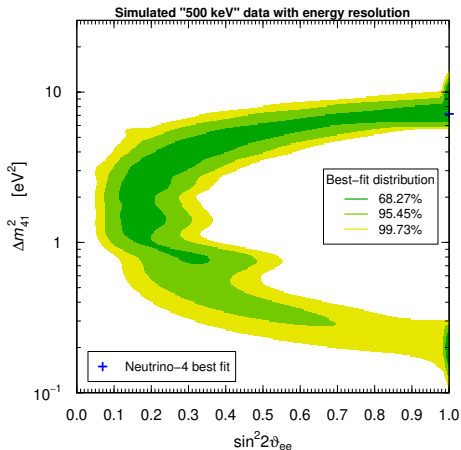
where  $z_i = (\bar{\theta}_i - \theta_i) \sqrt{n}$ ,  $c_{ij} = -E \left( \frac{\partial^2 \log f}{\partial \theta_i \partial \theta_j} \right)$ ,  $E$  denoting mathematical expectation, and  $\phi$  is of order  $1/\sqrt{n}$  and  $\|c_{ij}\|$  is positive definite. Denoting (3) by

*Theorem: If a population with a variate  $x$  is distributed according to the probability function  $f(x, \theta_1, \theta_2, \dots, \theta_h)$ , such that optimum estimates  $\bar{\theta}_i$  of the  $\theta_i$  exist which are distributed in large samples according to (3), then when the hypothesis  $H$  is true that  $\theta_i = \theta_{0i}$ ,  $i = m + 1, m + 2, \dots, h$ , the distribution of  $-2 \log \lambda$ , where  $\lambda$  is given by (2) is, except for terms of order  $1/\sqrt{n}$ , distributed like  $\chi^2$  with  $h - m$  degrees of freedom.*

# Deviations from $\chi^2$ Distribution (Wilks' Theorem)

[Agostini, Neumair, arXiv:1906.11854; Silaeva, Sinev, arXiv:2001.10752; Giunti, arXiv:2004.07577]  
[PROSPECT+STEREO, arXiv:2006.13147; Coloma, Huber, Schwetz, arXiv:2008.06083]

Even in the absence of real oscillations, binned data can often be fitted better by oscillations that reproduce the statistical fluctuations of the bins.



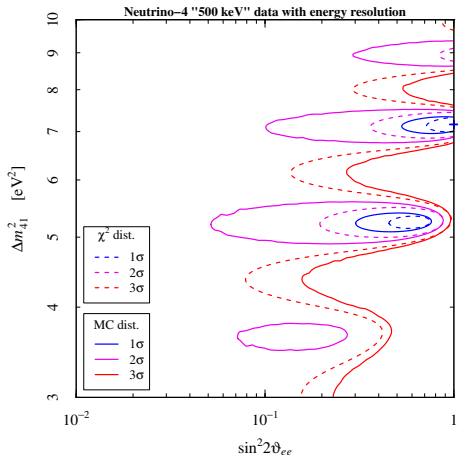
Distribution of best-fit points in a large set of random data generated without oscillations

	probability
$\sin^2 2\vartheta_{ee} < 0.1$	0.008
$0.1 < \sin^2 2\vartheta_{ee} < 0.5$	0.625
$0.5 < \sin^2 2\vartheta_{ee} < 0.9$	0.184
$\sin^2 2\vartheta_{ee} > 0.9$	0.183

[CG, Li, Ternes, Zhang, arXiv:2101.06785]

# Monte Carlo confidence intervals

- ▶ For each point on a grid in the  $(\sin^2 2\vartheta_{ee}, \Delta m_{41}^2)$  plane we generated a large number of random data sets (of the order of  $10^5$ ) with the uncertainties of the Neutrino-4 data set.
- ▶ For each random data set:
  - ▶ We calculated the value of  $\chi^2$  corresponding to the generating values of  $\sin^2 2\vartheta_{ee}$  and  $\Delta m_{41}^2$ :  $\chi_{\text{MC}}^2(\sin^2 2\vartheta_{ee}, \Delta m_{41}^2)$ .
  - ▶ We found the minimum value of  $\chi^2$  in the  $(\sin^2 2\vartheta_{ee}, \Delta m_{41}^2)$  plane:  $\chi_{\text{MC,min}}^2(\sin^2 2\vartheta_{ee}, \Delta m_{41}^2)$ .
- ▶ In this way, we obtained the distribution of  $\Delta\chi_{\text{MC}}^2(\sin^2 2\vartheta_{ee}, \Delta m_{41}^2) = \chi_{\text{MC}}^2(\sin^2 2\vartheta_{ee}, \Delta m_{41}^2) - \chi_{\text{MC,min}}^2(\sin^2 2\vartheta_{ee}, \Delta m_{41}^2)$ .
- ▶ This distribution allows us to determine if the value of  $\Delta\chi^2(\sin^2 2\vartheta_{ee}, \Delta m_{41}^2) = \chi^2(\sin^2 2\vartheta_{ee}, \Delta m_{41}^2) - \chi_{\text{min}}^2(\sin^2 2\vartheta_{ee}, \Delta m_{41}^2)$  obtained with the analysis of the actual Neutrino-4 data is included or not in a region with a fixed confidence level.



