

# A new region of deformation for neutron-rich nuclei at $N \sim 40$



Silvia M. Lenzi  
*University of Padua and INFN*

JAPAN-ITALY EFES Workshop  
Torino, 6-8 September 2010

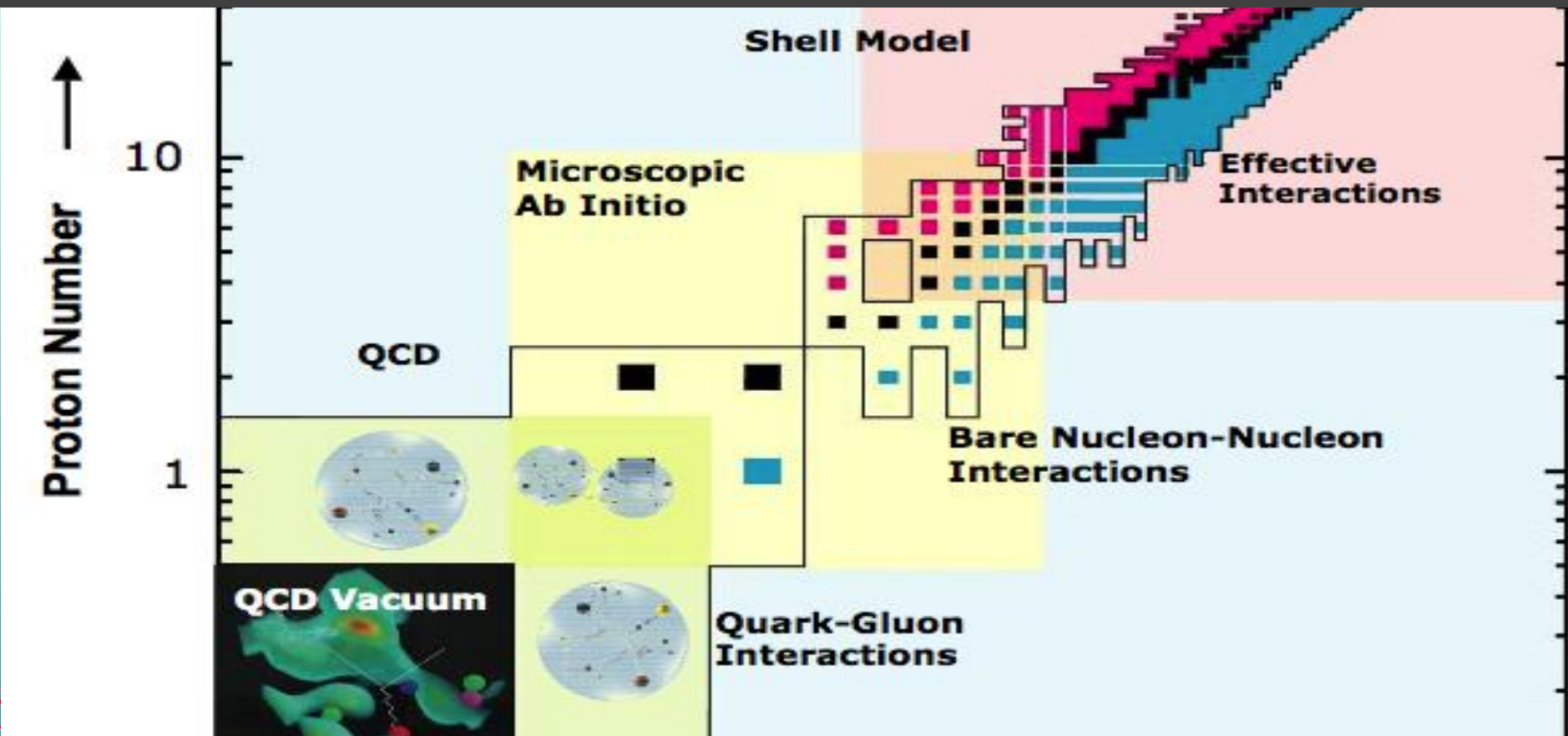
# Outline

The background features three prominent, curved, parallel bands of light that sweep across the frame from the top-left towards the bottom-right. The top band is primarily orange and red, the middle band is a mix of purple, blue, and yellow, and the bottom band is green. These bands are set against a dark, textured background that resembles a fine grid or a woven fabric.

