

# Muon and Electron $g-2$ , Proton and Cesium Weak Charges Implications on Dark $Z_d$ Models

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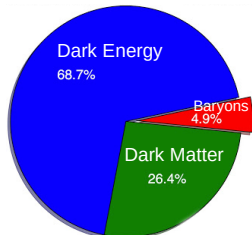
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[arXiv:2104.03280]

# Dark $Z_d$ models

- ▶ It is very likely that the energy of the Universe is composed by:
  - ▶ about 70% of Dark Energy,
  - ▶ about 25% of **non-baryonic Dark Matter**,
  - ▶ about 5% of baryonic matter.
- ▶ Therefore, there is a **Dark Sector** made of unknown particles and interactions.
- ▶ There are many models of all types, many based on new symmetries.
- ▶ A simple and attractive new symmetry (present in many models) is a **broken  $U(1)_d$**  gauge symmetry in the Dark Sector.
- ▶ The associated low-mass gauge boson is called:
  - ▶ **dark photon ( $A'$ )** if it couples only with  $J_{EM}^\mu$  (kinetic mixing with  $F_{\mu\nu}$ );
  - ▶ **dark  $Z$  ( $Z_d$ )** if it couples with  $J_{EM}^\mu$  and  $J_{NC}^\mu$  (in the past:  $Z'$ ,  $U$ ,  $V$ , ...).
- ▶ We consider a  $Z_d$  with **mass between about 10 MeV and 10 GeV**.
- ▶ This  $Z_d$  is a force mediator in the Dark Sector, not the Dark Matter, because it decays very quickly.
- ▶ **Vector Portal:**  $Z_d$  has a rich low-energy phenomenology.



► Low-energy Lagrangian:

$$\mathcal{L} \supset -\frac{1}{4} \widehat{B}_{\mu\nu} \widehat{B}^{\mu\nu} - \frac{1}{4} \widehat{D}_{\mu\nu} \widehat{D}^{\mu\nu} \boxed{-\frac{\sin \eta}{2} \widehat{B}_{\mu\nu} \widehat{D}^{\mu\nu}}$$

kinetic mixing

$$+\frac{1}{2} \widehat{M}_Z^2 \widehat{Z}_\mu \widehat{Z}^\mu + \frac{1}{2} \widehat{M}_D^2 \widehat{D}_\mu \widehat{D}^\mu \boxed{-\delta \widehat{M}_Z \widehat{M}_D \widehat{Z}_\mu \widehat{D}^\mu}$$

mass mixing

$$-e J_{\text{EM}}^\mu \widehat{A}_\mu - \frac{g}{2 \cos \theta_W} J_{\text{NC}}^\mu \widehat{Z}_\mu$$

$$\widehat{B}_{\mu\nu} = \partial_\mu \widehat{B}_\nu - \partial_\nu \widehat{B}_\mu \quad \leftarrow U(1)_Y$$

$$\widehat{D}_{\mu\nu} = \partial_\mu \widehat{D}_\nu - \partial_\nu \widehat{D}_\mu \quad \leftarrow U(1)_d$$

$$\widehat{Z}^\mu = \cos \theta_W W_3^\mu - \sin \theta_W \widehat{B}^\mu \quad g \sin \theta_W = g' \cos \theta_W = e$$

$$\widehat{A}^\mu = \sin \theta_W W_3^\mu + \cos \theta_W \widehat{B}^\mu \quad \leftarrow \text{massless}$$

► Diagonalization of kinetic term:

[see Babu, Kolda, March-Russell, hep-ph/9710441]

$$\widehat{B}_\mu = B_\mu - \tan \eta D_\mu \qquad \widehat{D}_\mu = \frac{1}{\cos \eta} D_\mu$$

$$\begin{aligned} \widehat{Z}^\mu &= \cos \theta_W W_3^\mu - \sin \theta_W B^\mu + \sin \theta_W \tan \eta D^\mu \\ &= \widetilde{Z}^\mu + \sin \theta_W \tan \eta D^\mu \end{aligned}$$

$$\begin{aligned} \widehat{A}^\mu &= \sin \theta_W W_3^\mu + \cos \theta_W B^\mu - \cos \theta_W \tan \eta D^\mu \\ &= A^\mu - \cos \theta_W \tan \eta D^\mu \end{aligned} \quad \leftarrow \text{massless}$$

► Low-energy Lagrangian:

$$\begin{aligned}
 \mathcal{L} \supset & +\frac{1}{2} \widehat{M}_Z^2 \widetilde{Z}_\mu \widetilde{Z}^\mu \\
 & +\frac{1}{2} \left[ \frac{\widehat{M}_D^2}{\cos^2 \eta} + \widehat{M}_Z^2 \sin^2 \theta_W \tan^2 \eta - 2\delta \widehat{M}_Z \widehat{M}_D \sin \theta_W \frac{\tan \eta}{\cos \eta} \right] D_\mu D^\mu \\
 & + \left[ \widehat{M}_Z^2 \sin \theta_W \tan \eta - \delta \frac{\widehat{M}_Z \widehat{M}_D}{\cos \eta} \right] \widetilde{Z}_\mu D^\mu \quad \text{mass mixing} \\
 & -e J_{EM}^\mu A_\mu \\
 & +e \cos \theta_W \tan \eta J_{EM}^\mu D_\mu \\
 & -\frac{g}{2 \cos \theta_W} J_{NC}^\mu \widetilde{Z}_\mu \\
 & -\frac{g}{2 \cos \theta_W} \sin \theta_W \tan \eta J_{NC}^\mu D_\mu
 \end{aligned}$$