	$\chi^2$ dist.	MC dist.
$p$ -value	0.0075	0.028
$\sigma$ -value	2.7	2.2

[CG, Li, Ternes, Zhang, arXiv:2101.06785]

**Conclusion on Neutrino-4:** the claimed indication in favor of short-baseline neutrino oscillations with very large mixing is rather doubtful.



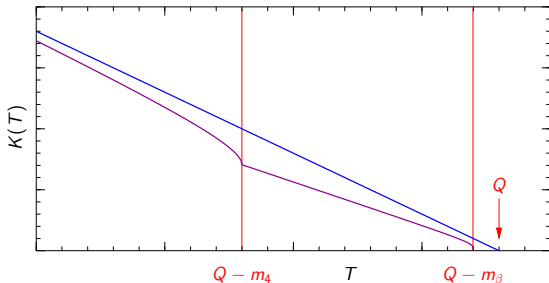
# Robust kinematical probe of $\nu_e - \nu_s$ mixing

Tritium Beta-Decay:  ${}^3\text{H} \rightarrow {}^3\text{He} + e^- + \bar{\nu}_e$

$$\frac{d\Gamma}{dT} = \frac{(\cos\vartheta_c G_F)^2}{2\pi^3} |\mathcal{M}|^2 F(E) p E K^2(T)$$

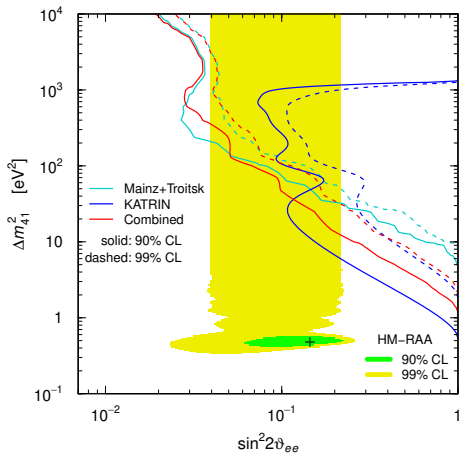
$$\frac{K^2(T)}{Q-T} = \sum_k |U_{ek}|^2 \sqrt{(Q-T)^2 - m_k^2} \theta(Q-T-m_k)$$

$$m_4 \gg m_{1,2,3} \Rightarrow \simeq (1 - |U_{e4}|^2) \sqrt{(Q-T)^2 - m_\beta^2} \theta(Q-T-m_\beta) \\ + |U_{e4}|^2 \sqrt{(Q-T)^2 - m_4^2} \theta(Q-T-m_4)$$



$$Q = M_{{}^3\text{H}} - M_{{}^3\text{He}} - m_e \\ = 18.58 \text{ keV}$$

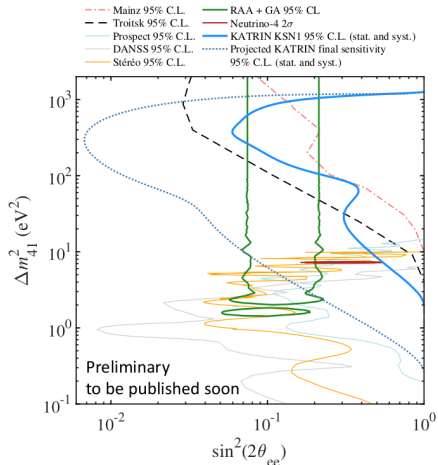
$$m_\beta^2 = \sum_{k=1}^3 |U_{ek}|^2 m_k^2$$



