Status of the reactor antineutrino anomalies and implications for active-sterile neutrino mixing

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Mainstream Three Neutrino Mixing Paradigm

- Supported by robust, abundant, and consistent solar, atmospheric and long-baseline (accelerator and reactor) neutrino oscillation data.
- Flavor Neutrinos: ν_e , ν_μ , ν_τ produced in Weak Interactions
- Massive Neutrinos: ν_1 , ν_2 , ν_3 propagate from Source to Detector
- Neutrino Mixing: a Flavor Neutrino is a superposition of Massive Neutrinos

$$\begin{pmatrix} |\nu_e\rangle\\ |\nu_\mu\rangle\\ |\nu_\tau\rangle \end{pmatrix} = \begin{pmatrix} U_{e1}^* & U_{e2}^* & U_{e3}^*\\ U_{\mu1}^* & U_{\mu2}^* & U_{\mu3}^*\\ U_{\tau1}^* & U_{\tau2}^* & U_{\tau3}^* \end{pmatrix} \begin{pmatrix} |\nu_1\rangle\\ |\nu_2\rangle\\ |\nu_3\rangle \end{pmatrix}$$

• U is the 3×3 unitary Neutrino Mixing Matrix

$$\blacktriangleright P_{\nu_{\alpha} \to \nu_{\beta}}(L) = \sum_{k,j} U_{\beta k} U_{\alpha k}^{*} U_{\beta j}^{*} U_{\alpha j} \exp\left(-i\frac{\Delta m_{kj}^{2}L}{2E}\right) \qquad (\alpha, \beta = e, \mu, \tau)$$

The oscillation probabilities depend on

U (osc. amplitude) and $\Delta m_{kj}^2 \equiv m_k^2 - m_j^2$ (osc. phase)

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- In the mainstream 3ν mixing paradigm there are two independent Δm^2 's:
 - $\Delta m_{SOL}^2 = \Delta m_{21}^2 \simeq 7.4 \times 10^{-5} \, \text{eV}^2$ Solar Mass Splitting
 - $\blacktriangleright \ \Delta m^2_{\rm ATM} \simeq |\Delta m^2_{\rm 31}| \simeq 2.5 \times 10^{-3} \, {\rm eV}^2$

Atmospheric Mass Splitting

The solar and atmospheric mass splittings generate oscillations that are detectable at the distances

$$L_{\text{SOL}}^{\text{osc}} \gtrsim \frac{E_{\nu}}{\Delta m_{\text{SOL}}^2} \approx 50 \text{ km } \frac{E_{\nu}}{\text{MeV}}$$

$$L_{\text{ATM}}^{\text{osc}} \gtrsim \frac{E_{\nu}}{\Delta m_{\text{ATM}}^2} \approx 1 \text{ km } \frac{E_{\nu}}{\text{MeV}}$$

The solar and atmospheric mass splittings cannot explain flavor neutrino transitions at shorter distances.

Short-Baseline Neutrino Oscillation Anomalies



Minimal perturbation of 3ν mixing: effective 3+1 with $|U_{e4}|, |U_{\mu4}|, |U_{\tau4}| \ll 1$

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Effective 3+1 SBL Oscillation Probabilities



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Common Parameterization of 4ν **Mixing**

$$U = \left[W^{34} R^{24} W^{14} R^{23} W^{13} R^{12} \right] \operatorname{diag} \left(1, e^{i\lambda_{21}}, e^{i\lambda_{31}}, e^{i\lambda_{41}} \right)$$

 $=\begin{pmatrix} c_{12}c_{13}c_{14} & s_{12}c_{13}c_{14} & c_{14}s_{13}e^{-i\delta_{13}} & s_{14}e^{-i\delta_{14}} \\ \dots & \dots & c_{14}s_{24} \\ \dots & \dots & c_{14}c_{24}s_{34}e^{-i\delta_{34}} \\ \dots & \dots & c_{14}c_{24}c_{34} \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & e^{i\lambda_{21}} & 0 & 0 \\ 0 & 0 & e^{i\lambda_{31}} & 0 \\ 0 & 0 & 0 & e^{i\lambda_{41}} \end{pmatrix}$

$$|U_{e4}|^2 = \sin^2 \vartheta_{14} \implies \sin^2 2\vartheta_{ee} = 4|U_{e4}|^2 \left(1 - |U_{e4}|^2\right) = \sin^2 2\vartheta_{14}$$
$$U_{\mu4}|^2 = \cos^2 \vartheta_{14} \sin^2 \vartheta_{24} \simeq \sin^2 \vartheta_{24} \Rightarrow \sin^2 2\vartheta_{\mu\mu} = 4|U_{\mu4}|^2 \left(1 - |U_{\mu4}|^2\right) \simeq \sin^2 2\vartheta_{24}$$

