



# Misura di $J/\psi$ nello Spettrometro per Muoni in p-p

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**Quinto Convegno Nazionale  
sulla Fisica di ALICE**

**Trieste 12-14 September 2009**

# Outlook

Physics motivations for  $J/\psi$  study in p-p

The ALICE Muon Spectrometer

First  $J/\psi$  paper analysis

The polarization issue

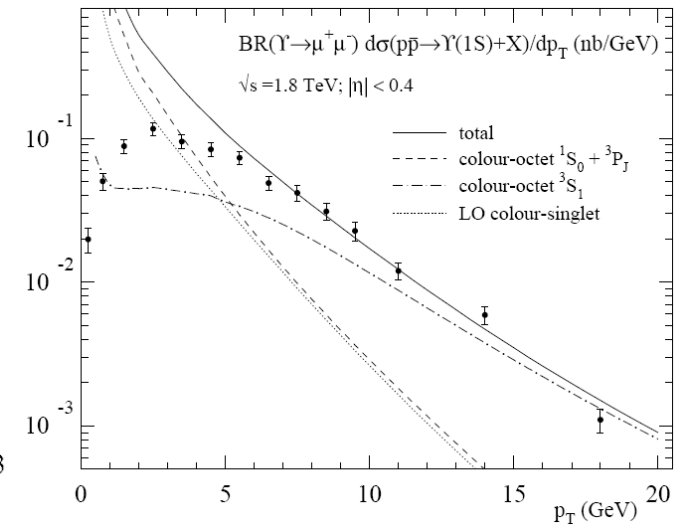
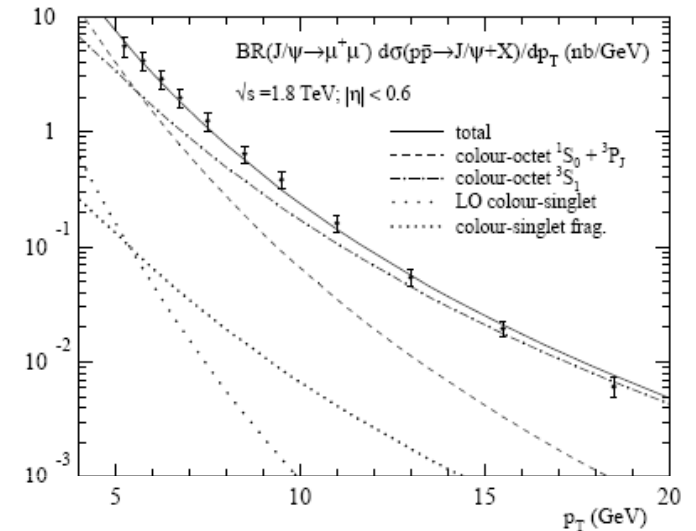
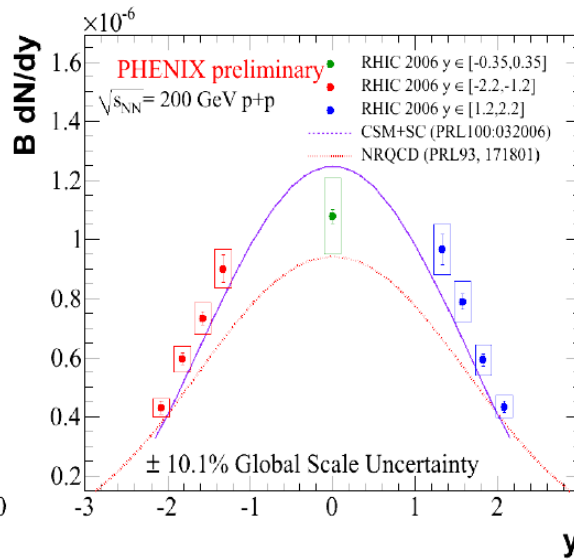
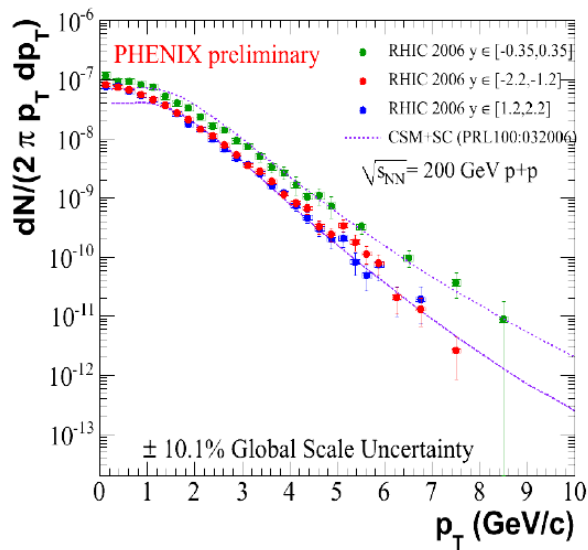
Conclusions and Ongoings

# J/ψ in pp: physics motivations (I)

Need to understand the production mechanism.

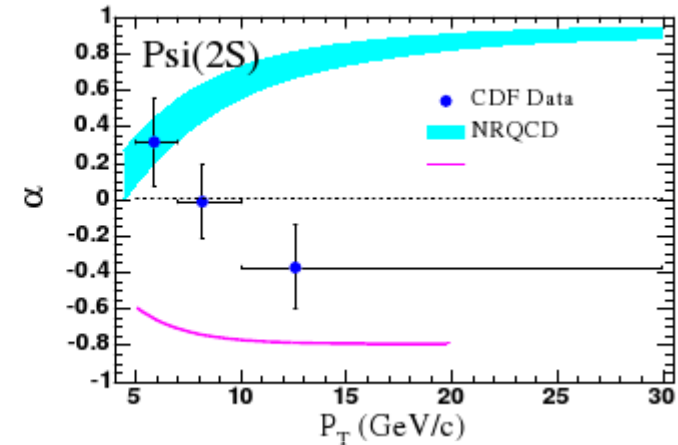
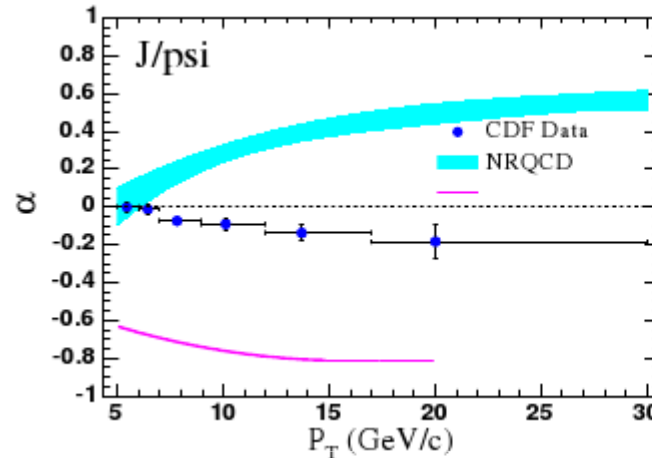
Several models:

- **CEM**: phenomenological, not so predictive;
- **CSM**: bad x-sect. Fit (ruled out in the '90s);
- **COM (NRQCD)**: good x-sect. fit for all quarkonia;
- **CSM + s-channel cut**: describes polarization data.

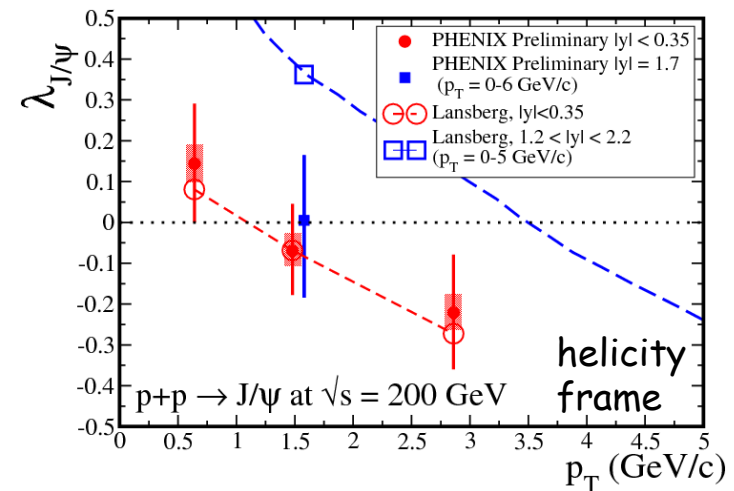


# J/ψ in pp: physics motivations (II)

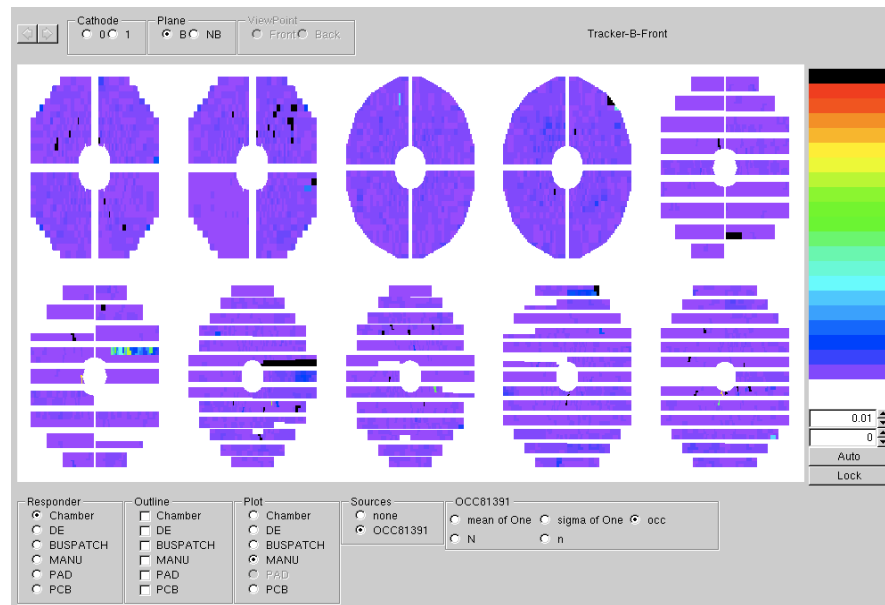
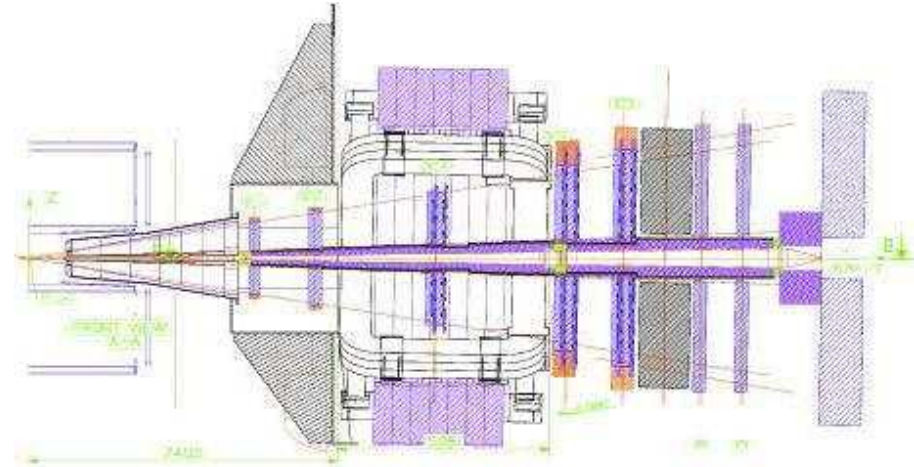
NRQCD fails in predicting polarization at high  $P_T$



CSM+ s-channel cut (NNLO perturbative calculation): describes polarization data from PHENIX at mid-rapidity. Still problems at forward rapidity.