[Giunti, Y.F. Li, Y.Y. Zhang, arXiv:1912.12956]

$$\Delta m_{41}^2 \simeq m_4^2$$

$$\sin^2 2\vartheta_{ee} = 4|U_{e4}|^2 (1 - |U_{e4}|^2) \simeq 4|U_{e4}|^2 \quad \text{for} \quad |U_{e4}|^2 \ll 1$$



[KATRIN @ Neutrino 2020]

[arXiv:2011.05087]

# 3+1: Appearance vs Disappearance

▶ SBL Oscillation parameters:  $\Delta m_{41}^2$   $|U_{e4}|^2$   $|U_{\mu4}|^2$  ( $|U_{\tau4}|^2$ )

▶ Amplitude of  $\nu_e$  disappearance:

$$\sin^2 2\vartheta_{ee} = 4|U_{e4}|^2 (1 - |U_{e4}|^2) \simeq 4|U_{e4}|^2$$

▶ Amplitude of  $\nu_\mu$  disappearance:

$$\sin^2 2\vartheta_{\mu\mu} = 4|U_{\mu4}|^2 (1 - |U_{\mu4}|^2) \simeq 4|U_{\mu4}|^2$$

▶ Amplitude of  $\nu_\mu \rightarrow \nu_e$  transitions:

$$\sin^2 2\vartheta_{e\mu} = 4|U_{e4}|^2 |U_{\mu4}|^2 \simeq \frac{1}{4} \sin^2 2\vartheta_{ee} \sin^2 2\vartheta_{\mu\mu}$$

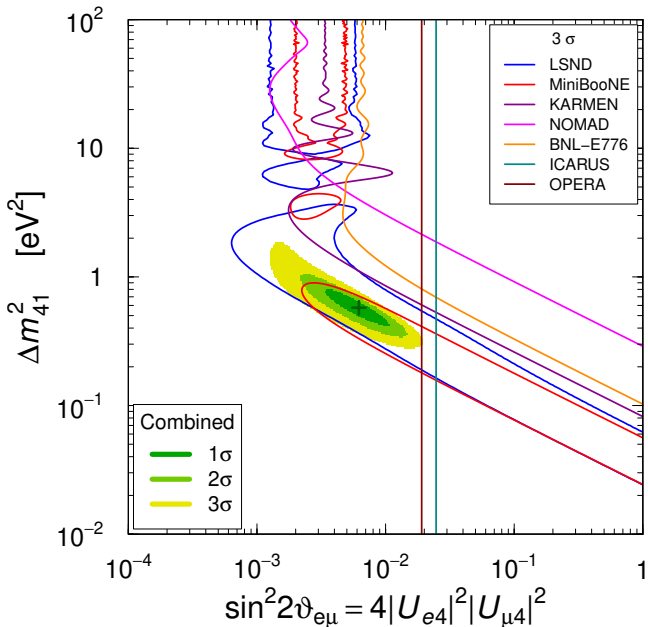
quadratically suppressed for small  $|U_{e4}|^2$  and  $|U_{\mu4}|^2$



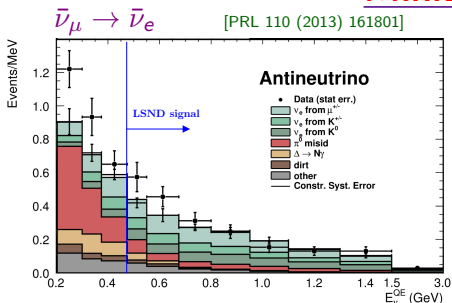
Appearance-Disappearance Tension

[Okada, Yasuda, IJMPA 12 (1997) 3669; Bilenky, CG, Grimus, EPJC 1 (1998) 247]

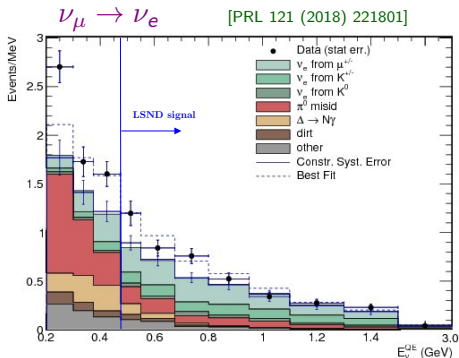
# $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ and $\nu_\mu \rightarrow \nu_e$ Appearance



# MiniBooNE

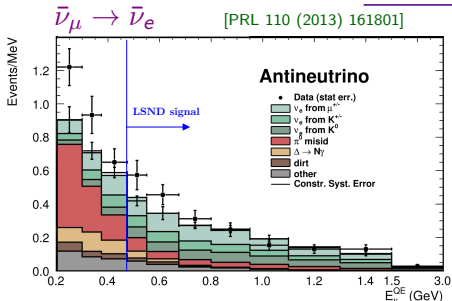


- ▶ Purpose: check the LSND signal
- ▶ Different  $L \simeq 540$  m
- ▶ Different  $200 \text{ MeV} \leq E \lesssim 3 \text{ GeV}$
- ▶ Similar  $L/E \Rightarrow$  Oscillations Smoking Gun?