► Diagonalization of mass term:

[see Babu, Kolda, March-Russell, hep-ph/9710441]

$$\begin{pmatrix} \tilde{Z}^\mu \\ D^\mu \end{pmatrix} = \begin{pmatrix} \cos \xi & -\sin \xi \\ \sin \xi & \cos \xi \end{pmatrix} \begin{pmatrix} Z^\mu \\ Z_d^\mu \end{pmatrix}$$

$$\tan 2\xi = \frac{-2 \cos \eta \left( \hat{M}_Z^2 \sin \theta_W \sin \eta - \delta \hat{M}_Z \hat{M}_D \right)}{\hat{M}_D^2 + \hat{M}_Z^2 (\sin^2 \theta_W \sin^2 \eta - \cos^2 \eta) - 2\delta \hat{M}_Z \hat{M}_D \sin \theta_W \sin \eta}$$

$$\hat{M}_Z^2 = m_Z^2 \left[ 1 - \sin^2 \xi \left( 1 - \frac{m_{Z_d}}{m_Z} \right) \right]$$

$$\text{► } \sin \eta, \delta \ll 1 \quad \Longrightarrow \quad \sin \xi \simeq \frac{m_Z^2 \sin \theta_W \sin \eta - \delta m_Z m_{Z_d}}{m_Z^2 - m_{Z_d}^2}$$

$$m_Z^2 \simeq \hat{M}_Z^2 \left[ 1 + \sin^2 \xi \left( 1 - \frac{\hat{M}_D}{\hat{M}_Z} \right) \right]$$

$$m_{Z_d}^2 \simeq \hat{M}_D^2 \left[ 1 + \sin^2 \xi \left( 1 - \frac{\hat{M}_Z}{\hat{M}_D} \right) + \sin^2 \eta \left( 1 + \sin^2 \theta_W \frac{\hat{M}_Z}{\hat{M}_D} \right) - 2\delta \sin \xi \sin \theta_W \frac{m_Z}{m_{Z_d}} \right]$$

► Low-energy Lagrangian:

$$\begin{aligned}
 \mathcal{L} \supset & -\frac{1}{4} B_{\mu\nu} B^{\mu\nu} - \frac{1}{4} D_{\mu\nu} D^{\mu\nu} + \frac{1}{2} m_Z^2 Z_\mu Z^\mu + \frac{1}{2} m_{Z_d}^2 Z_{d\mu} Z_d^\mu - e J_{\text{EM}}^\mu A_\mu \\
 & - \frac{g}{2 \cos \theta_W} (\cos \xi + \sin \theta_W \tan \eta \sin \xi) J_{\text{NC}}^\mu Z_\mu \\
 & + e \cos \theta_W \tan \eta \sin \xi J_{\text{EM}}^\mu Z_\mu \quad \leftarrow \text{quadratically suppressed} \\
 & + e \cos \theta_W \tan \eta \cos \xi J_{\text{EM}}^\mu Z_{d\mu} \quad \leftarrow Z_d \text{ EM interactions} \\
 & - \frac{g}{2 \cos \theta_W} (\sin \theta_W \tan \eta \cos \xi - \sin \xi) J_{\text{NC}}^\mu Z_{d\mu} \quad \leftarrow Z_d \text{ NC interactions}
 \end{aligned}$$

- ▶ Common convenient definition:

$$\mathcal{L}_{Z_d}^{\text{EM}} = -e \varepsilon J_{\text{EM}}^\mu Z_{d\mu} \implies \tan \eta \cos \xi = -\frac{\varepsilon}{\cos \theta_W}$$

- ▶ Neutral-Current interaction:

$$\mathcal{L}_{Z_d}^{\text{NC}} = -\frac{g}{2 \cos \theta_W} (-\varepsilon \tan \theta_W - \sin \xi) J_{\text{NC}}^\mu Z_{d\mu}$$

- ▶  $\sin \eta, \delta \ll 1 \implies \sin \eta \simeq -\frac{\varepsilon}{\cos \theta_W} \implies \sin \xi \simeq -\frac{m_Z^2 \tan \theta_W \varepsilon + \delta m_Z m_{Z_d}}{m_Z^2 - m_{Z_d}^2}$

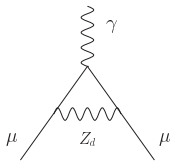
$$\mathcal{L}_{Z_d}^{\text{NC}} = -\frac{g}{2 \cos \theta_W} \frac{m_{Z_d}}{m_Z} \delta' J_{\text{NC}}^\mu Z_{d\mu}$$

with  $\delta' \simeq \left( \delta + \frac{m_{Z_d}}{m_Z} \varepsilon \tan \theta_W \right) \left( 1 - \frac{m_{Z_d}^2}{m_Z^2} \right)^{-1}$