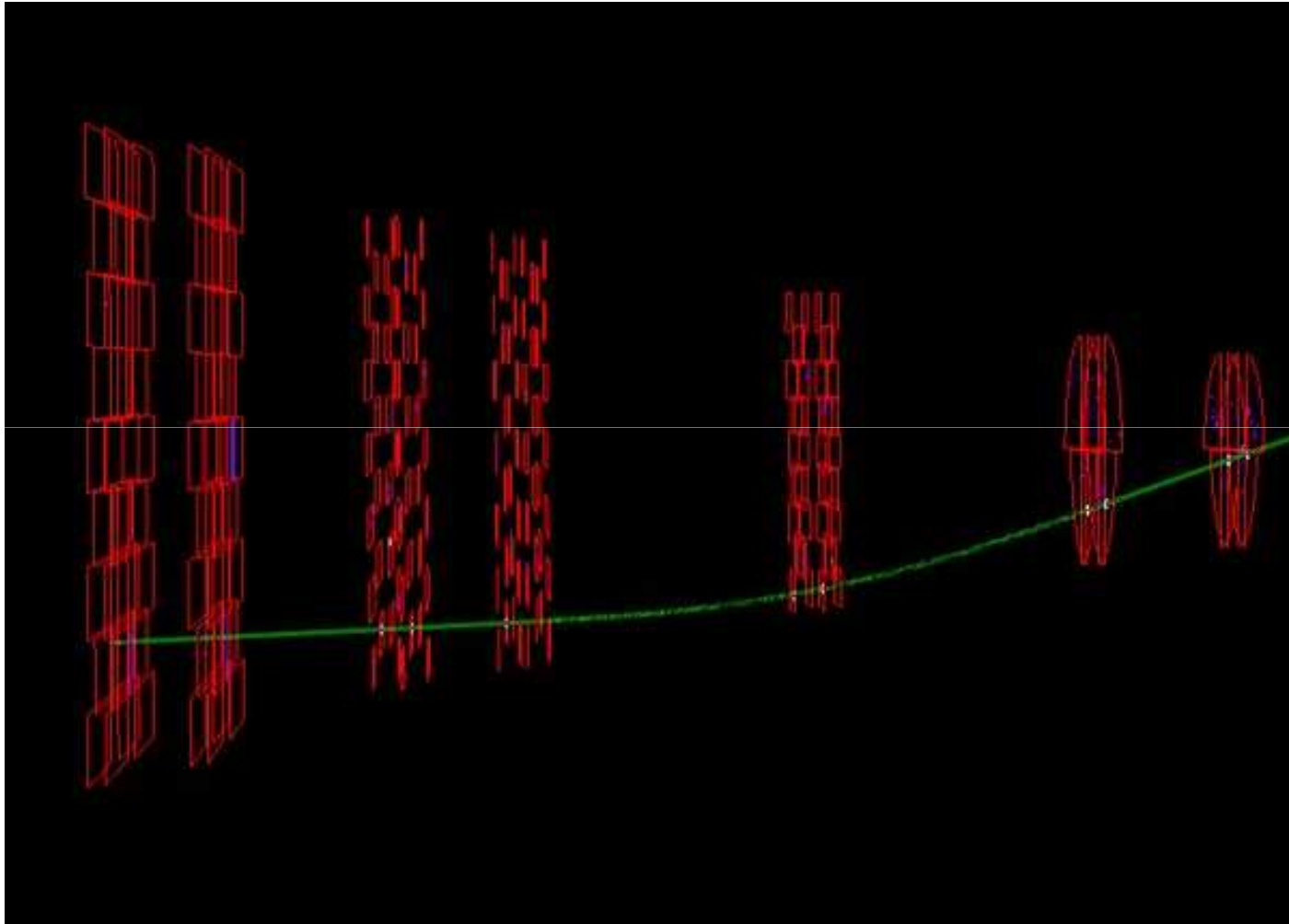


# Muon Spectrometer: Setup



- Front absorber
  - Beam Shield
    - Dipole magnet ( $\int B dl = 3 \text{ Tm}$ )
      - 5 tracking stations (MWPCs with bi-cathode pad readout): spatial resolution below  $100 \mu\text{m}$  in the bending plane, around  $700 \mu\text{m}$  in the non-bending plane
        - Iron wall (muon filter)
- 2 trigger stations (4 planes of RPCs): fast response ( $\sim 2 \text{ ns}$ ), spatial resolution  $\sim 1 \text{ cm}$

# Muon Spectrometer: cosmic run



First curved  
cosmic muon  
event (tracked and  
triggered)

Nice view!

But we expect  
more than 90  
couples of this  
tracks per hour  
coming from  $J/\psi$ s  
during the first  
run of LHC...!\*

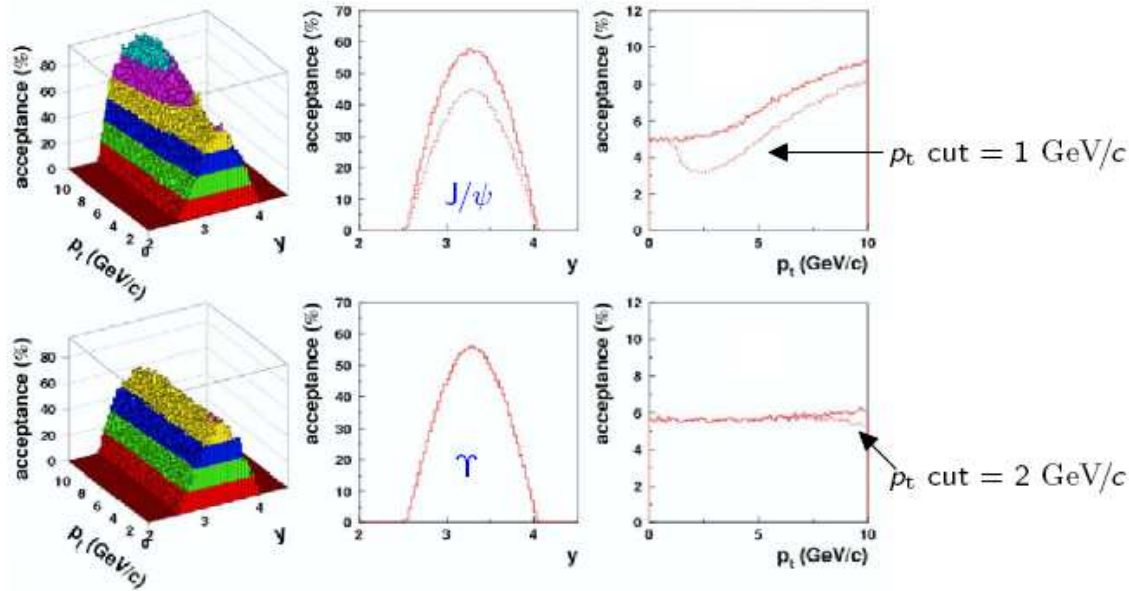
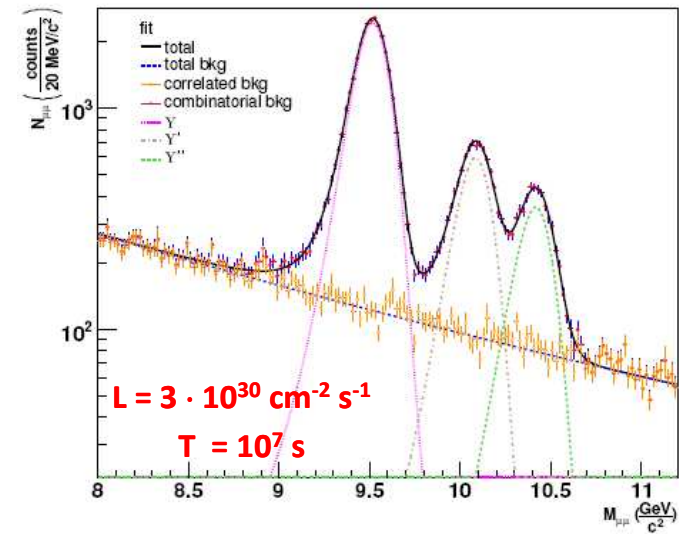
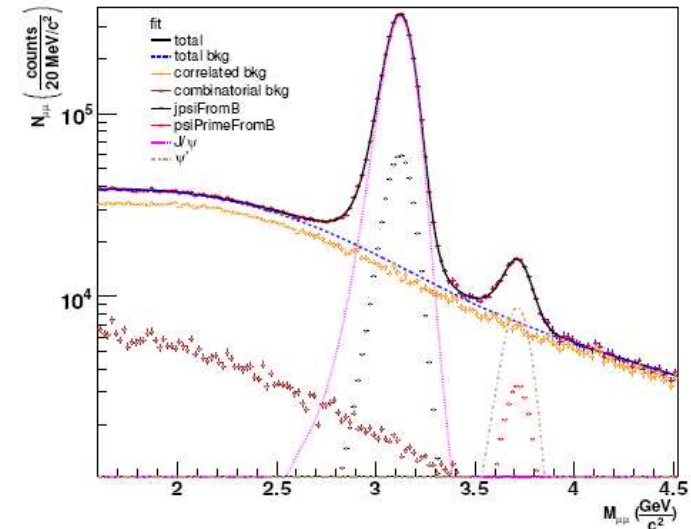
\*actually this number refers to the trigger rate.

# Muon Spectrometer: performances in pp

state	S ( $\times 10^3$ )	B ( $\times 10^3$ )	S/B	$S/\sqrt{S+B}$
J/ $\psi$	2807	235	12.0	1610
$\psi'$	75	120	0.62	170
$\Upsilon$	27.1	2.6	10.4	157
$\Upsilon'$	6.8	2.0	3.4	73
$\Upsilon''$	4.2	1.8	2.4	55

ALICE-INT-2006-029

Mass resolution:  
70 MeV for the J/ $\psi$ , 100 MeV for the  $\Upsilon$





# First Analysis

Assuming  $340 \cdot 10^{-3}$  Hz  $J/\psi$  trigger rate low  $p_T$  at  $L=3 \cdot 10^{30}$   $\text{cm}^{-2} \text{s}^{-1}$  (ALICE-INT-2006-0002), at  $L=2.3 \cdot 10^{29}$   $\text{cm}^{-2} \text{s}^{-1}$  we expect:  $J/\psi$  trigger rate  $\sim 26 \cdot 10^{-3}$  Hz

Assuming 12% running efficiency (F. Antinori - Physics Forum July 2009) we expect from  $10^4$  to  $4 \cdot 10^4$   $J/\psi$ s in the first 5 months

For  $10^4$   $J/\psi$ s we expect 100  $J/\psi$ s with  $p_T > 11$  GeV  $\rightarrow$  Good for differential studies!

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Which measurements can be performed with this statistics?

- $J/\psi$  integrated production cross section
- $J/\psi$  differential cross section
- $J/\psi$  polarization (integrated over the other kinematical variables?)