- Introduction
- Evidence of deformation at  $N \sim 40$
- Shell model description
- Conclusions

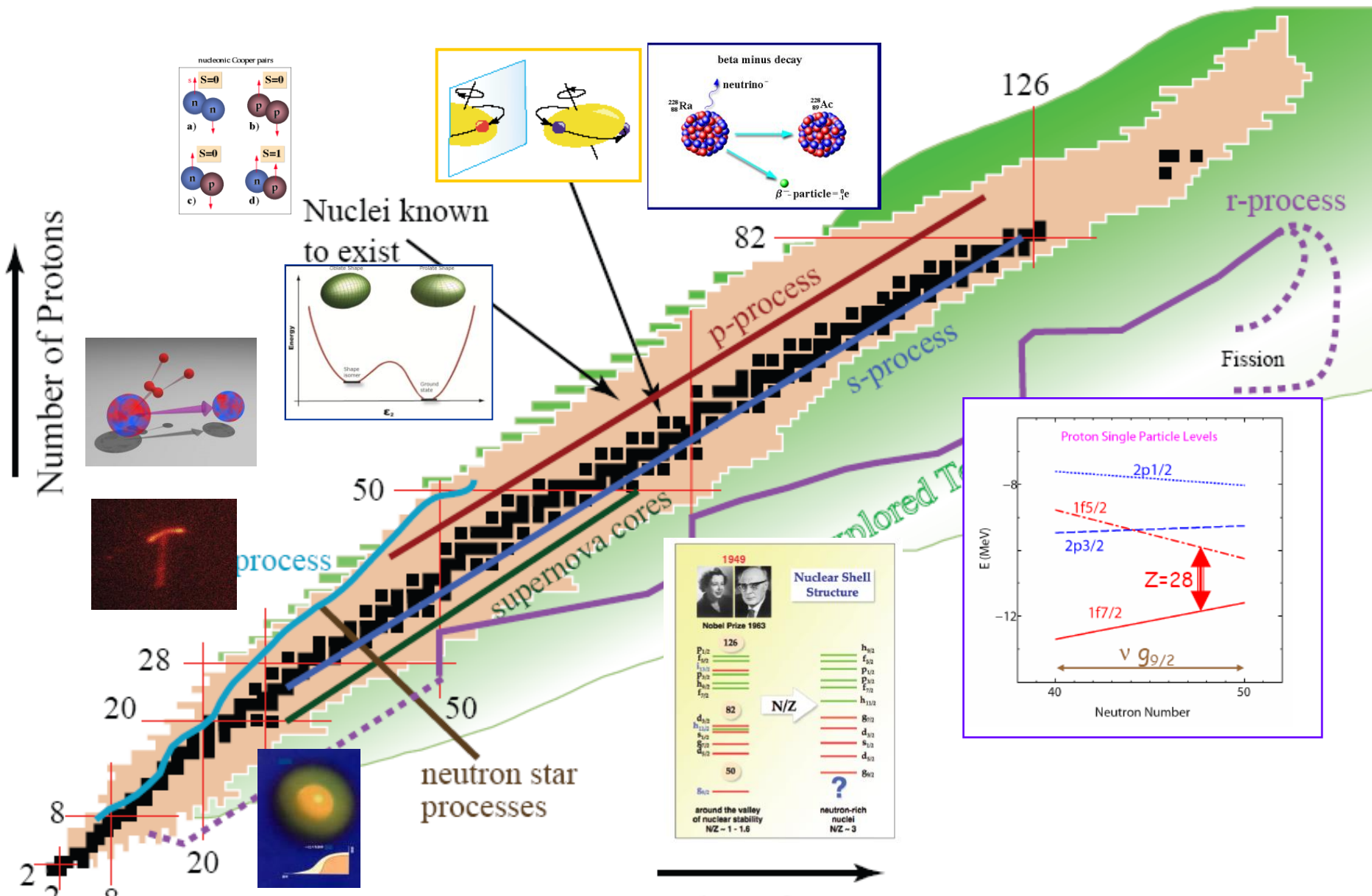
# Open questions

- How does the nuclear force depend on isospin?
- What are the limits of existence for bound nuclei?



- Which are the properties of exotic nuclei at the limits of binding?
- What's new? collective motion, shapes, decay modes?

# Shell evolution far from stability



# Origin of monopole drifts

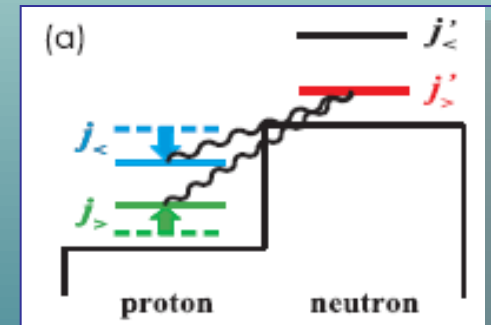
Explaining, reproducing and predicting shell structure far from stability

- proton-neutron spin-flip interaction

$$V_{\sigma\tau} = \tau \cdot \tau \sigma \cdot \sigma f_{\sigma\tau}(r)$$