Short-Baseline Reactor Neutrino Oscillations



- $\Delta m_{\rm SBL}^2 \gtrsim 0.5 \, {\rm eV}^2 \gg \Delta m_{\rm ATM}^2$
- SBL oscillations are averaged at the Daya Bay, RENO, and Double Chooz near detectors no spectral distortion
- The reactor antineutrino anomaly is model dependent (depends on the theoretical reactor neutrino flux calculation; is it reliable?).

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Reactor Antineutrino 5 MeV Bump (Shoulder)



- Discovered in 2014 by RENO, Double Chooz, Daya Bay.
- Cannot be explained by neutrino oscillations (SBL oscillations are averaged in RENO, DC, DB).
- If it is due to a theoretical miscalculation of the spectrum, it can have opposite effects on the anomaly:

[see: Berryman, Huber, arXiv:1909.09267]

 If it is a 4-6 MeV excess it increases the anomaly: recent HKSS flux calculation
 [Hayen, Kostensalo, Severijns, Suhonen, arXiv:1908.08302]
 If it is a 1-4 MeV suppression it decreases the anomaly: recent EF flux calculation
 [Estienne, Fallot, et al, arXiv:1904.09358]
 new KI ²³⁵U flux renormalization
 [Kopeikin, Skorokhvatov, Titov, arXiv:2103.01684]

Model Indep. Measurements of Reactor ν Osc.

Ratios of spectra at different distances







DANSS on a lifting platform

Neutrino-4



PROSPECT



STEREO







▶ 2018: remarkable agreement of the DANSS and NEOS best-fit regions at $\Delta m_{41}^2 \approx 1.3 \text{ eV}^2 \implies$ model independent indication in favor of SBL oscillations. [Gariazzo, Giunti, Laveder, Li, arXiv:1801.06467]

[Dentler, Hernandez-Cabezudo, Kopp, Machado, Maltoni, Martinez-Soler, Schwetz, arXiv:1803.10661]

- 2019: decreased agreement between NEOS and DANSS allowed regions. [CG, Y.F. Li, Y.Y. Zhang, arXiv:1912.12956]
- ► 2020: No 2σ DANSS allowed regions (exclusion curve). No compelling indication of oscillations. In practice these reactor experiments exclude large values of $|U_{e4}|^2$ for $0.1 \leq \Delta m_{41}^2 \leq 10 \text{ eV}^2$

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Neutrino-4

[arXiv:1708.00421, arXiv:1809.10561, arXiv:2003.03199, arXiv:2005.05301, arXiv:2006.13639]



Due to some peculiar characteristics of its construction, reactor SM-3 provides the most favorable conditions to search for neutrino oscillations at short distances. However, SM-3 reactor, as well as other research reactors, is located on the Earth's surface, hence, cosmic background is the major difficulty in considered experiment.



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[A. Serebrov, 17 September 2020]



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- Neutrino-4 best fit: $\sin^2 2\vartheta_{ee} = 0.26$ $\Delta m_{41}^2 = 7.25 \text{ eV}^2$
- Very large mixing!
- Not a small perturbation of 3ν mixing.
- Tension with solar neutrino bound.