## First $J/\psi$ papers

CDF

Paper based on 889  $J/\psi$



Integrated cross section  
Differential cross section  $d\sigma/dp_T$

PHENIX

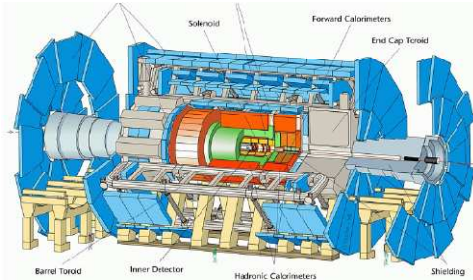
Paper based on 65  $J/\psi$  in  $\mu^+\mu^-$



Differential cross section  $d\sigma/dp_T$ ,  
 $d\sigma/dy$

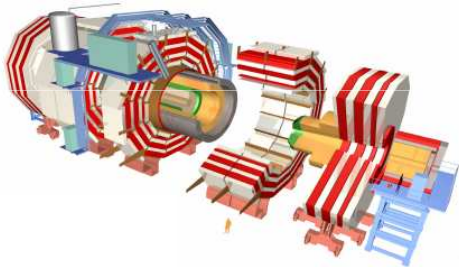


# Other LHC experiments



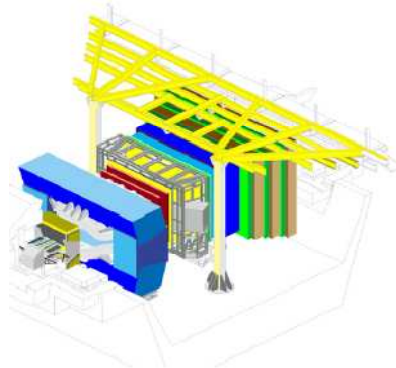
## ATLAS:

- $-2.5 < \eta < 2.5$
- mass resolution  $\sim 50\text{MeV}$
- prompt  $J/\psi$ s separated with fit to proper time distribution
- $10^4 J/\psi$  for  $1\text{pb}^{-1}$  at  $\sqrt{s}=10\text{TeV}$  (high  $p_T$  trig)
- can cover the full  $\cos\theta$  range reaching very high  $p_T$



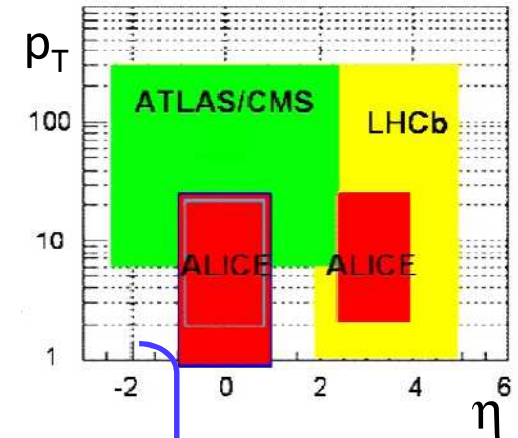
## CMS:

- $-2.5 < \eta < 2.5$
- mass resolution  $\sim 30\text{MeV}$
- $2 \cdot 10^4 J/\psi$  for  $1\text{pb}^{-1}$  at  $\sqrt{s}=10\text{TeV}$  (high  $p_T$  trig)



## LHCb:

- $2 < \eta < 5.5$
- vertex tracking detector (VELO) covering the forward region  $\rightarrow$  very good mass resolution  $\sigma(M) \sim 11\text{MeV}$
- $2 \cdot 10^5 J/\psi$  for  $1\text{pb}^{-1}$  at  $\sqrt{s}=10\text{TeV}$  (larger acc.)



Very competitive wrt ALICE

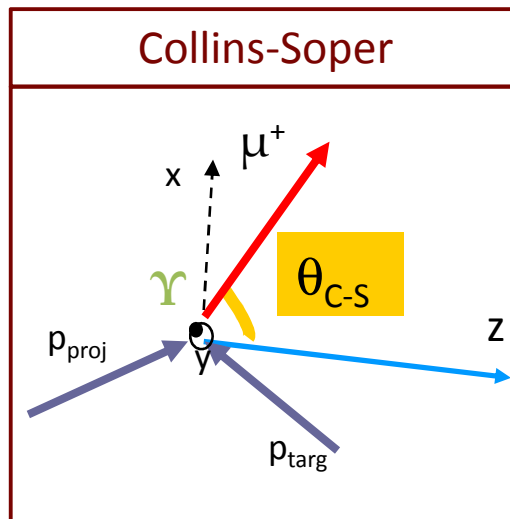
# Polarization: basic concepts

The polarization of Quarkonium is gleaned through the analysis of the angular distribution of daughter particles (e.g.  $\mu^+\mu^-$ ) which follows the trend:

$$\frac{1}{\sigma} \frac{d\sigma}{d\cos(\theta)d\phi} = 1 + \lambda \cos^2(\theta) + \mu \sin(2\theta) \cos(\phi) + \frac{\nu}{2} \sin^2(\theta) \cos(2\phi)$$

$\lambda = 1$  Transverse polarization

$\lambda = -1$  Longitudinal polarization



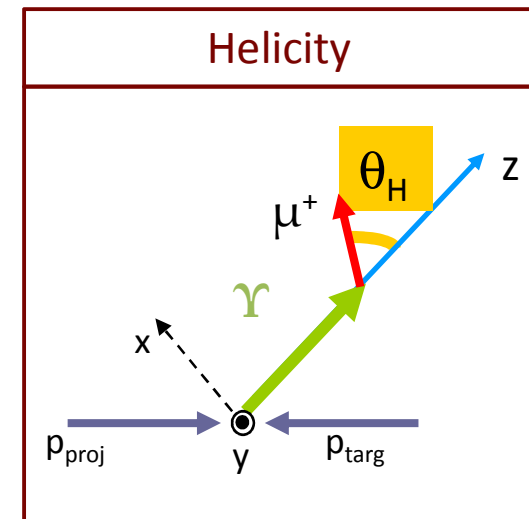
## Reference frames:

### **Collins-Soper (CS):**

The z-axis is the bisector of the projectile and - the target in the quarkonium rest frame.

### **Helicity (HE):**

The z-axis is the direction of the quarkonium in the CM frame.

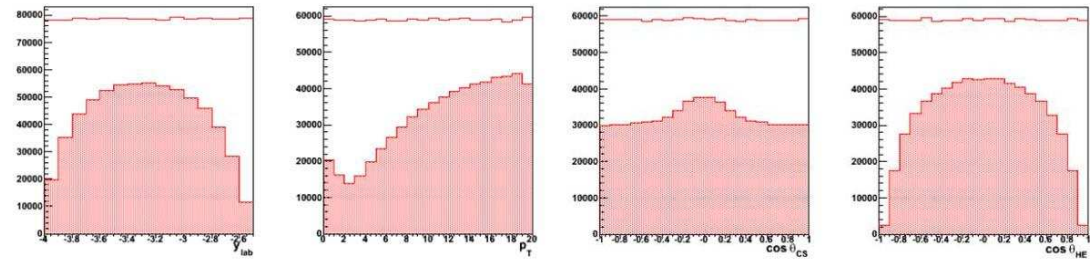


# J/psi polarization in pp: acceptances

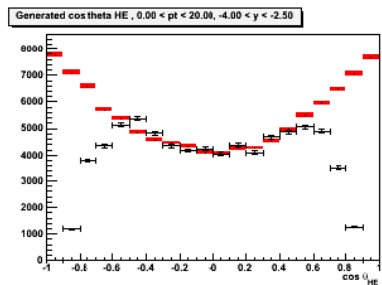
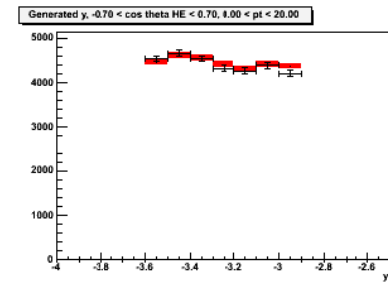
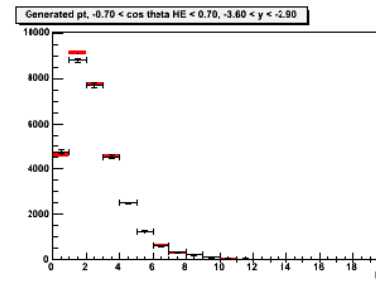
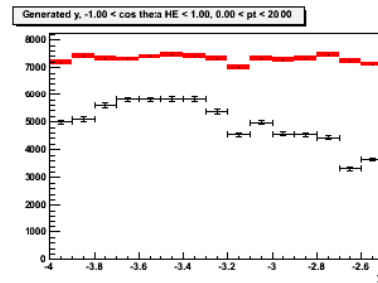
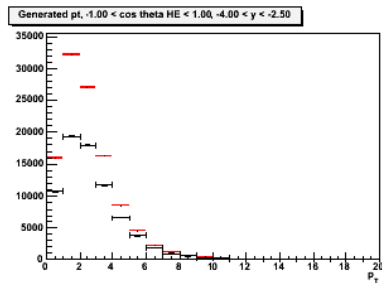
High S/B: bkg. neglecton

state	S ( $\times 10^3$ )	B ( $\times 10^3$ )	S/B	$S/\sqrt{S+B}$
J/ $\psi$	2807	235	12.0	1610
$\psi'$	75	120	0.62	170
$\Upsilon$	27.1	2.6	10.4	157
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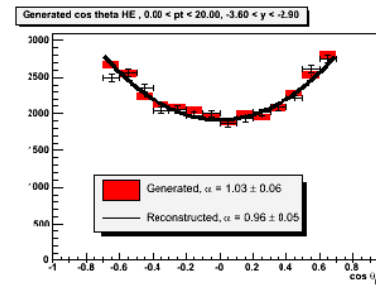
3-D acceptance correction: flat  $y$ ,  $p_T$ ,  $\cos\vartheta$ .



The correction has to be made in fiducial regions where the 3D acceptance do not range over too many orders of magnitude.



— Generated  
— Accept. corrected



$-3.6 < y < 2.9, -0.7 < \cos \theta < 0.7$

— Generated  
— Accept. corrected

# J/ψ polarization in pp@14TeV

Luminosity =  $3 \cdot 10^{30} \text{ cm}^{-2} \text{ s}^{-1}$   
time =  $10^7 \text{ s}$   
J/ψ =  $2.8 \cdot 10^6$

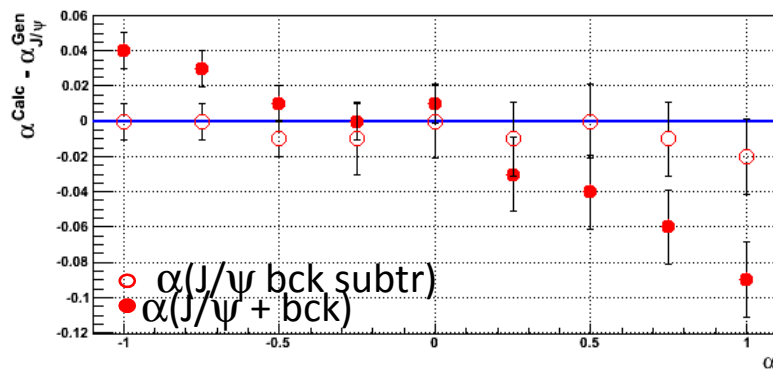


The number of J/ψ is enough to perform a detailed study as a function of  $p_T$ .