- tensor force  $V_T = \tau \cdot \tau \left( [\sigma \cdot \sigma]^{(2)} \cdot Y^{(2)} \right) f(r)$

- three-body forces



T. Otsuka et al., PRL 95 (2005) 232502



# The effective interaction

A schematic (simplified) view

$$H = H_m + H_M$$

monopole      Multipole

 $H_m$ 

- “unperturbed” energy of the different configurations in which the valence nucleons are distributed
- determines the single particle energies or ESPE
- dominant role far from stability

 $H_M$ 

- correlations
- mixing of configurations
- coherence
- energy gains



# Understanding monopole effects

The monopole matrix element of an operator  $V$  can be written as

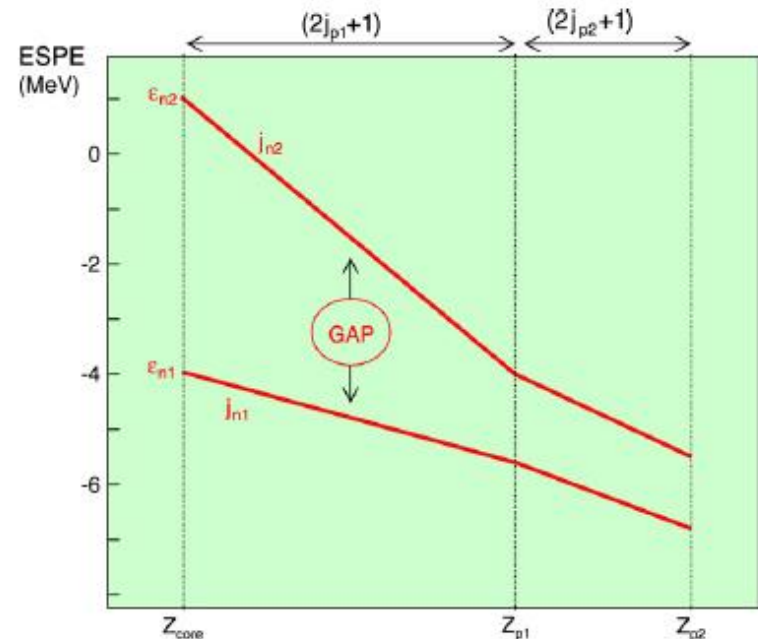
$$v_{j,j'} = \frac{\sum_{m,m'} \langle j_p m j_n m' | V | j m j' m' \rangle}{\sum_{m,m'} 1}$$