- ▶  $m_{Z_d} \ll m_Z \implies \delta' \simeq \delta + \frac{m_{Z_d}}{m_Z} \varepsilon \tan \theta_W$  [Davoudiasl, Lee, Marciano, arXiv:1507.00352]



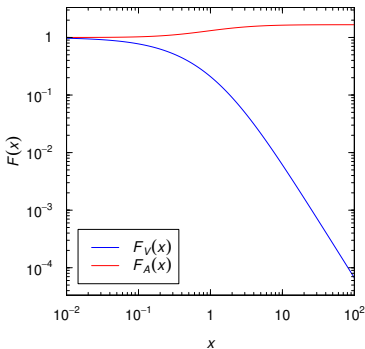
# Anomalous Magnetic Moments of Charged Leptons



$$a_{\ell,V}^{Z_d} = \frac{\alpha}{2\pi} \left( \varepsilon + \frac{m_{Z_d}}{m_Z} \delta' \frac{1 - 4 \sin^2 \theta_W}{4 \sin \theta_W \cos \theta_W} \right)^2 F_V \left( \frac{m_{Z_d}}{m_\ell} \right)$$

$$a_{\ell,A}^{Z_d} = -\frac{G_F m_\ell^2}{8\sqrt{2}\pi^2} \delta'^2 F_A \left( \frac{m_{Z_d}}{m_\ell} \right) \quad \ell = e, \mu$$

[Boehm, Fayet, hep-ph/0305261; Pospelov, arXiv:0811.1030; Davoudiasl, Lee, Marciano, arXiv:1205.2709]



▶  $m_{Z_d} \ll m_Z \implies \delta'$  contribution to  $a_{\ell,V}^{Z_d}$  is negligible

▶  $a_{\ell,V}^{Z_d}$  is suppressed for  $m_{Z_d} \gg m_\ell$

▶  $a_{\ell,A}^{Z_d}$  is negligible:

$$\frac{G_F m_\ell^2}{8\sqrt{2}\pi^2} \simeq 1.2 \times 10^{-9} \ll \frac{\alpha}{2\pi} \simeq 1.2 \times 10^{-3}$$

▶ Electron Anomalous Magnetic Moment:

[Hanneke, Fogwell, Gabrielse, arXiv:0801.1134]  
[LKB20, Nature 588 (2020) 7836]

$$\Delta a_e^{\text{Rb}} = a_e^{\text{exp}} - a_e^{\text{Rb}} = 0.48(30) \times 10^{-12}$$

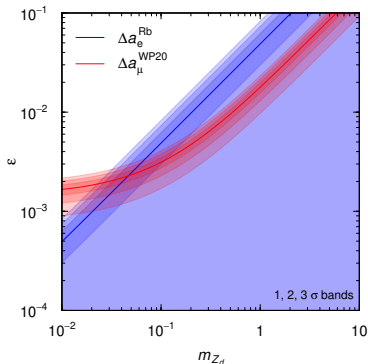
(1.6  $\sigma$ )

▶ Muon Anomalous Magnetic Moment:

[WP20, arXiv:2006.04822]  
[FNAL Muon g-2, arXiv:2104.03281]

$$\Delta a_\mu^{\text{WP20}} = a_\mu^{\text{exp}} - a_\mu^{\text{WP20}} = 251(59) \times 10^{-11}$$

(4.2  $\sigma$ )



▶ Positive deviations from SM can be explained by positive  $a_{\ell, \nu}^{Z_d}$ .

▶ Note that negative

[Berkeley, arXiv:1812.04130]

$$\Delta a_e^{\text{Cs}} = -0.88(36) \times 10^{-12}$$

cannot be explained by positive  $a_{e, \nu}^{Z_d}$ .

# $Z_d$ Neutral Current Interactions

At low  $Q^2$  momentum transfer:

[Davoudiasl, Lee, Marciano, arXiv:1507.00352]

▶  $G_F \rightarrow \rho_d G_F$  with  $\rho_d = 1 + \delta'^2 f\left(\frac{Q^2}{m_{Z_d}^2}\right)$

$$= 1 + \left(\delta + \frac{m_{Z_d}}{m_Z} \varepsilon \tan \theta_W\right)^2 f\left(\frac{Q^2}{m_{Z_d}^2}\right)$$

▶  $\sin^2 \theta_W(Q^2) \rightarrow \kappa_d \sin^2 \theta_W(Q^2)$  with

$$\kappa_d = 1 - \varepsilon \delta' \frac{m_{Z_d}}{m_Z} \cot \theta_W f\left(\frac{Q^2}{m_{Z_d}^2}\right)$$

$$= 1 - \varepsilon \left(\delta + \frac{m_{Z_d}}{m_Z} \varepsilon \tan \theta_W\right) \frac{m_Z}{m_{Z_d}} \cot \theta_W f\left(\frac{Q^2}{m_{Z_d}^2}\right)$$

$$\simeq 1 - \varepsilon \delta \frac{m_Z}{m_{Z_d}} \cot \theta_W f\left(\frac{Q^2}{m_{Z_d}^2}\right) \leftarrow \text{dominant for } m_{Z_d} \ll m_Z$$