Assuming 200000 reconstructed J/ψ in p-p @ 14 TeV (all the statistics we have)

when injecting  $\alpha=0$  we get:

- $1 < p_T < 4 \text{ GeV}/c$ :  $\alpha = -0.02 \pm 0.02$
- $4 < p_T < 7 \text{ GeV}/c$ :  $\alpha = -0.03 \pm 0.04$
- $p_T > 7 \text{ GeV}/c$ :  $\alpha = -0.03 \pm 0.05$



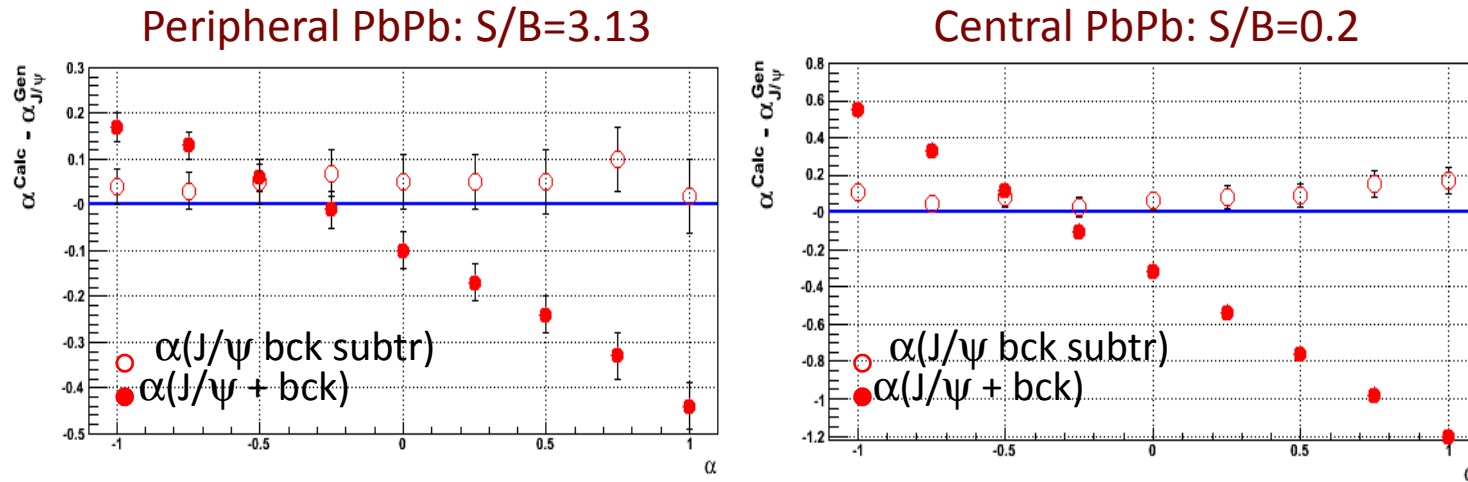
The background contribution is estimated by:

- Adding CORR+UNCORR bkg to the J/ψ peak;
- Using the MC Templates method\* to subtract it (see the  $\Upsilon$  case)

The bias of the  $\alpha$  parameter estimation depends on  $\alpha$  itself (in any case not too big)

\*Robert J. Cropp, *A Measurement of the Polarization of J/psi Mesons Produced in High-Energy pp Collisions*, 2000

# J/psi polarization in PbPb@5.5A TeV



In this case the Bkg cannot be neglected. New method for extracting polarization

Luminosity =  $5 \cdot 10^{26} \text{ cm}^{-2} \text{ s}^{-1}$   
time =  $10^6 \text{ s}$   
J/ $\psi$  = 133000 (central events)  
J/ $\psi$  = 21700 (peripheral events)  
Total J/ $\psi$  =  $6.8 \cdot 10^5$



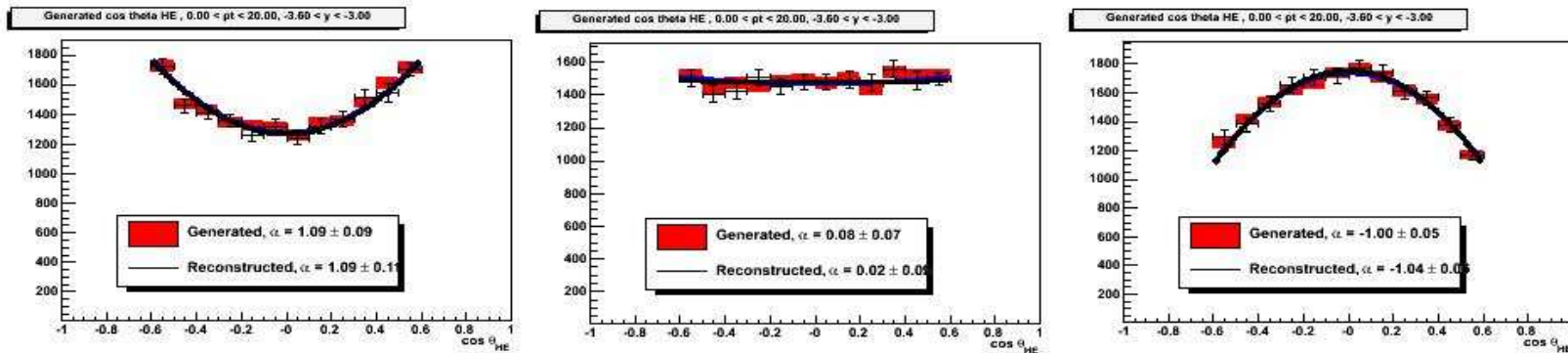
The number of J/ $\psi$  is enough to perform a study as a function of centrality.  
Absolute statistical error  $\sim 0.05$  for all centralities (for peripheral, smaller statistics compensated by the smaller background)

# $\Upsilon$ polarization in pp: performances (I)

Analysis made on a sample of 27100  $\Upsilon$   
(expected yield in pp @  $L=3 \cdot 10^{30} \text{cm}^{-2} \text{s}^{-1}$  in  
 $10^7 \text{s}$  (\*)).

After kinematical cuts we have  
13000  $\Upsilon$

## Elicità



$p_T$ bin (GeV/c)	$\alpha_{\text{gen}}$	$\alpha_{\text{rec}} \text{ (HE)}$	$\alpha_{\text{rec}} \text{ (CS)}$
$0 < p_T < 20$	1	$1.09 \pm 0.11$	$0.96 \pm 0.10$
	0	$0.02 \pm 0.09$	$0.02 \pm 0.08$
	-1	$-1.04 \pm 0.05$	$-0.94 \pm 0.05$

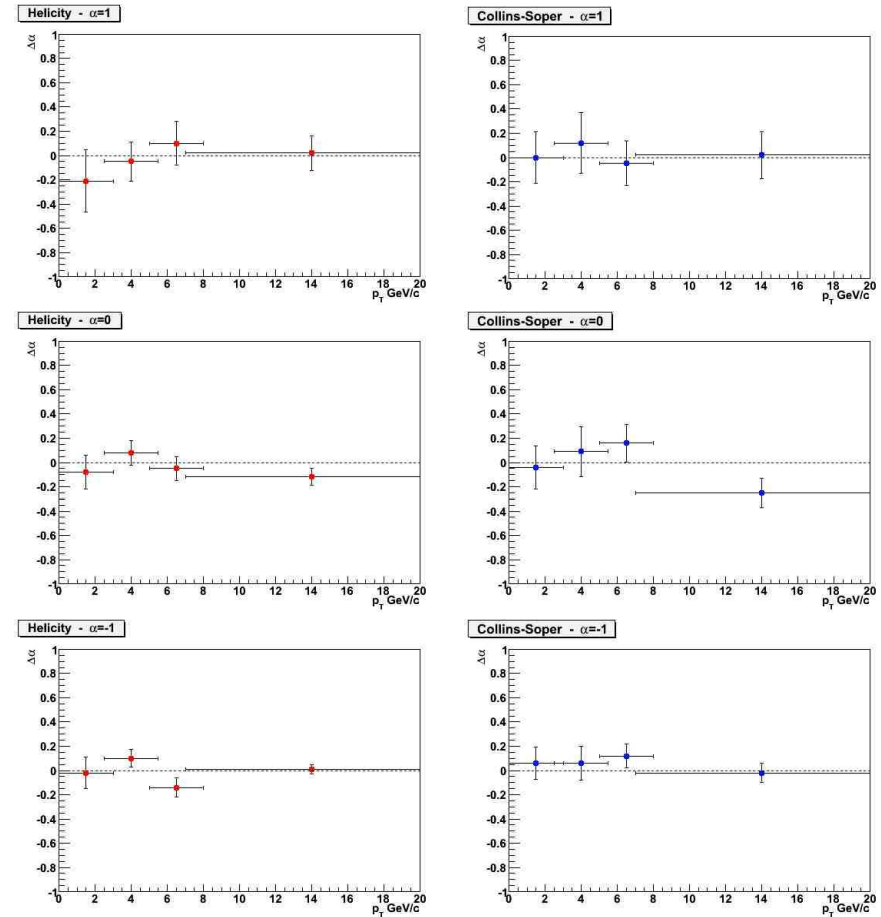
Statistical error ranges from  
0.05 and 0.11

Good agreement between  $\alpha_{\text{gen}}$  and  $\alpha_{\text{rec}}$   
after acceptance corrections

(\*) ALICE-INT-2006-029

# $\Upsilon$ polarization in pp: performances (II)

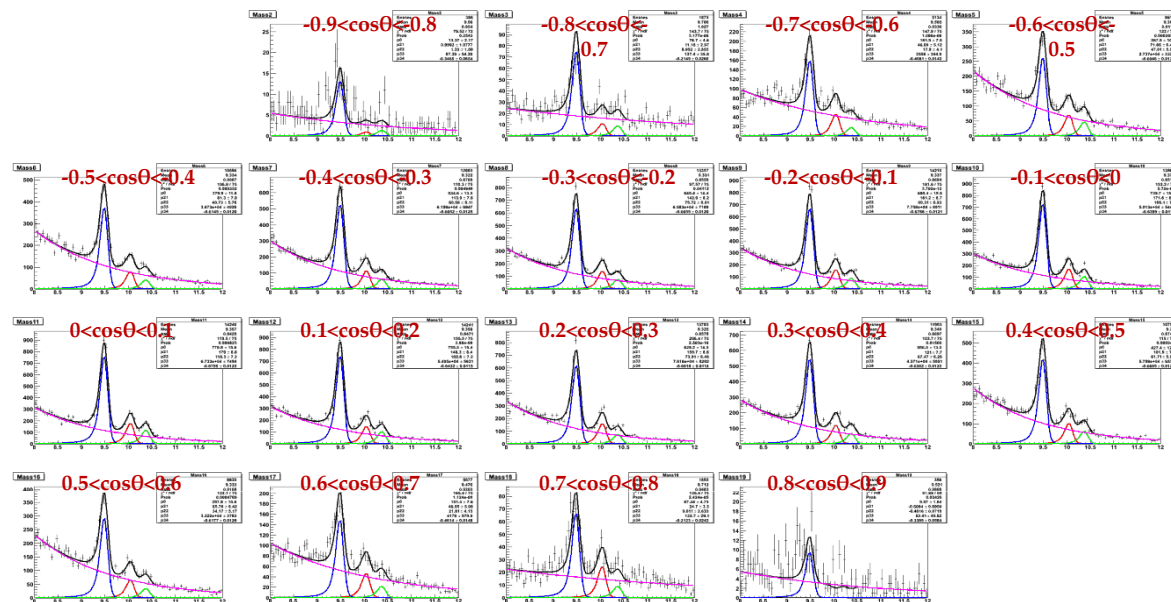
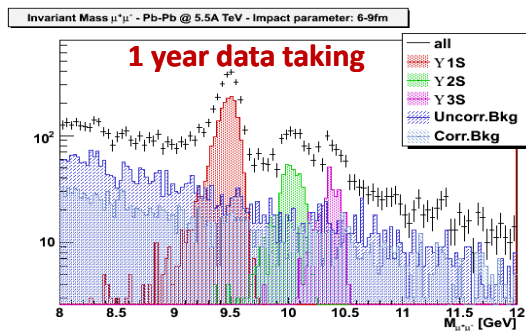
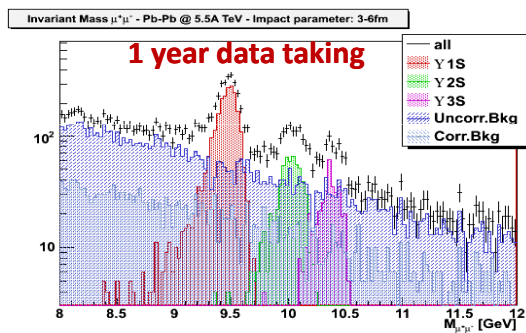
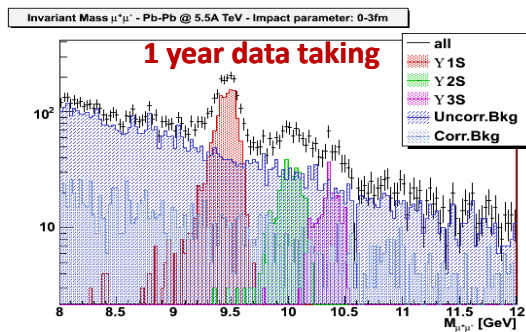
$p_T$ bin (GeV/c)	$\alpha_{\text{gen}}$	$\Delta\alpha_{\text{rec}}$		$Y_{\text{rec}}$ dopo tagli ( $\#Y_{\text{gen}} = 27100$ )	
		HE	CS	HE	CS
$0 < p_T < 3$	1	$-0.21 \pm 0.25$	$0.00 \pm 0.21$	~5100	~4900
	0	$-0.11 \pm 0.18$	$-0.04 \pm 0.18$		
	-1	$-0.02 \pm 0.13$	$0.06 \pm 0.13$		
$3 < p_T < 5$	1	$-0.05 \pm 0.16$	$0.12 \pm 0.25$	~5600	~4700
	0	$0.14 \pm 0.12$	$0.09 \pm 0.21$		
	-1	$0.10 \pm 0.07$	$0.06 \pm 0.14$		
$5 < p_T < 8$	1	$0.10 \pm 0.18$	$-0.05 \pm 0.18$	~5100	~4600
	0	$-0.04 \pm 0.12$	$0.16 \pm 0.16$		
	-1	$-0.14 \pm 0.08$	$0.12 \pm 0.10$		
$8 < p_T < 20$	1	$0.02 \pm 0.14$	$0.02 \pm 0.19$	~4000	~3500
	0	$-0.02 \pm 0.09$	$-0.25 \pm 0.12$		
	-1	$0.01 \pm 0.04$	$-0.02 \pm 0.08$		