- ▶ No money, no Near Detector
- ▶ Large beam-related background
- ▶ Large flux and cross section uncertainties

# MiniBooNE



▶ LSND signal?

▶ LSND: excess only for

$$\frac{L}{E} \lesssim 1.2 \frac{m}{\text{MeV}}$$

▶ MiniBooNE: the LSND excess should be at

$$E \gtrsim \frac{540 \text{ m}}{1.2 \text{ m}} \text{ MeV} \simeq 450 \text{ MeV}$$

▶ New large excess for

$$E \lesssim 450 \text{ MeV}$$

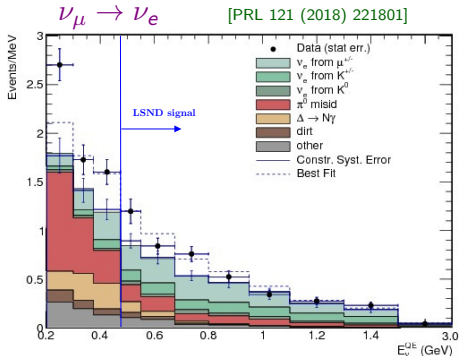
MiniBooNE low-energy anomaly

Maybe due to additional

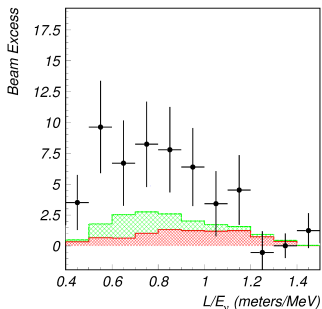
$\Delta \rightarrow N\gamma$  background?

[Ioannian et al, arXiv:1909.08571, arXiv:1912.01524]

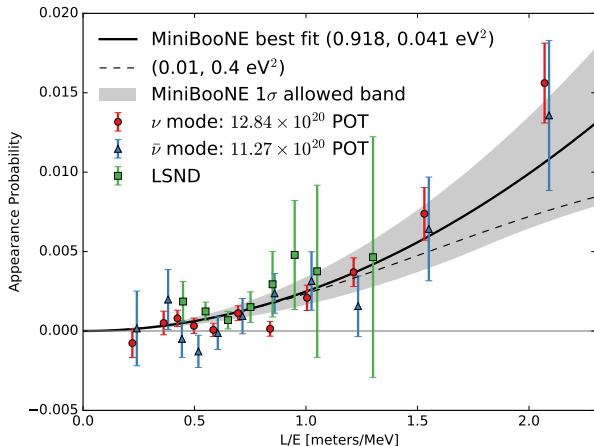
To be checked by MicroBooNE@FNAL?



► The MiniBooNE low-energy excess is at larger  $L/E$  than LSND.

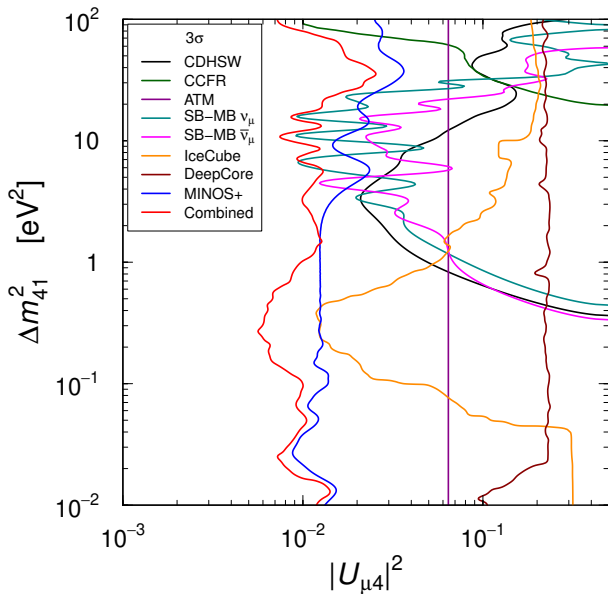


[LSND, PRD 64 (2001) 112007]