We consider the **low-energy** Neutral Current measurements:

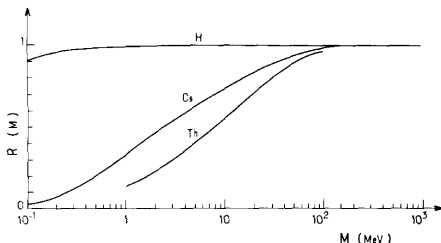
- ▶  $Q_{\text{weak}}$  measurement of **proton** weak charge  $Q_W^p$  at  $Q^2 = (157 \text{ MeV})^2$ :

$$f\left(\frac{Q^2}{m_{Z_d}^2}\right) = \frac{m_{Z_d}^2}{m_{Z_d}^2 + Q^2} \rightarrow \begin{cases} 1 & \text{for } m_{Z_d}^2 \gg Q^2 \\ 0 & \text{for } m_{Z_d}^2 \ll Q^2 \end{cases}$$

- ▶ **APV** (Atomic Parity Violation) measurement of the  $^{133}\text{Cs}$  weak charge  $Q_W^{133\text{Cs}}$  at  $Q^2 \approx (2.4 \text{ MeV})^2$ :

$$f\left(\frac{Q^2}{m_{Z_d}^2}\right) = R(m_{Z_d})$$

nuclear structure effect



[Bouchiat, Piketty, PLB 128 (1983) 73]  
[see also Bouchiat, Fayet, hep-ph/0410260]

- ▶ Then, the dominant effect of  $\kappa_d$  to  $\sin^2 \theta_W(Q^2)$  is maximal at

$$m_{Z_d}^2 \simeq Q^2$$

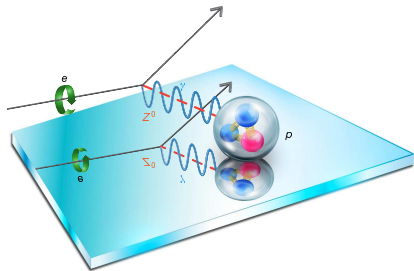
# $Q_{\text{weak}}$ Proton Weak Charge Measurement

[arXiv:1905.08283]

Parity-violating asymmetry in the scattering of polarized electrons on protons:

$$A_{ep} = \frac{\sigma_+ - \sigma_-}{\sigma_+ + \sigma_-} \approx -\frac{G_F Q^2}{4\sqrt{2}\pi\alpha} Q_W^p$$

$$Q_W^{p,\text{exp}} = 0.0719 (45)$$



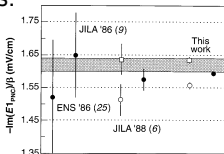
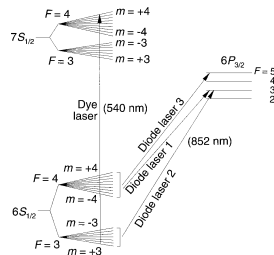
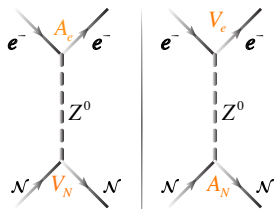
$$Q_W^{p,\text{SM}} = -2 g_{AV}^{ep}(\sin^2 \theta_W) \left(1 - \frac{\alpha}{2\pi}\right) = 0.0711 (2)$$

$$g_{AV}^{ep}(\sin^2 \theta_W) = -0.0357 \approx -\frac{1}{2} + 2 \sin^2 \theta_W$$

$$Q_W^{p,Z_d} = -2 \rho_d g_{AV}^{ep}(\kappa_d \sin^2 \theta_W) \left(1 - \frac{\alpha}{2\pi}\right)$$

# Atomic Parity Violation

- ▶ Amplitude of the **Parity Non-Conserving (PNC)** transition between the 6S and 7S states of **Cesium**.
- ▶ **Why Cesium?** The atomic structure is the most accurately known (1%): a single valence electron outside of a tightly bound Xe-like inner core.
- ▶ Electric-dipole (E1) transitions are forbidden between the equal-parity 6S and 7S states.
- ▶ Parity-violating NC electron-nucleus interactions generate a very small ( $\sim 10^{-11}$ ) admixture of states with opposite parity: 6P states mix with 6S and with 7S states, leading to very small E1 transitions.



$$\frac{\text{Im}E_{\text{PNC}}}{\beta} = -21.5935(56) \text{ mV/cm}$$

[Boulder, Wood et al, Science 275 (1997) 1759]

$\beta$ : Stark vector transition polarizability

$$Q_W^{133\text{Cs,exp}} = N_{133\text{Cs}} \left( \frac{\text{Im}E_{\text{PNC}}}{\beta} \right)_{\text{exp}} \left( \frac{Q_W^{133\text{Cs}}}{N_{133\text{Cs}} \text{Im}E_{\text{PNC}}(R_n)} \right)_{\text{th}} \beta_{\text{exp+th}}$$