[Palazzo, arXiv:1105.1705, arXiv:1201.4280] [Giunti, Laveder, Li, Liu, Long, arXiv:1210.5715] [Gariazzo, Giunti, Laveder, Li, arXiv:1703.00860]

Oscillations of Last Neutrino-4 Results

[arXiv:2005.05301]

version	date	$(\Delta m^2_{41})_{\rm bf}$	$(\sin^2 2\vartheta_{ee})_{bf}$	statistical significance
v1	9 May 2020	$\textbf{7.25} \pm \textbf{1.0}$	$\textbf{0.26} \pm \textbf{0.09}$	2.8σ
v2	18 Jun 2020	$\textbf{7.25} \pm \textbf{1.0}$	$\textbf{0.26} \pm \textbf{0.09}$	2.8σ
v3	31 Jul 2020	$\textbf{7.25} \pm \textbf{1.09}$	$\textbf{0.26} \pm \textbf{0.09}$	2.9σ
v4	16 Aug 2020	$\textbf{7.25} \pm \textbf{1.09}$	$\textbf{0.26} \pm \textbf{0.09}$	2.9σ
v5	14 Feb 2021	7.2 ± 1.13	$\textbf{0.29}\pm\textbf{0.12}$	2.4σ
vб	21 Feb 2021	7.2 ± 1.13	$\textbf{0.26} \pm \textbf{0.08}$	3.2σ
v7	5 Apr 2021	7.3 ± 1.17	0.36 ± 0.12	2.9σ

Energy calibration of the full-scale detector

Pu-Be neutron source

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We approximate the energy resolution with the function

$$R(E_{\rm p},E_{\rm p}') = \frac{1}{\sqrt{2\pi}\sigma_{E_{\rm p}}} \exp\left(-\frac{(E_{\rm p}-E_{\rm p}')^2}{2\sigma_{E_{\rm p}}^2}\right) \quad \text{with} \quad \sigma_{E_{\rm p}} = 0.19 \sqrt{\frac{E_{\rm p}}{{\rm MeV}}} \,{\rm MeV}$$

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[CG, Li, Ternes, Zhang, arXiv:2101.06785]

- Disconcerting comment in arXiv:2005.05301v7: The simultaneous usage of energy interval ΔE = 500 keV and energy resolution σ = 250 keV is incorrect, because it includes into the analysis the resolution of the detector twice as it was done in the work [Giunti, Li, Ternes, Zhang, arXiv:2101.06785].
- The Neutrino-4 collaboration thinks that energy binning takes into account the energy resolution.
- It is obvious that an event with an unknown true energy in an unknown energy bin can be counted in another bin because of the energy resolution.
- ► This effect is obviously not taken into account by the binning.
- This effect can be neglected if the energy resolution is much smaller than the bin width.
- This effect cannot be neglected in the Neutrino-4 experiment, where the the bin width is only twice of the energy resolution.

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Neutrino-4: Oscillations or Fluctuations?



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Wilks Theorem (1938)

THE LARGE-SAMPLE DISTRIBUTION OF THE LIKELIHOOD RATIO FOR TESTING COMPOSITE HYPOTHESES¹

BY S. S. WILKS

Let $P_{\Omega}(O_n)$ be the least upper bound of P for the simple hypotheses in Ω , and $P_{\omega}(O_n)$ the least upper bound of P for those in ω . Then

(2)
$$\lambda = \frac{P_{\omega}(O_n)}{P_{\mathfrak{a}}(O_n)}$$

which optimum estimates of the θ 's exist. That is, we shall assume the existence of functions $\tilde{\theta}_i(x_1, \cdots, x_n)$ (maximum likelihood estimates of the θ_i) such that⁴ their distribution is

(3)
$$\frac{|c_{ij}|^{\frac{1}{2}}}{(2\pi)^{h/2}}e^{-\frac{1}{2}\sum_{i,j=1}^{h}c_{ij}z_{i}z_{j}}(1+\phi)\,dz_{1}\cdots dz_{h}$$

where $z_i = (\hat{\theta}_i - \theta_i)\sqrt{n}$, $c_{ij} = -E\left(\frac{\partial^2 \log f}{\partial \theta_i \partial \theta_j}\right)$, E denoting mathematical expectation, and ϕ is of order $1/\sqrt{n}$ and $||c_{ij}||$ is positive definite. Denoting (3) by

Theorem: If a population with a variate x is distributed according to the probability function $f(x, \theta_1, \theta_2 \cdots \theta_h)$, such that optimum estimates $\tilde{\theta}_i$ of the θ_i exist which are distributed in large samples according to (3), then when the hypothesis H is true that $\theta_i = \theta_{0i}$, i = m + 1, m + 2, \cdots h, the distribution of $-2 \log \lambda$, where λ is given by (2) is, except for terms of order $1/\sqrt{n}$, distributed like χ^2 with h - mdegrees of freedom.