[MiniBooNE, PRL 121 (2018) 221801]

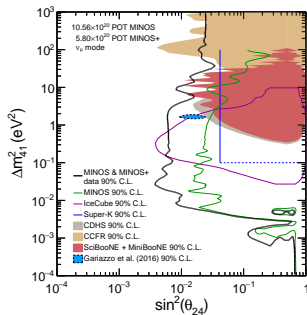
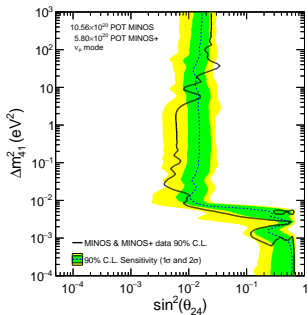
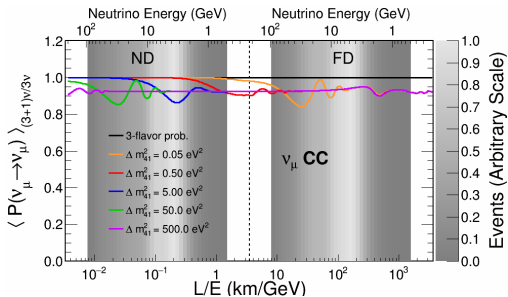
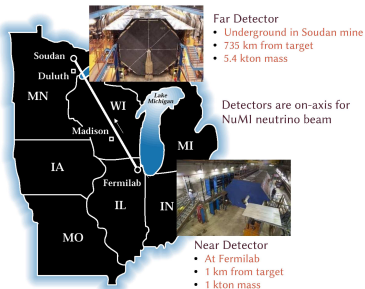
# $\nu_\mu$ and $\bar{\nu}_\mu$ Disappearance





# MINOS+

[PRL 122 (2019) 091803, arXiv:1710.06488]

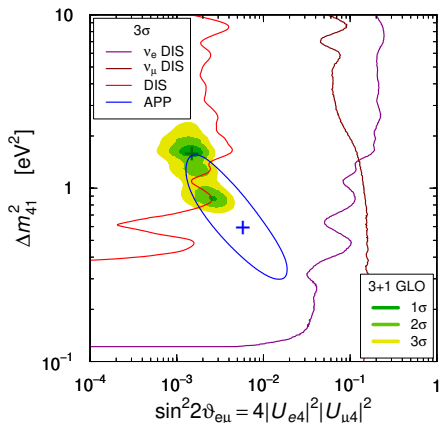


# Global Appearance-Disappearance Tension

$$\nu_e \text{ DIS} \\ \sin^2 2\vartheta_{ee} \simeq 4|U_{e4}|^2$$

$$\nu_\mu \text{ DIS} \\ \sin^2 2\vartheta_{\mu\mu} \simeq 4|U_{\mu 4}|^2$$

$$\nu_\mu \rightarrow \nu_e \text{ APP} \\ \sin^2 2\vartheta_{e\mu} = 4|U_{e4}|^2|U_{\mu 4}|^2 \simeq \frac{1}{4} \sin^2 2\vartheta_{ee} \sin^2 2\vartheta_{\mu\mu}$$



▶  $\nu_\mu \rightarrow \nu_e$  is quadratically suppressed!

▶ 2016 Global Fit:

$$\chi^2/\text{NDF} = 304.0/275$$

$$\text{GoF} = 11\%$$

$$\chi_{\text{PG}}^2/\text{NDF}_{\text{PG}} = 15.0/2$$

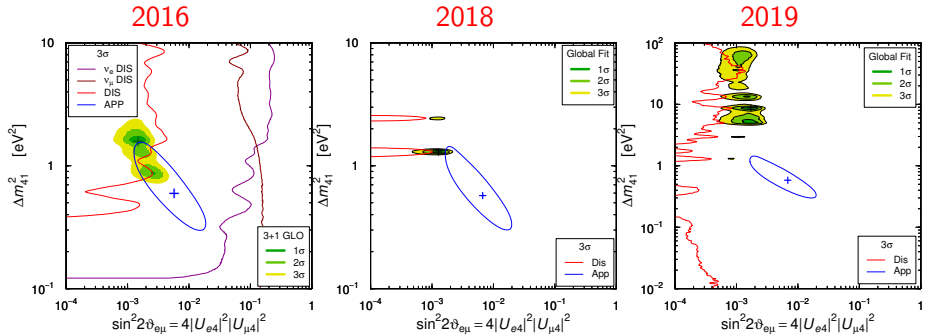
$$\text{GoF}_{\text{PG}} = 6 \times 10^{-4} \quad \leftarrow \text{☹}$$