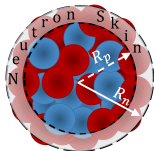
$N_{133\text{Cs}} = 78$  neutron number of  $^{133}\text{Cs}$

$$\left. \begin{aligned} \left( \frac{\text{Im}E_{\text{PNC}}}{\beta} \right)_{\text{exp}} &= -1.5924 \pm 0.0055 \text{ mV/cm} \\ &= (-3.0967 \pm 0.0107) \times 10^{-13} e/a_B^2 \\ &\quad \text{[Boulder + physics/0412017]} \\ \beta_{\text{exp+th}} &= (27.064 \pm 0.033) a_B^3 \\ &\quad \text{[hep-ph/0204134 + 1905.02768]} \end{aligned} \right\} \text{[PDG 2020]}$$

Without neutron skin of  $^{133}\text{Cs}$  (i.e.  $R_n = R_p$ ):

$$\left( \frac{N_{133\text{Cs}} \text{Im}E_{\text{PNC}}(R_n)}{Q_W^{133\text{Cs}}} \right)_{\text{th}}^{\text{w.n.s.}} = (0.8995 \pm 0.0040) \times 10^{-11} e a_B$$

[Dzuba, Berengut, Flambaum, Roberts, arXiv:1207.5864]



▶ Neutron skin:  $\Delta R_{np} \equiv R_n - R_p$ .

▶ Previous determinations of  $Q_W^{133\text{Cs,exp}}$  used the value of  $\Delta R_{np}(^{133}\text{Cs})$  given by the empirical relation obtained from the fit of hadronic measurements:

$$\Delta R_{np}^{\text{had}} = (-0.04 \pm 0.03) + (1.01 \pm 0.15) \frac{N - Z}{A} \text{ fm}$$

▶ This gives  $\Delta R_{np}^{\text{had}}(^{133}\text{Cs}) = 0.13 \pm 0.04 \text{ fm}$

▶  $R_p(^{133}\text{Cs}) = 4.807 \pm 0.001 \text{ fm} \implies R_n^{\text{had}}(^{133}\text{Cs}) = 4.94 \pm 0.04 \text{ fm}$

▶ This hadronic determination of  $\Delta R_{np}$  is affected by considerable model dependencies and uncontrolled approximations

[see: Thiel, Sfienti, Piekarewicz, Horowitz, Vanderhaeghen, arXiv:1904.12269]

▶ This determination of  $R_n(^{133}\text{Cs})$  gives  $Q_W^{133\text{Cs,exp}} = -72.82 \pm 0.42$

[PDG 2020]





$$Q_W^{133\text{Cs,exp}} = -72.94 \pm 0.43$$

$$Q_W^{133\text{Cs,SM}} = -2 \left[ Z_{133\text{Cs}} (g_{AV}^{ep}(\sin^2 \theta_W) + 0.00005) \right. \\ \left. + N_{133\text{Cs}} (g_{AV}^{en} + 0.00006) \right] \left( 1 - \frac{\alpha}{2\pi} \right)$$

$$Z_{133\text{Cs}} = 55 \quad g_{AV}^{ep}(\sin^2 \theta_W) = -0.0357 \approx -\frac{1}{2} + 2 \sin^2 \theta_W$$

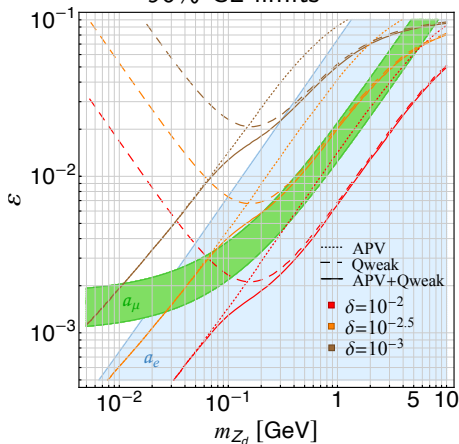
$$N_{133\text{Cs}} = 78 \quad g_{AV}^{en} = 0.495 \approx \frac{1}{2}$$

$$Q_W^{133\text{Cs,SM}} = -73.23 \pm 0.01$$

[PDG 2020]

$$Q_W^{133\text{Cs,Z}_d} = -2 \rho_d \left[ Z_{133\text{Cs}} (g_{AV}^{ep}(\kappa_d \sin^2 \theta_W) + 0.00005) \right. \\ \left. + N_{133\text{Cs}} (g_{AV}^{en} + 0.00006) \right] \left( 1 - \frac{\alpha}{2\pi} \right)$$

### 90% CL limits



$$\blacktriangleright \chi_i^2 = \frac{[X_i^{\text{exp}} - X_i^{\text{th}}(\varepsilon, \delta, m_{Z_d})]^2}{\sigma_i^2}$$

$$X_i^{\text{exp}} = a_\mu^{\text{exp}}, a_e^{\text{exp}}, Q_W^{p,\text{exp}}, Q_W^{133\text{Cs},\text{exp}}$$