Good agreement between  $\alpha_{\text{gen}}$  and  $\alpha_{\text{rec}}$   
 Statistical errors: from 0.03 to 0.19

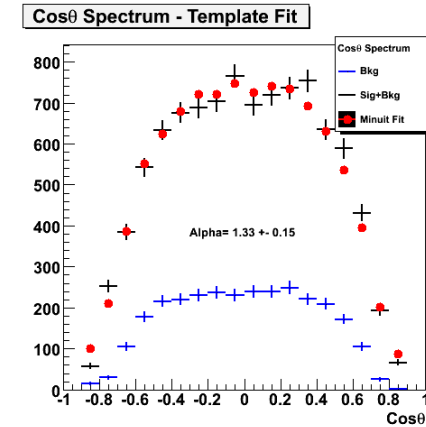
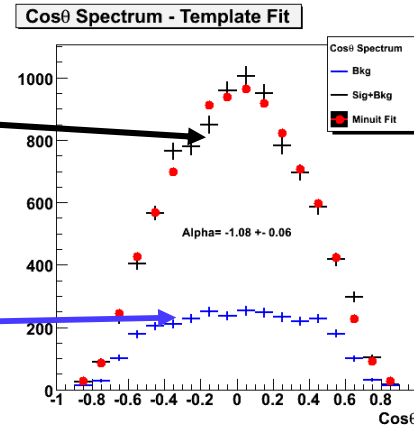
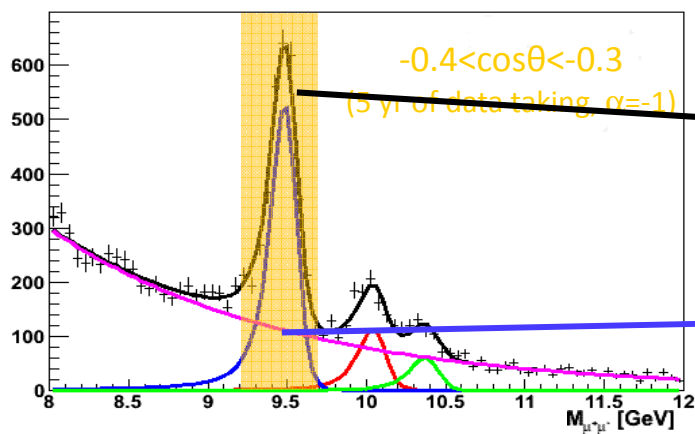


# $\Upsilon$ polar. in PbPb: MC Template Method

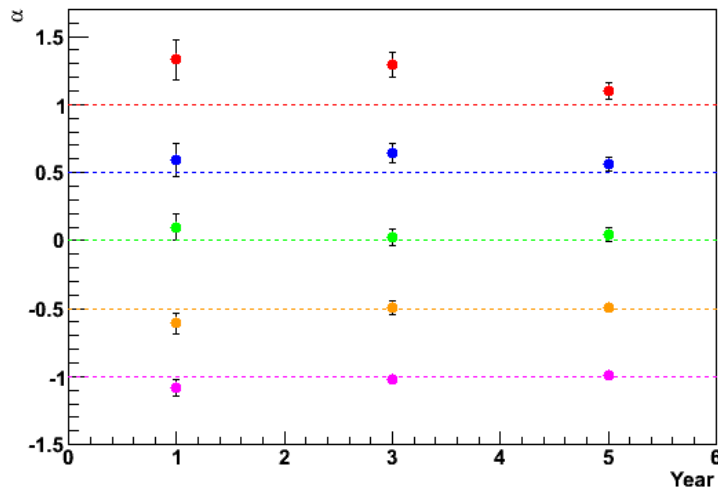


- Sample divided in 20  $\cos\vartheta$  bins;
- For each  $\cos\vartheta$  bin a mass spectrum is done and fitted;
- The fits allow the evaluation of the bkg. (B) and of the signal+bkg (S+B) contributions;
- The values of B and S+B are plotted in a  $\cos\vartheta$  spectrum;

# $\Upsilon$ polarization in PbPb: performances

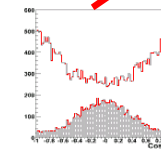
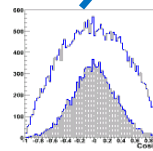


Y1S - Polarization reconstruction



- The S+B  $\cos\theta$  spectrum is fitted with a linear superposition of two templates (one transversely polarized and one longitudinally) plus the Bkg contribution;
- The coefficients of the linear superposition give the value of  $\alpha$ .

$$\left\{ \frac{1-\alpha}{3+\alpha} \cdot T_L(\cos\theta) \right\} + \left\{ \frac{2(1+\alpha)}{3+\alpha} \cdot T_T(\cos\theta) \right\} + Bkg(\cos\theta) = F_{S+B}(\cos\theta)$$



# Polarization in PDC09 (pp @10TeV)

Id	cycle	description	software	run range	events per sub-run	events produced	status	request
91	LHC09a10	dijet trigger, w/o polarization, residual	v4-17-Rev-04 (root: v5-24-00, geant3: v1-11)	100400 to 100436	100	3420400	completed	2 $10^8$
94	LHC09a11	dijet trigger, pol. (.3/.3/0./1./0.), residual	v4-17-Rev-05 (root: v5-24-00, geant3: v1-11)	101014 to 101018	100	475400	completed	4 $10^8$
95	LHC09a12	dijet trigger, pol. (-.3/.3/0./1./0.), residual	same as 94	102000 to 102005	100	270000	completed	4 $10^8$
96	LHC09a13	dijet trigger, pol. (0./0./0./1./0.), residual	same as 94	103000 to 103005	100	371900	completed	4 $10^8$
98	LHC09a16	dijet trigger, w/o pol, full, secret deadmaps & x-sect.	same as 94	111001 to 111005	100		not yet started	4 $10^8$
99	LHC09a17	1jet trigger, full, w/o field	same as 94	112001 to 112008	100	662700	completed	6 $10^8$
100	LHC09a18	min. bias, w/o pol., residual	same as 94	113001 to 1000001	400	9856800 (until 113040)	running	2 $10^8$

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In particular 3 productions with polarized quarkonia:

- LHC09a11:  $\alpha_{J/\psi} = 0.3$ ,  $\alpha_{\psi'} = 0.3$ ,  $\alpha_{\Upsilon} = 0.$ ,  $\alpha_{\Upsilon'} = 1.$ ,  $\alpha_{\Upsilon''} = 0.$
- LHC09a12:  $\alpha_{J/\psi} = -0.3$ ,  $\alpha_{\psi'} = -0.3$ ,  $\alpha_{\Upsilon} = 0.$ ,  $\alpha_{\Upsilon'} = 1.$ ,  $\alpha_{\Upsilon''} = 0.$
- LHC09a13:  $\alpha_{J/\psi} = 0.$ ,  $\alpha_{\psi'} = 0.$ ,  $\alpha_{\Upsilon} = 0.$ ,  $\alpha_{\Upsilon'} = 1.$ ,  $\alpha_{\Upsilon''} = 0.$

Simulation done using AliGenMUONCocktailpp:

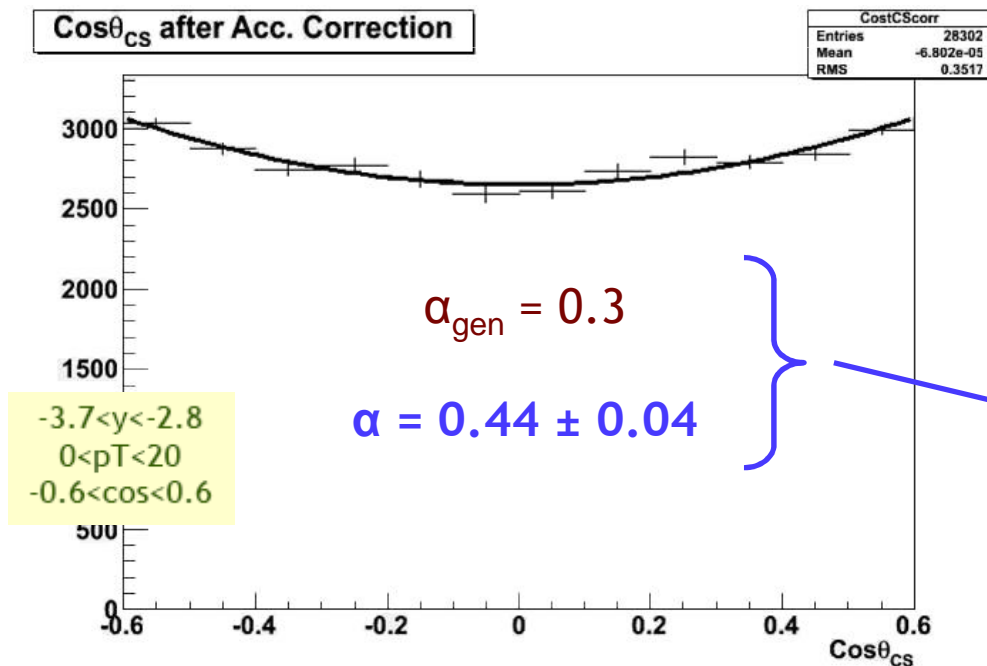
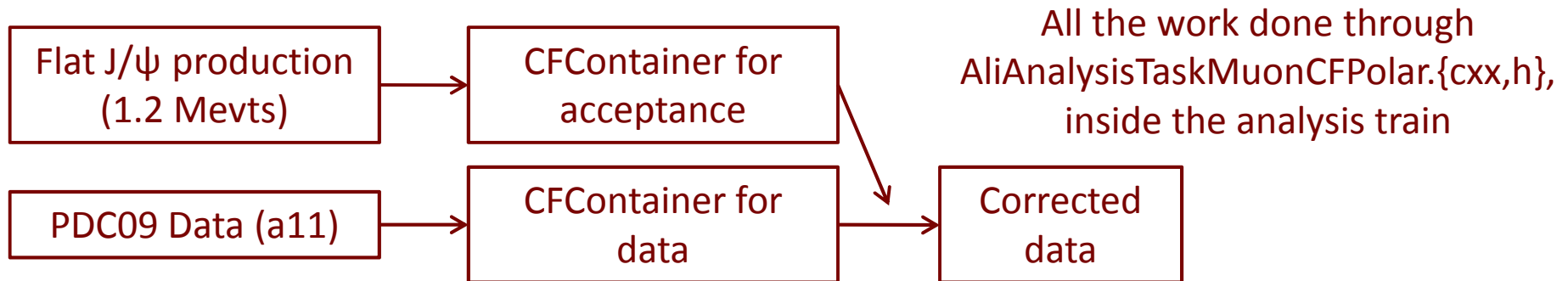
-Pythia mBias

-5 resonances

-Open heavy flavors.