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Deviations from χ^2 Distribution (Wilks' Theorem)

[Agostini, Neumair, arXiv:1906.11854; Silaeva, Sinev, arXiv:2001.10752; Giunti, arXiv:2004.07577] [PROSPECT+STEREO, arXiv:2006.13147; Coloma, Huber, Schwetz, arXiv:2008.06083]

Even in the absence of real oscillations, binned data can often be fitted better by oscillations that reproduce the statistical fluctuations of the bins.



Distribution of best-fit points in a large set of random data generated without oscillations

	probability
${ m sin}^2 2artheta_{ee} < 0.1$	0.008
$0.1 < \sin^2 2 \vartheta_{ee} < 0.5$	0.625
$0.5 < \sin^2 2 \vartheta_{ee} < 0.9$	0.184
$\sin^2 2 \vartheta_{ee} > 0.9$	0.183



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Monte Carlo confidence intervals

- For each point on a grid in the (sin²2ϑ_{ee}, Δm²₄₁) plane we generated a large number of random data sets (of the order of 10⁵) with the uncertainties of the Neutrino-4 data set.
- For each random data set:
 - We calculated the value of χ² corresponding to the generating values of sin²2ϑ_{ee} and Δm²₄₁: χ²_{MC}(sin²2ϑ_{ee}, Δm²₄₁).
 - We found the minimum value of χ^2 in the $(\sin^2 2\vartheta_{ee}, \Delta m_{41}^2)$ plane: $\chi^2_{MC,min}(\sin^2 2\vartheta_{ee}, \Delta m_{41}^2)$.
- ► In this way, we obtained the distribution of $\Delta \chi^2_{MC}(\sin^2 2\vartheta_{ee}, \Delta m^2_{41}) = \chi^2_{MC}(\sin^2 2\vartheta_{ee}, \Delta m^2_{41}) \chi^2_{MC,min}(\sin^2 2\vartheta_{ee}, \Delta m^2_{41}).$
- ► This distribution allows us to determine if the value of $\Delta \chi^2(\sin^2 2\vartheta_{ee}, \Delta m_{41}^2) = \chi^2(\sin^2 2\vartheta_{ee}, \Delta m_{41}^2) \chi^2_{\min}(\sin^2 2\vartheta_{ee}, \Delta m_{41}^2)$ obtained with the analysis of the actual Neutrino-4 data is included or not in a region with a fixed confidence level.



	χ^2 dist.	MC dist.
<i>p</i> -value	0.0075	0.028
σ -value	2.7	2.2

[CG, Li, Ternes, Zhang, arXiv:2101.06785]

Conclusion on Neutrino-4: the claimed indication in favor of short-baseline neutrino oscillations with very large mixing is rather doubtful.

Robust kinematical probe of $\nu_e - \nu_s$ mixing



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[Giunti, Y.F. Li, Y.Y. Zhang, arXiv:1912.12956]

 $\Delta m_{41}^2 \simeq m_4^2$

[KATRIN @ Neutrino 2020]

[arXiv:2011.05087]

 $\sin^2 2\vartheta_{ee} = 4|U_{e4}|^2 (1 - |U_{e4}|^2) \simeq 4|U_{e4}|^2 \quad \text{for} \quad |U_{e4}|^2 \ll 1$

3+1: Appearance vs Disappearance

- ► SBL Oscillation parameters: $\Delta m_{41}^2 |U_{e4}|^2 |U_{\mu4}|^2$ ($|U_{\tau4}|^2$)
- Amplitude of v_e disappearance:

$$\sin^2 2\vartheta_{ee} = 4|U_{e4}|^2 \left(1 - |U_{e4}|^2\right) \simeq 4|U_{e4}|^2$$

• Amplitude of ν_{μ} disappearance:

 $\sin^2 2\vartheta_{\mu\mu} = 4|U_{\mu4}|^2 (1 - |U_{\mu4}|^2) \simeq 4|U_{\mu4}|^2$