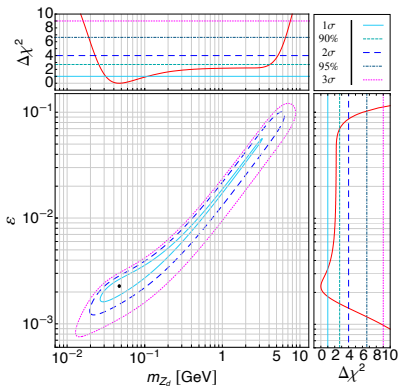
$$X_i^{\text{th}} = a_\mu^{Z_d}, a_e^{Z_d}, Q_W^{p,Z_d}, Q_W^{133\text{Cs},Z_d}$$

$$\blacktriangleright Q^2(Q_{\text{weak}}) = (157 \text{ MeV})^2$$

$$Q^2(\text{APV}) \approx (2.4 \text{ MeV})^2$$

$\blacktriangleright$   $Q_{\text{weak}}$  and APV constraints depend strongly on  $\delta$

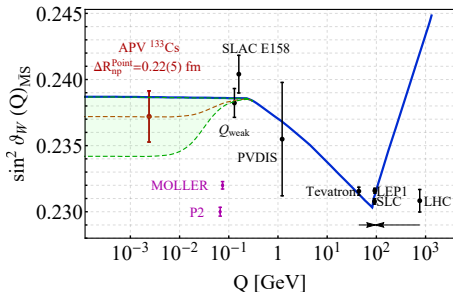
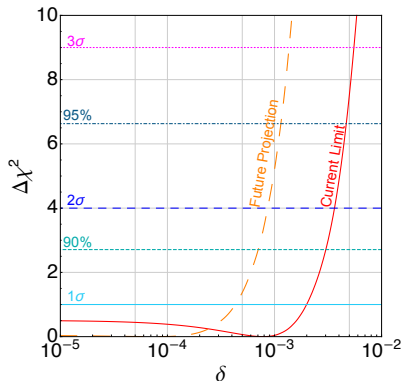
$\blacktriangleright$  For  $\delta > 10^{-2}$  the  $Z_d$  explanation of  $a_\mu^{\text{exp}}$  is disfavored by APV and more strongly by  $Q_{\text{weak}} + \text{APV}$



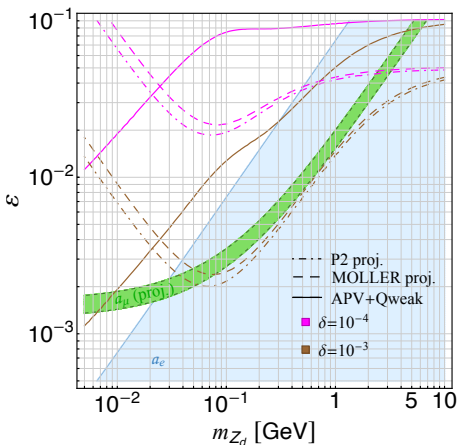
$$m_{Z_d} = 47_{-16}^{+61} \text{ MeV}$$

$$\epsilon = 2.3_{-0.4}^{+1.1} \times 10^{-3}$$

$$\delta < 2 \times 10^{-3}$$



## Future prospects



- **MOLLER@JLab**: Measurement Of a Lepton Lepton Electroweak Reaction

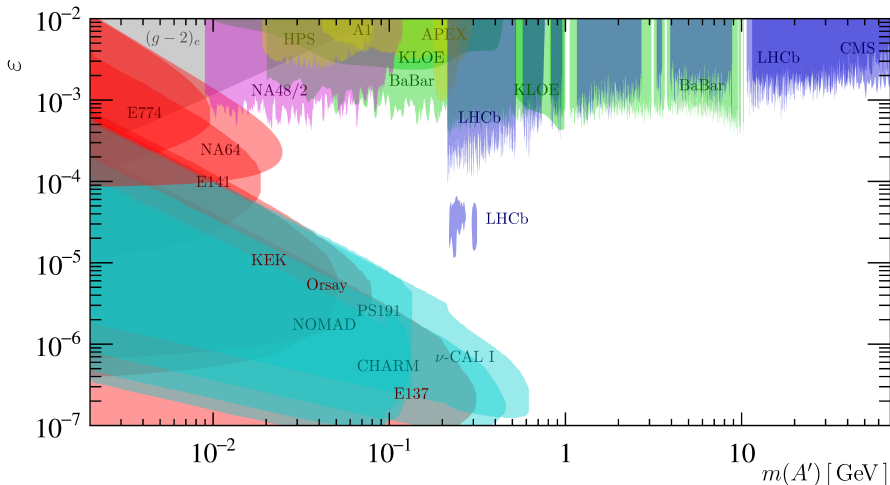
[arXiv:1411.4088]

Precise measurement ( $\approx \pm 3 \times 10^{-4}$ ) of  $\sin^2 \theta_W$  at  $Q^2 \approx (70 \text{ MeV})^2$  with parity-violating asymmetry in polarized **electron-electron** (Møller) scattering ( $Q_W^e$ )