▶ Similar tension in

$$3 + 2, \quad 3 + 3, \quad \dots, \quad 3 + N_s$$

[Giunti, Zavanin, arXiv:1508.03172]

# Global Appearance-Disappearance Tension

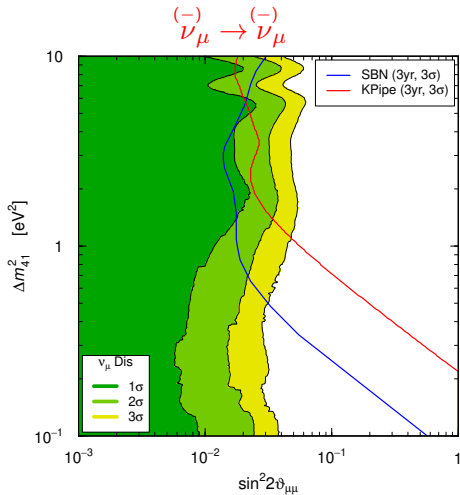
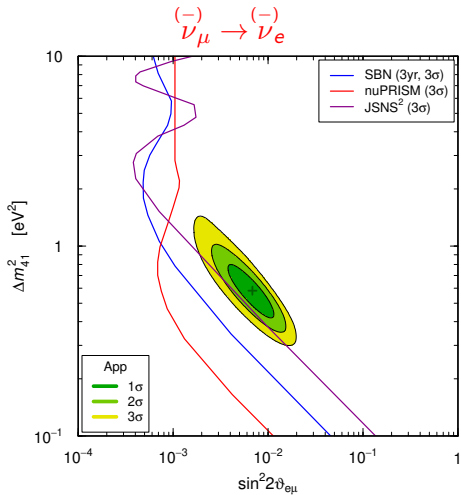


- ▶ 2016: Global Fit:  $\text{GoF}_{\text{PG}} \approx 6 \times 10^{-4}$
- ▶ 2018: Global Fit:  $\text{GoF}_{\text{PG}} \approx 2 \times 10^{-7}$
- ▶ 2019: Global Fit:  $\text{GoF}_{\text{PG}} \approx 7 \times 10^{-11}$

[arXiv:1602.01390, arXiv:1606.07673]

[arXiv:1801.06467, arXiv:1803.10661, arXiv:1901.08330]

# New Dedicated Experiments



# Conclusions

- ▶ Light sterile neutrinos can be powerful messengers of new physics beyond the SM.
- ▶ Historically, their existence is motivated by the reactor, Gallium and LSND short-baseline anomalies.
- ▶ The reactor antineutrino anomaly, discovered in 2011, is disappearing, because of new neutrino flux calculations and the absence of a clear model-independent signal in the new experiments (DANSS, PROSPECT, STEREO).
- ▶ The claimed Neutrino-4 indication in favor of short-baseline neutrino oscillations with very large mixing is rather doubtful.
- ▶ Important model-independent tests of the effect of  $m_4$  in  $\beta$ -decay (KATRIN), electron-capture (ECHo, HOLMES) and  $\beta\beta_{0\nu}$ -decay experiments.

- ▶ In principle, the simplest explanation of the LSND and MiniBooNE  $\nu_e$ -like excesses is neutrino oscillations, that requires a new  $\Delta m_{\text{SBL}}^2$  associated with a sterile neutrino.
- ▶ Unfortunately, the LSND and MiniBooNE  $\nu_e$ -like excesses are too large to be compatible with the existing bounds on  $\nu_e$  and  $\nu_\mu$  disappearance in the framework of  $3 + N_s$  active-sterile neutrino mixing:

### APPEARANCE-DISAPPEARANCE TENSION

- ▶ Alternative (ad hoc) explanations exist with a heavy sterile neutrino produced and decayed in the detector.
- ▶ Promising Fermilab SBN program aimed at a conclusive solution of the mystery with three Liquid Argon Time Projection Chamber (LArTPC): a near detector (LAr1-ND), an intermediate detector (MicroBooNE) and a far detector (ICARUS-T600).
- ▶ It is important that LArTPC detectors can distinguish a single  $\nu_e$ -induced electron from a  $\gamma$  or a collimated  $e^+e^-$  pair.