The polarization is given using AliDecayerPolarized. It can be set with different values to each resonance. Only the  $\cos\vartheta$  spectrum can be changed (until now).

# Polarization analysis from PDC09



The 3D acceptance correction ( $y$ ,  $p_T$  and  $\cos\vartheta$  - 2D and 4D are possible) is made in fiducial regions chosen in order to have acceptance not ranging on too many orders of magnitude.

**Discrepancy:  
 due to  $B \rightarrow J/\psi + X$ ?  
 UNDER STUDY.**

# Conclusions and Ongoings

## Conclusions

The muon spectrometer of the ALICE experiment is ready to take data – cosmic runs show good performances of the entire detector.

The first  $J/\psi$  paper could be done using statistics of  $10^4$  events (less than 5 months of data taking) allowing the study of integrated and differential ( $d\sigma/dp_T$ ,  $d\sigma/dy$ ) cross sections and (maybe) an integrated over  $p_T$  value of polarization.

The polarization analysis can be done both in pp and PbPb. The bkg contribution has been studied and, at least in the second case, a bkg-subtraction strategy has to be implemented.

A first look to PDC09 data gives encouraging results.

## Coming next

Full analysis of PDC09 data (polarization &  $p_T/y$  spectra)

Study of  $B \rightarrow J/\psi + X$  contribution to the  $\cos\vartheta$  spectrum

# Backup Slides

# Muon spectrometer parameters (I)

## Muon detection

Polar, azimuthal angle coverage	$2 \leq \theta \leq 9, 2\pi$	
Minimum muon momentum	4 GeV/c	
Resonance detection	J/ψ	Υ
Pseudo-rapidity coverage	$-4.0 \leq \eta \leq -2.5$	$-4.0 \leq \eta \leq -2.5$
Transverse momentum range	$0 \leq p_t$	$0 \leq p_t$
Mass resolution	70 MeV	100 MeV

## Front absorber

Longitudinal position (from IP)	$-5030\text{mm} \leq z \leq -900\text{mm}$
Total thickness (materials)	10λ (carbon-concrete-steel)

## Dipole magnet

Nominal magnetic field, field integral	0.7 T, 3 Tm
Free gap between poles	2.972 – 3.956 m
Overall magnet length	4.97m
Longitudinal position (from IP)	-z = 9.87m (centre of the dipole yoke)

## Tracking chambers

Number of stations, number of planes per station	5, 2
Longitudinal position of stations	-z = 5357, 6860, 9830, 12920, 14221 mm
Anodecathode gap (equal to wire pitch)	2.1 mm for st. 1; 2.5 mm for st. 2-5
Gas mixture	80%Ar/20%CO <sub>2</sub>
Pad size st. 1 (bending plane)	4 × 6, 4 × 12, 4 × 24mm <sup>2</sup>
Pad size st. 2 (bending plane)	5 × 7.5, 5 × 15, 5 × 30mm <sup>2</sup>
Pad size st. 3, 4 and 5 (bending plane)	5 × 25, 5 × 50, 5 × 100mm <sup>2</sup>
Max. hit density st. 15 (central PbPb × 2)	5.0, 2.1, 0.7, 0.5, 0.6 · 10 <sup>-2</sup> hits cm <sup>-2</sup>
Spatial resolution (bending plane)	≈ 70 μm



# Muon spectrometer parameters (II)

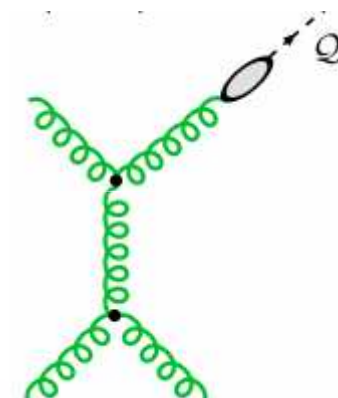
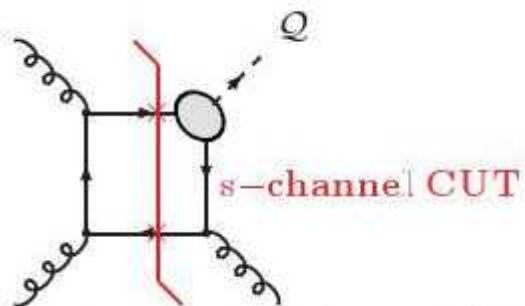
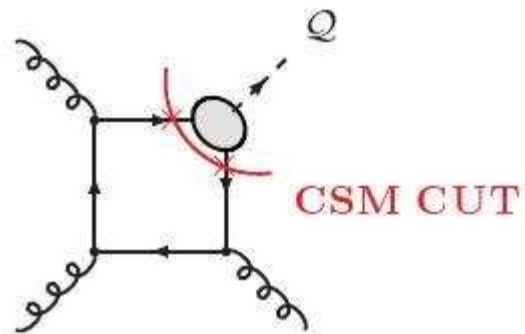
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<b>Tracking electronics</b>	
Total number of FEE channels	$1.09 \times 10^6$
Shaping amplifier peaking time	$1.2 \mu s$
<b>Trigger chambers</b>	
Number of stations, planes per station	2, 2
Longitudinal position of stations	$-z = 16\ 120, 17\ 120\ \text{mm}$
Total number of RPCs, total active surface	72, $\sim 150\text{m}^2$
Gas gap	single, 2 mm
Electrode material and resistivity	Bakelite <sup>TM</sup> , $\rho = 24 \times 10^9\ \text{cm}$
Gas mixture	Ar/C <sub>2</sub> H <sub>2</sub> F <sub>4</sub> /i-butane/SF <sub>6</sub> ratio 49/40/7/1
Pitch of readout strips (bending plane)	10.6, 21.2, 42.5 mm (for trigger st. 1)
Max. strip occupancy bend. (non bend.) plane	3%(10%) in central Pb-Pb
Maximum hit rate on RPCs	3 (40) Hz $\text{cm}^{-2}$ in Pb-Pb (Ar-Ar)
<b>Trigger electronics</b>	
Total number of FEE channels	$2.1 \times 10^4$
Number of local trigger cards	234 + 2

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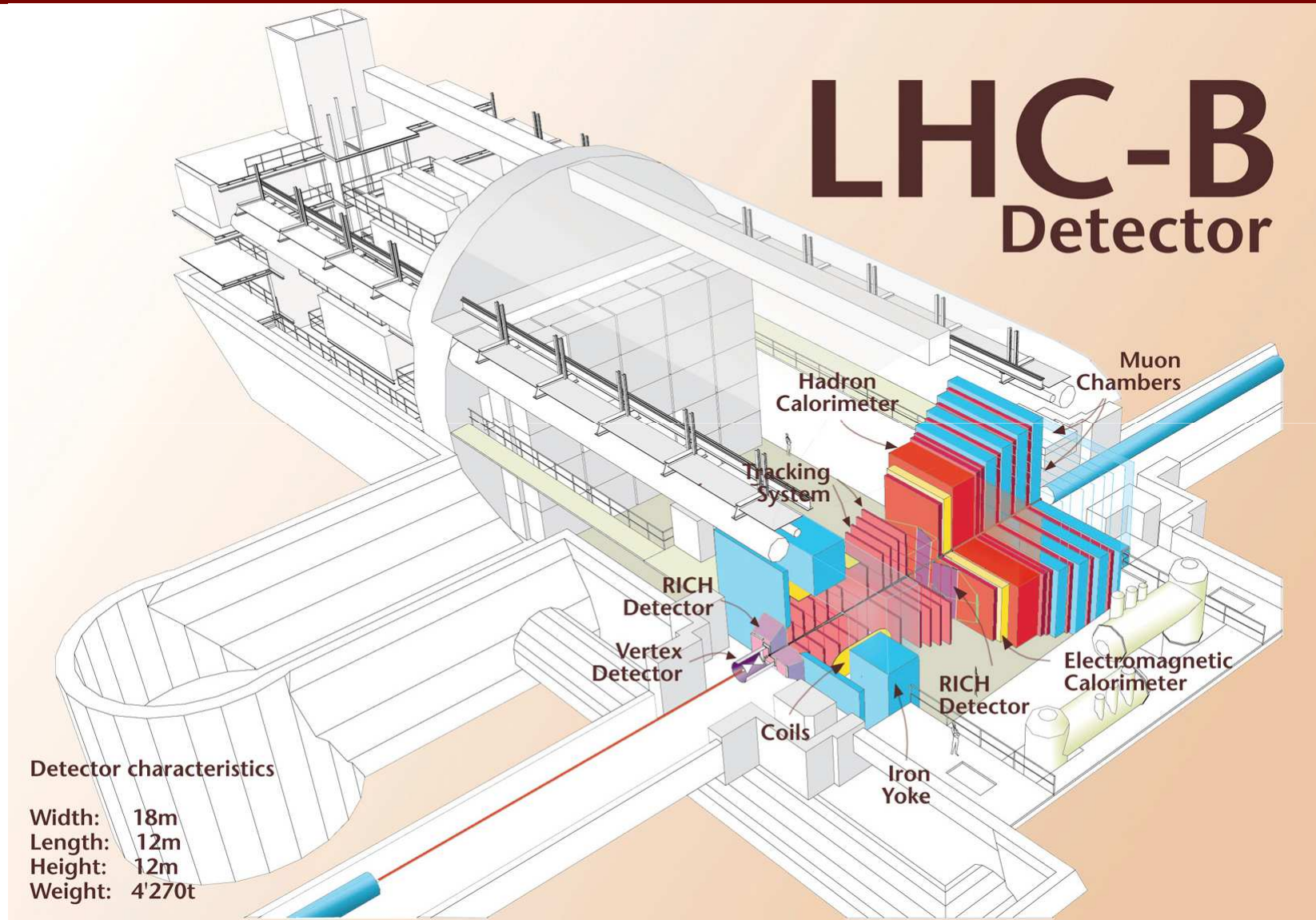
Font: ALICE Physics Performance Report Vol. I, J. Phys. G: Nucl. Part. Phys. 30 (2004)