- **P2@MESA** (Mainz): [arXiv:1802.04759]

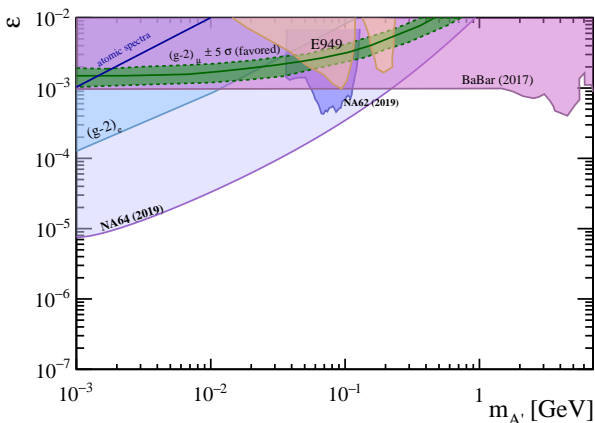
Precise measurement ( $\approx \pm 3 \times 10^{-4}$ ) of  $\sin^2 \theta_W$  at  $Q^2 \approx (70 \text{ MeV})^2$  with parity-violating asymmetry in polarized **electron-proton** scattering ( $Q_W^p$ )

# Dark Photon Constraints



Constraints on **visible**  $A'$  decays from **electron beam dumps**, **proton beam dumps**,  $e^+e^-$  colliders,  $pp$  collisions, meson decays, and **electron on fixed target** experiments.

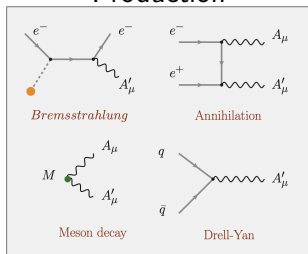
[Graham, Hearty, Williams, arXiv:2104.10280, adapted from Ilten, Soreq, Williams, Xue, arXiv:1801.04847]



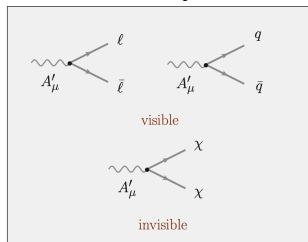
## Constraints on invisible $A'$ decays

[Fabbrichesi, Gabrielli, Lanfranchi, arXiv:2005.01515]

## Production

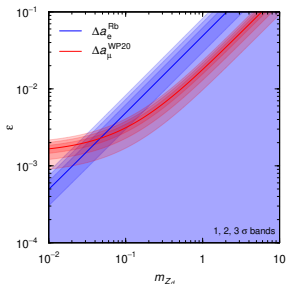


## Decay

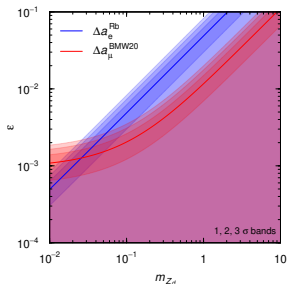


# $(g-2)_\mu$ What Ifs

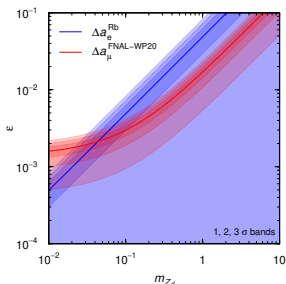
Standard FNAL+BNL – WP20



FNAL+BNL – BMW20



FNAL – WP20



$$\Delta a_\mu^{\text{WP20}} = 251 \pm 59 \quad (4.2\sigma)$$

$$\Delta a_\mu^{\text{BMW20}} = 107 \pm 69 \quad (1.6\sigma)$$

$$\Delta a_\mu^{\text{FNAL-WP20}} = 230 \pm 69 \quad (3.3\sigma)$$

[WP20, arXiv:2006.04822]

[FNAL Muon  $g-2$ , arXiv:2104.03281]

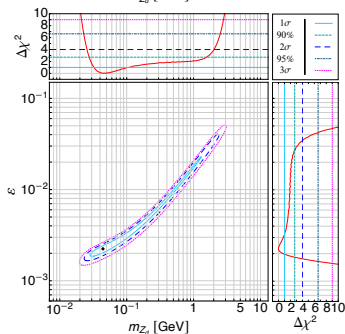
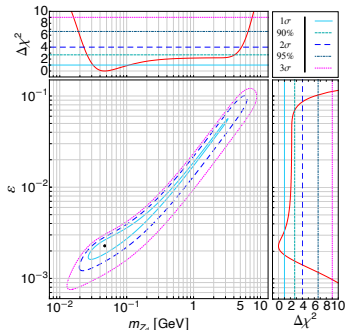
[BMW20, Borsanyi et al, arXiv:2002.12347]