• Amplitude of $\nu_{\mu} \rightarrow \nu_{e}$ transitions:

 $\sin^{2} 2\vartheta_{e\mu} = 4|U_{e4}|^{2}|U_{\mu4}|^{2} \simeq \frac{1}{4}\sin^{2} 2\vartheta_{ee}\sin^{2} 2\vartheta_{\mu\mu}$ quadratically suppressed for small $|U_{e4}|^{2}$ and $|U_{\mu4}|^{2}$ \downarrow Appearance-Disappearance Tension

[Okada, Yasuda, IJMPA 12 (1997) 3669; Bilenky, CG, Grimus, EPJC 1 (1998) 247]

 $\bar{\nu}_{\mu}
ightarrow \bar{\nu}_{e}$ and $\nu_{\mu}
ightarrow \nu_{e}$ Appearance



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MiniBooNE



- Purpose: check the LSND signal
- Different $L \simeq 540$ m
- Different 200 MeV $\leq E \lesssim$ 3 GeV
- Similar $L/E \implies$ Oscillations Smoking Gun?
- No money, no Near Detector
- Large beam-related background
- Large flux and cross section uncertainties

MiniBooNE



LSND signal?

• LSND: excess only for $\frac{L}{E} \lesssim 1.2 \frac{m}{\text{MeV}}$

 MiniBooNE: the LSND excess should be at

 $E\gtrsim {540\,{
m m}\over 1.2\,{
m m}}\,{
m MeV}\simeq 450\,{
m MeV}$



 $E \lesssim 450 \, {
m MeV}$

MiniBooNE low-energy anomaly

Maybe due to additional $\Delta \rightarrow N\gamma$ background?

[Ioannisian et al, arXiv:1909.08571, arXiv:1912.01524]

To be checked by MicroBooNE@FNAL?

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• The MiniBooNE low-energy excess is at larger L/E than LSND.



[MiniBooNE, PRL 121 (2018) 221801]

ν_{μ} and $\bar{\nu}_{\mu}$ Disappearance



MINOS+



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Global Appearance-Disappearance Tension



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Global Appearance-Disappearance Tension



2016: Global Fit: GoF_{PG} ≈ 6 × 10⁻⁴
2018: Global Fit: GoF_{PG} ≈ 2 × 10⁻⁷ [at 2019: Global Fit: GoF_{PG} ≈ 7 × 10⁻¹¹

[arXiv:1602.01390, arXiv:1606.07673]

[arXiv:1801.06467, arXiv:1803.10661, arXiv:1901.08330]

New Dedicated Experiments



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Conclusions

- Light sterile neutrinos can be powerful messengers of new physics beyond the SM.
- Historically, their existence is motivated by the reactor, Gallium and LSND short-baseline anomalies.
- The reactor antineutrino anomaly, discovered in 2011, is disappearing, because of new neutrino flux calculations and the absence of a clear model-independent signal in the new experiments (DANSS, PROSPECT, STEREO).
- The claimed Neutrino-4 indication in favor of short-baseline neutrino oscillations with very large mixing is rather doubtful.
- Important model-independent tests of the effect of m₄ in β-decay (KATRIN), electron-capture (ECHo, HOLMES) and ββ_{0ν}-decay experiments.

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- ▶ In principle, the simplest explanation of the LSND and MiniBooNE ν_e -like excesses is neutrino oscillations, that requires a new Δm_{SBL}^2 associated with a sterile neutrino.
- Unfortunately, the LSND and MiniBooNE ν_e-like excesses are too large to be compatible with the existing bounds on ν_e and ν_μ disappearance in the framework of 3 + N_s active-sterile neutrino mixing:

APPEARANCE-DISAPPEARANCE TENSION

- Alternative (ad hoc) explanations exist with a heavy sterile neutrino produced and decayed in the detector.
- Promising Fermilab SBN program aimed at a conclusive solution of the mystery with three Liquid Argon Time Projection Chamber (LArTPC): a near detector (LAr1-ND), an intermediate detector (MicroBooNE) and a far detector (ICARUS-T600).
- ▶ It is important that LArTPC detectors can distinguish a single ν_e -induced electron from a γ or a collimated e^+e^- pair.