# Production mechanism

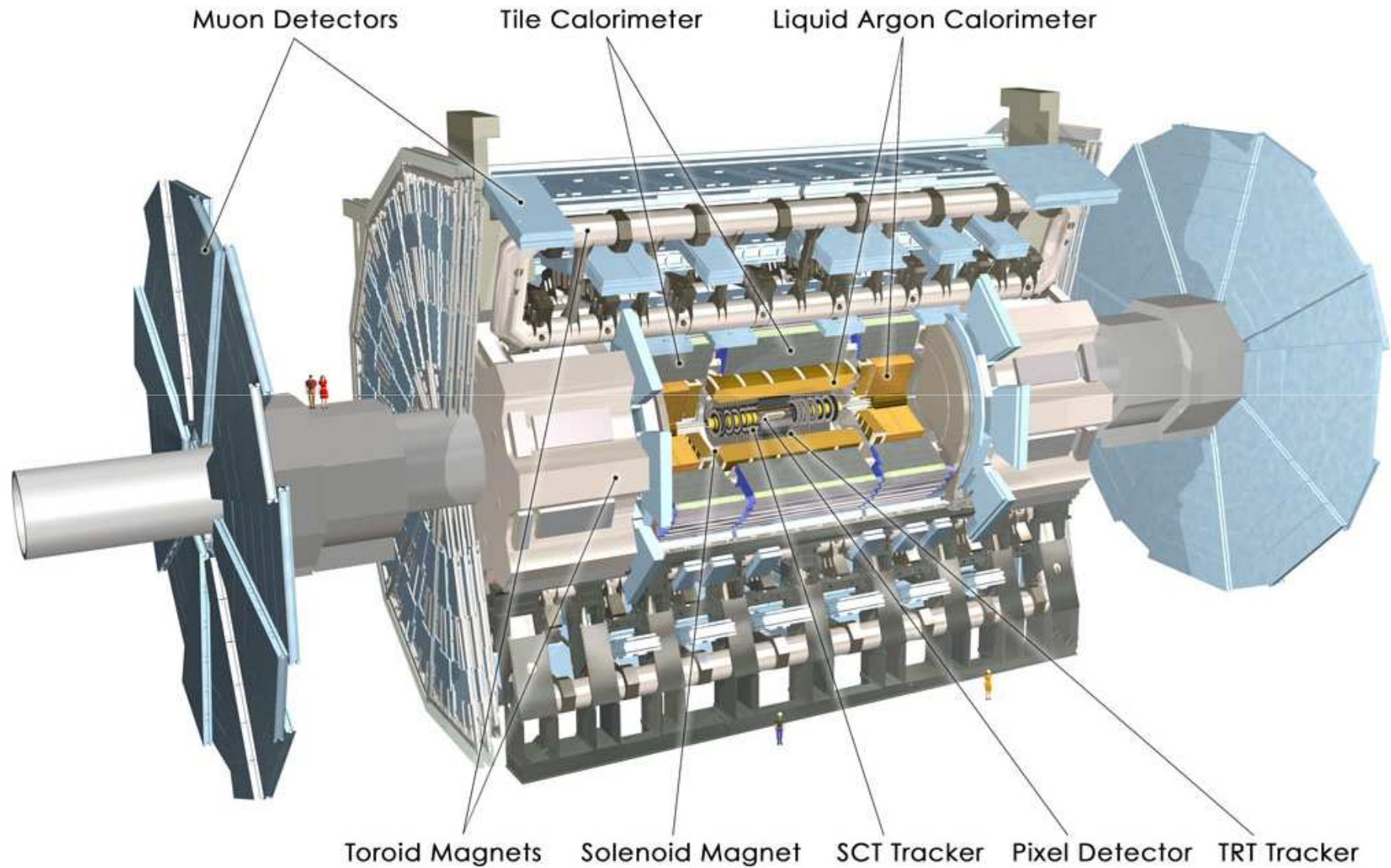


JPL, J.R. Cudell, Yu.L. Kalinovsky, PLB633:301,2006

# The LHCb Detector

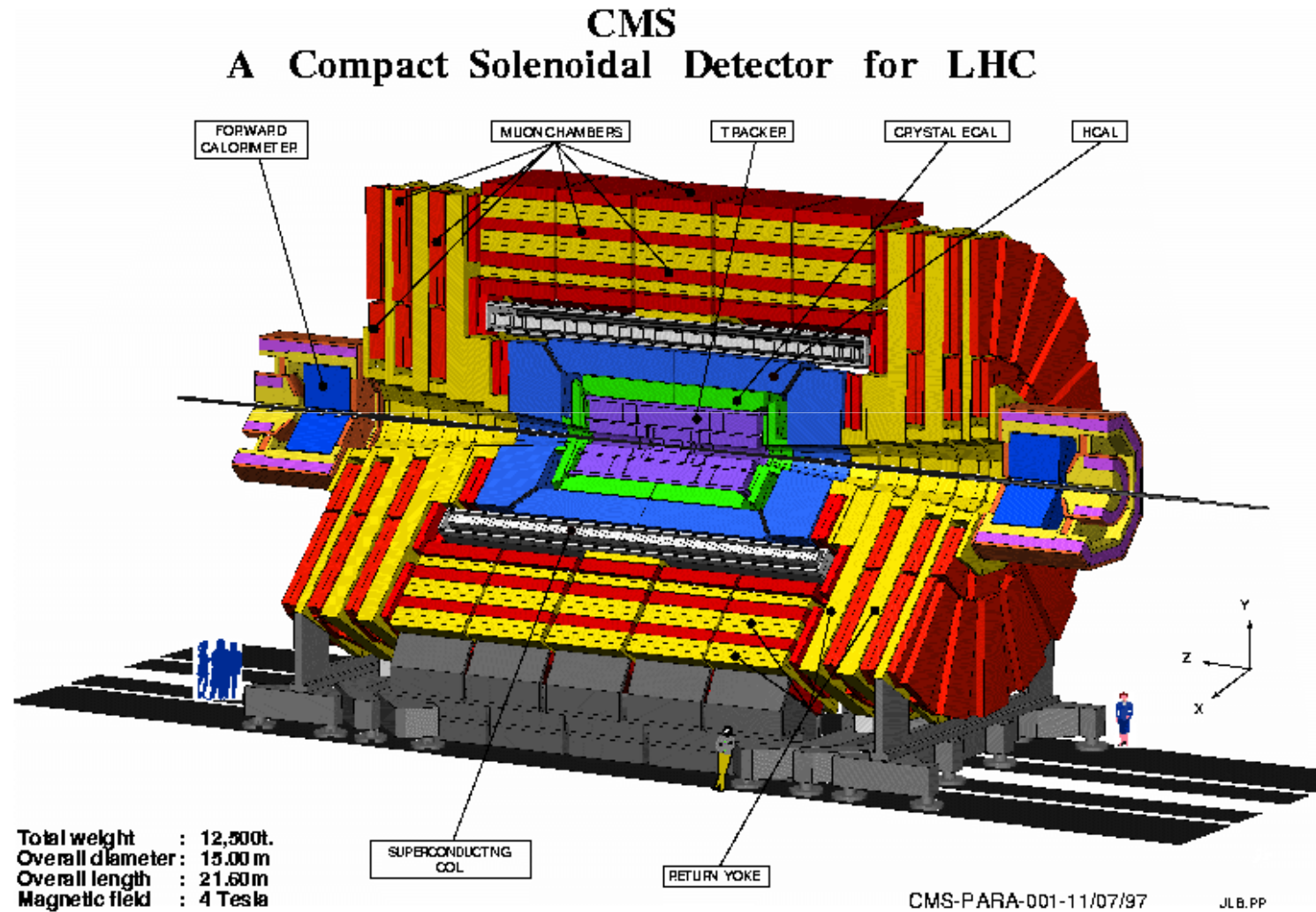


# The ATLAS Detector

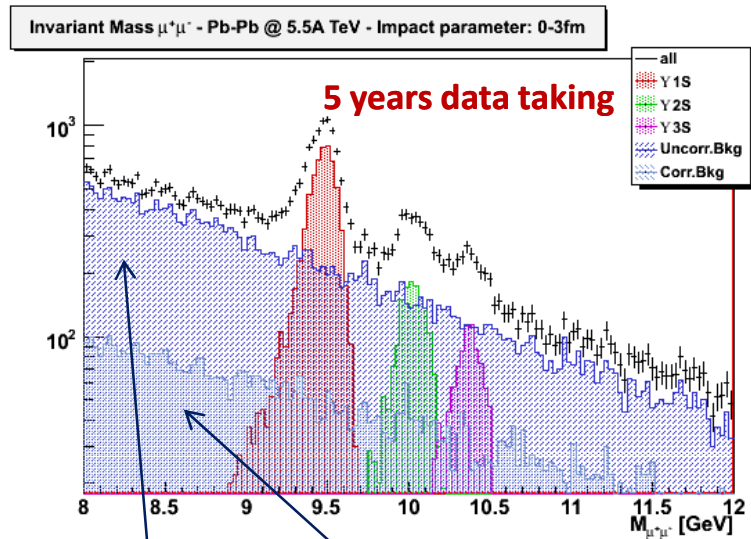




# The CMS Detector



# Preparing Data Samples (I)



$b\bar{b} \rightarrow \bar{B}^0 B^+ + X \rightarrow D^+ \mu^- \nu_\mu + \bar{D}^0 \mu^+ \nu_\mu \rightarrow \mu^+ \mu^- \nu_\mu + \mu^- \mu^+ \nu_\mu + X$   
 $c\bar{c} \rightarrow D^+ + \bar{D}^0 + X \rightarrow \mu^+ \mu^- + X$

bb – cc – bc contributions

- **Signal:**  $\Upsilon(1S)$ ,  $\Upsilon(2S)$  and  $\Upsilon(3S)$  samples generated with AliGenParam and reconstructed with full-simulation. Generation done with several degrees of polarization: -1, -0.5, 0, 0.5, 1.
- **Correlated Background:** generated with Pythia by Rachid Guernane\* and reconstructed with fast simulation
- **Uncorrelated Background:** generated through parametrization and reconstructed with the fast simulation approach (see \$ALICE\_ROOT/FASTSIM/uncorrBg.C)

$\pi$  and K contribution to background negligible in 8-12 GeV mass region

**1, 3 and 5 years of data taking have been considered ( $L = 5 \cdot 10^{26} \text{ cm}^{-2} \text{ s}^{-1}$ )**

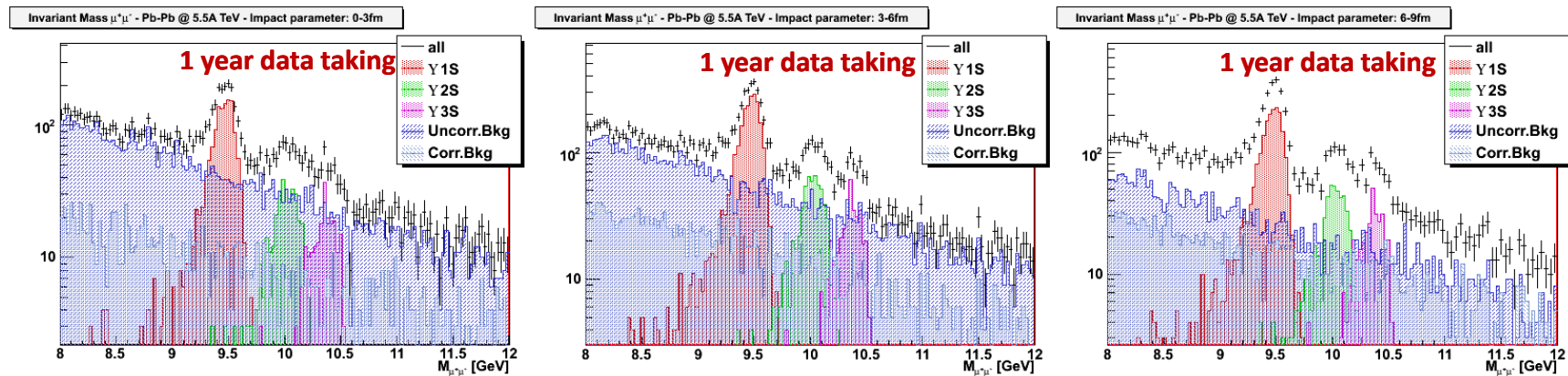
\*ALICE-INT-2005-018 version 1.0

# Preparing Data Samples (II)

The relative weights of correlated and uncorrelated bkg have been taken from Smbat Grigoryan's work, published in PPR-Vol.2