# Conclusions

- ▶ A light **Dark  $Z_d$**  is an attractive Vector Portal to the Dark Sector.
- ▶  $Z_d$  couples with the EM current  $J_{EM}^\mu$  and the weak NC  $J_{NC}^\mu$
- ▶ 3 parameters:  $\varepsilon$  (kinetic mixing),  $\delta$  (mass mixing), and  $m_{Z_d}$
- ▶  $Z_d$  effects are observable in low- $Q^2$  processes
- ▶  $Z_d$  can explain positive **lepton  $g - 2$  anomalies**
- ▶ We considered the low-energy NC constraints from
  - ▶  $Q_{\text{weak}}$  measurement of **proton** weak charge  $Q_W^p$  at  $Q^2 = (157 \text{ MeV})^2$
  - ▶ APV measurement of the  **$^{133}\text{Cs}$**  weak charge  $Q_W^{^{133}\text{Cs}}$  at  $Q^2 = (157 \text{ MeV})^2$
- ▶ We found a preferred region at
$$m_{Z_d} = 47_{-16}^{+61} \text{ MeV}, \quad \varepsilon = 2.3_{-0.4}^{+1.1} \times 10^{-3}, \quad \delta < 2 \times 10^{-3}$$
- ▶ Dark-photon-like constraints from other experiments need further study.

## Extra Slides



- **Present:** combined fit of  $Q_{\text{weak}}$ , APV,  $a_e$ , and  $a_\mu$  experimental results:

$$m_{Z_d} = 47_{-16}^{+61} \text{ MeV}$$

$$\epsilon = 2.3_{-0.4}^{+1.1} \times 10^{-3}$$

$$\delta < 2 \times 10^{-3}$$

- **Future:** combined fit of  $Q_{\text{weak}}$ , APV, and  $a_e$  experimental results, the projections for P2 and MOLLER, and future  $a_\mu$  expected sensitivity:

$$m_{Z_d} = 44_{-12}^{+63} \text{ MeV}$$

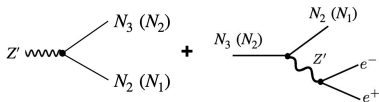
$$\epsilon = 2.2_{-0.3}^{+1.0} \times 10^{-3}$$

$$\delta < 4 \times 10^{-4}$$

# Revised constraints on semi-visible DP

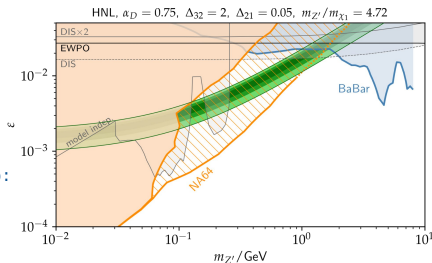
## Scenario 3: Heavy Neutral Leptons ( $Z' \rightarrow N_1 N_2$ AND $Z' \rightarrow N_3 N_2$ )

AA, M.Hostert, S.Pascoli  
arXiv: 2007.11813



Pair of dark fermions + 1 sterile neutrino:

- 1) **Approximate  $L \leftrightarrow R$  symmetry** suppresses diagonal couplings
- 2) Compatible with light neutrino masses
- 3) Possible solution to other anomalies (e.g. MiniBooNe)



**Possibility of opening up large regions of  $(g-2)$  parameter space!**

**Note: subject to NA64 analysis efficiencies**

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[Asli M. Abdullahi @ Invisibles21 Workshop]

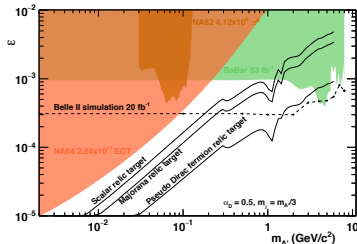
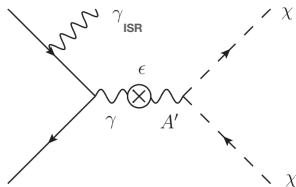
# Dark Photon at Belle II

## What?

- Dark sector mediator which couples to SM photon

## How?

- Belle II looks into  $e^+e^- \rightarrow \gamma_{ISR} A'$ ;  $A' \rightarrow \chi\chi$
- Final state: Single  $\gamma$  + Missing Energy
- $m_{A'}^2 = 4E_{beam}^* (E_{beam}^* - E_{\gamma_{ISR}}^*)$ ; Easy to find  $A'$  mass
- Newly designed trigger allows sensitivity down to 0.5 GeV of single photon

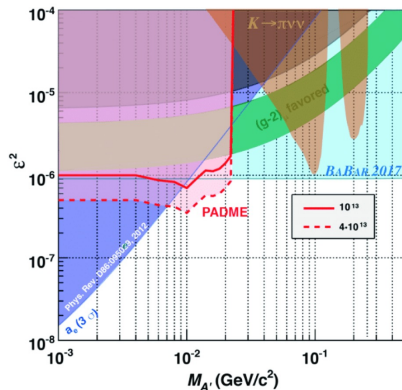


Based on M. Graham, C. Hearty, M. Williams, *Annu. Rev. Nucl. Part. Sci.* 2021, 71:37



## Physics goals

- Dark photons:  $e^+e^- \rightarrow \gamma A'$ 
  - Final states:
    - Visible  $A' \rightarrow e^+e^-$
    - Invisible  $A' \rightarrow \chi\chi$



[Elizabeth Long @ Invisibles21 Workshop]