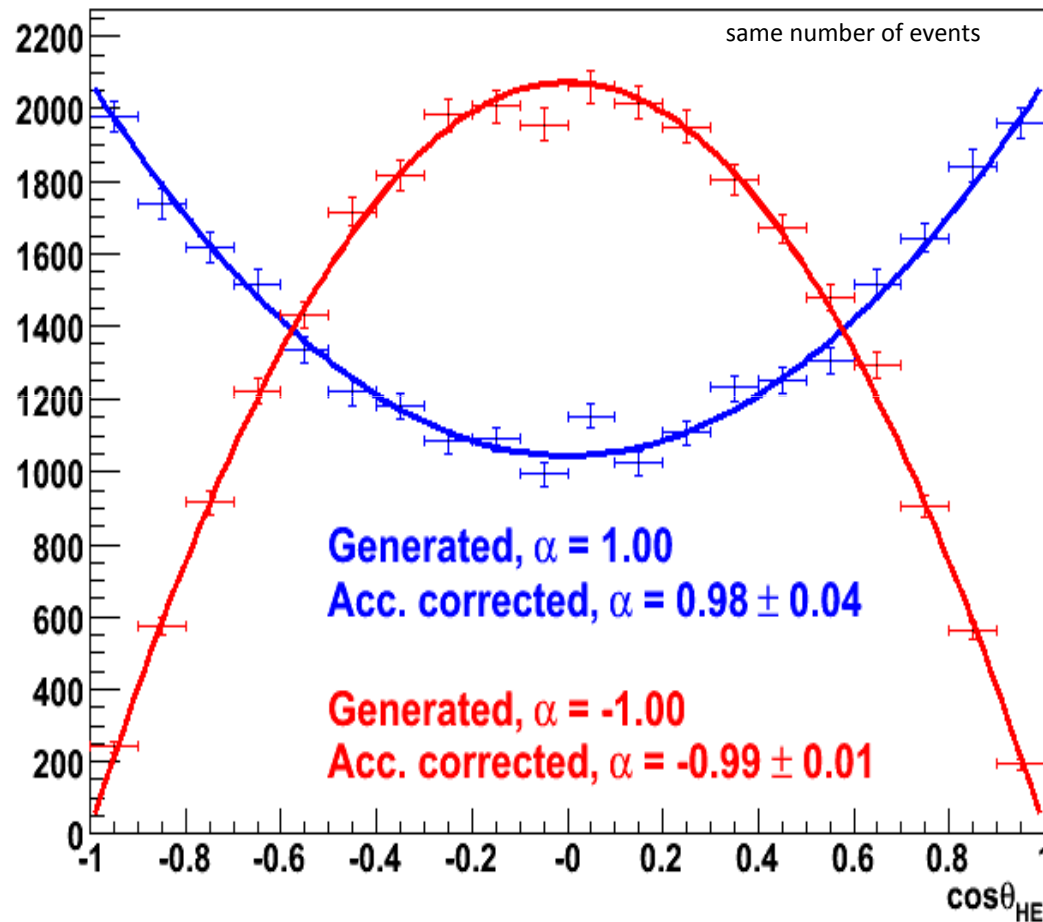
The contribution of each type of bkg is different in the 5 centrality classes: 5 different data samples have been prepared for each polarization

We did all the work integrating over the impact parameter, but in the future a study of the centrality dependence of the  $\alpha$  parameter could be done using the same generated data





# Angular distribution fit: error on $\alpha$

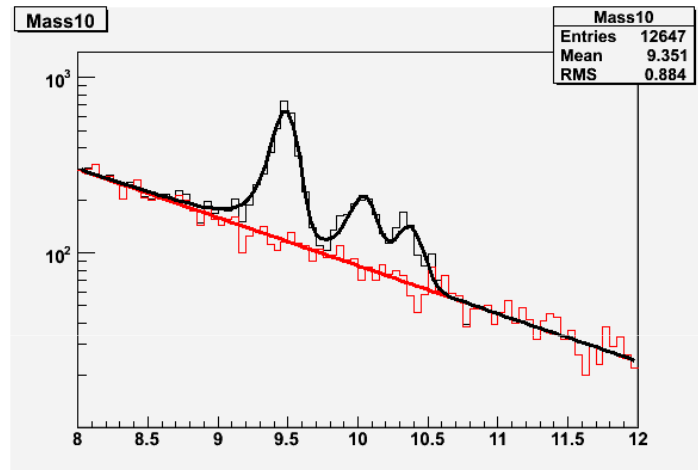


With the same number of reconstructed events the error on  $\alpha$  increases while  $\alpha$  enhances.

In the Least Squares fitting method if  $f(x) = p_0 \cdot (1 + \alpha \cdot x^2)$  then for  $p_0$  large  $\sigma_\alpha \propto 1/p_0$

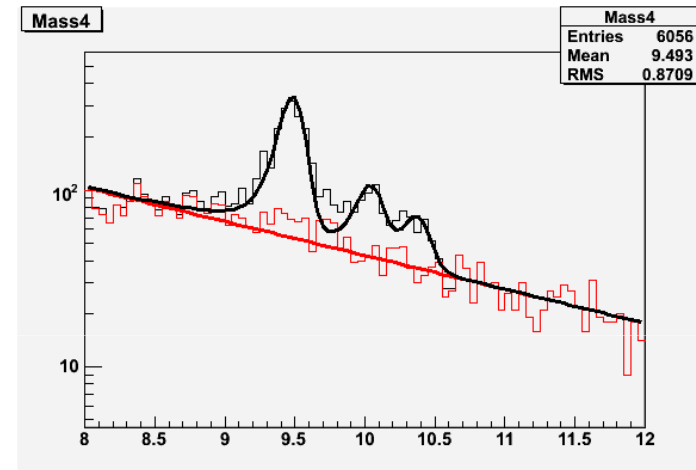
# Bias on high values of $\alpha$

In peripheral  $\cos\theta$  bins we sometimes underestimate the background contribution:



Central  $\cos\theta$  bins: the Bkg shape seems to be perfectly exponential  $\rightarrow$  the contribution is well estimated

**Only for high values of  $\alpha$  because in that case the shape of the  $\cos\theta$  depends more directly on the behaviour of the most peripheral bins**



Edges of the  $\cos\theta$  distribution: the Bkg shape is not exponential  $\rightarrow$  the contribution is underestimated



The spectrum shape is wider



$\alpha$  is bigger

# Fit of the $\cos\vartheta$ spectrum: minimization

Template fit to the  $\cos\theta$  spectrum done with MINUIT minimizing the quantity:

$$\chi^2 = 2 \cdot \sum_i \left\{ (E_i + \beta_i - D_i) - D_i \cdot \ln\left(\frac{E_i + \beta_i}{D_i}\right) + (\beta_i - S_i) - S_i \cdot \ln\left(\frac{\beta_i}{S_i}\right) \right\}$$

where:

$$\beta_i = \frac{1}{4} \left[ -(2E_i - D_i - S_i) + \sqrt{(2E_i - D_i - S_i)^2 + 8S_iE_i} \right]$$

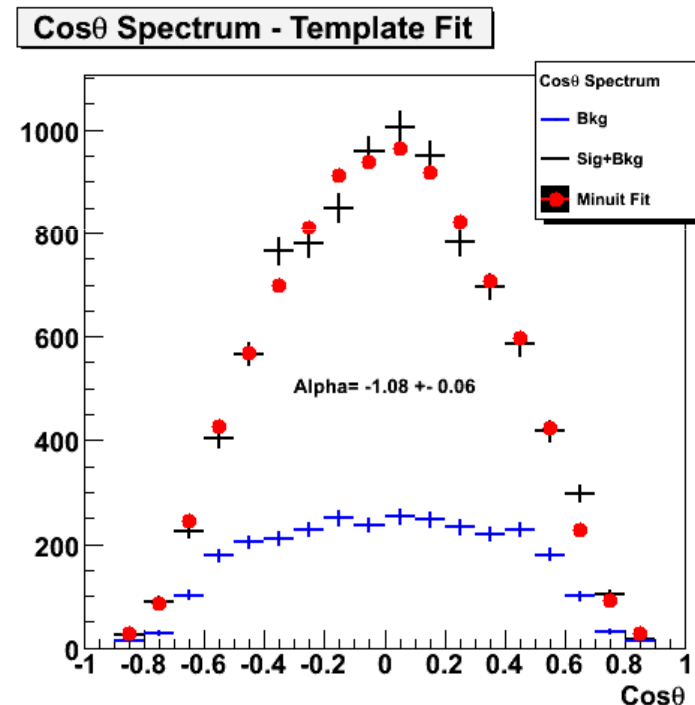
$D_i$  : *Signal + Bkg events*       $S_i$  : *Bkg events*

$E_i$  : *expected number of Signal events*

$\beta_i$  : *expected number of Bkg events*

The formula is correct when signal+background and background errors are both poissonian.

We suppose background errors to be poissonian: not completely correct because not obtained from an event counting technique.



T. Devlin, *Correlations from Systematic Corrections to Poisson-Distributed Data in Log-Likelihood Functions*, CDF public note CDF/DOC/JET/PUBLIC/3126 (1995)

# How to study polarization

The polarization of Quarkonium is gleaned through the analysis of the angular distribution of daughter particles (e.g.  $\mu^+\mu^-$ ) which follows the trend:

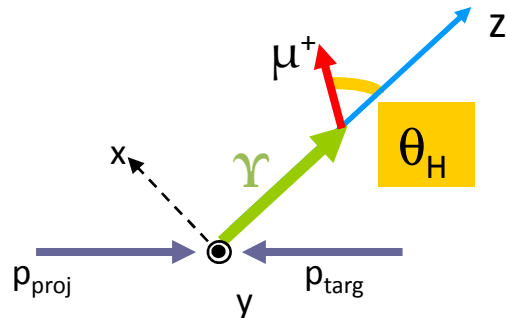
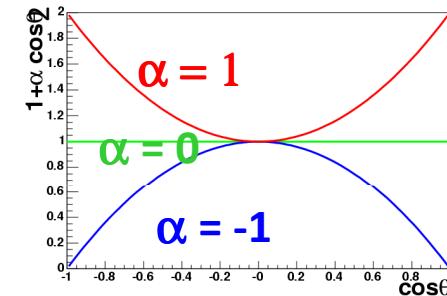
$$\xi_L = \frac{\sigma_L}{\sigma_{TOT}} = \frac{1 - \alpha}{3 + \alpha}$$

$$\xi_T = 1 - \xi_L$$

$$\frac{d\Gamma}{d\cos\theta^*} \propto \frac{3}{2(\alpha + 3)} (1 + \alpha \cos^2 \theta^*)$$

$\alpha=1$  Transverse polarization

$\alpha=-1$  Longitudinal polarization



The angular distribution is usually analyzed in the  $\Upsilon$  C.M. frame. Polarization angle defined as the angle between  $\mu^+$  momentum and a “polarization axis” which can be chosen in different ways.

We use the helicity (HE) reference frame, in which the z-axis is the direction of the  $\Upsilon$  momentum in the p-p C.M. frame.