As the orbit  $j'$  is occupied, the single-particle energy of an orbit  $j$ ,  $e_j$ , is changed linearly by

$$e_j = v_{j,j'} n_{j'}$$

T. Otsuka et al.,  
PRL 104, 012501 (2010)

O. Sorin, M.-G. Porquet / Progress in Particle and Nuclear Physics 61 (2008) 602-673

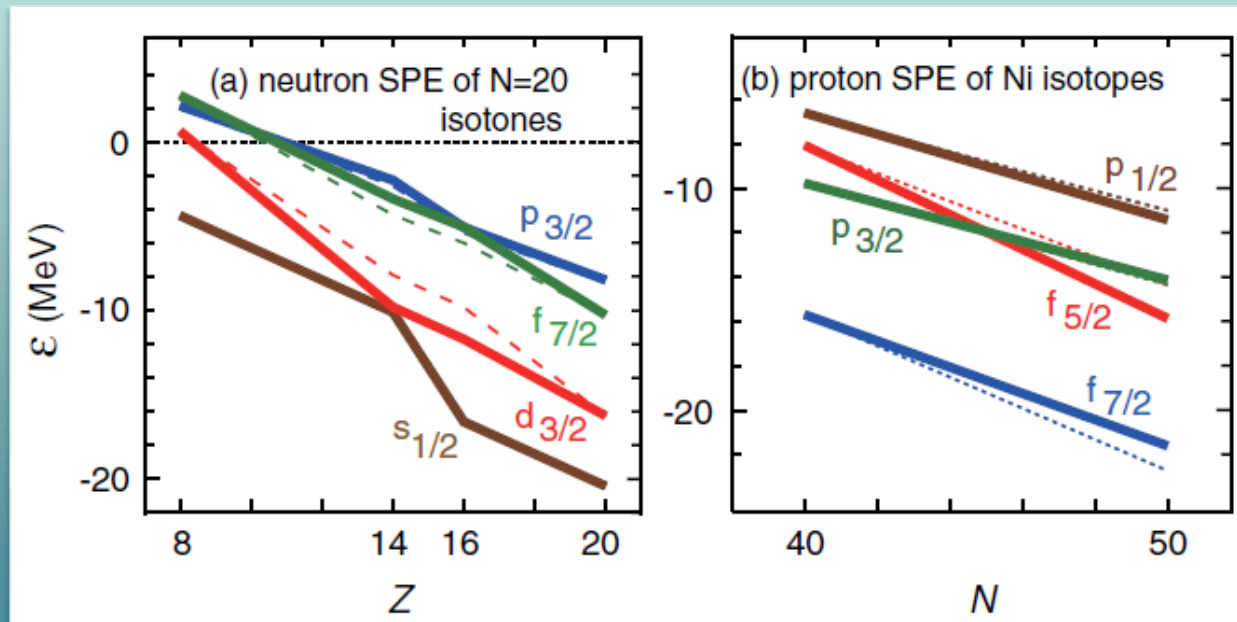


# Effects of the tensor force on the spe

Shell model calculations using a schematical potential  $V_{MU}$



only central  
central + tensor

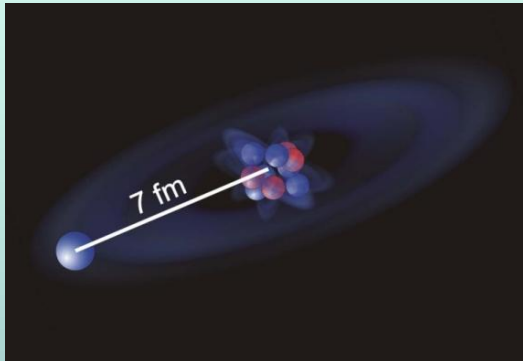


T. Otsuka et al.,  
PRL 104, 012501 (2010)





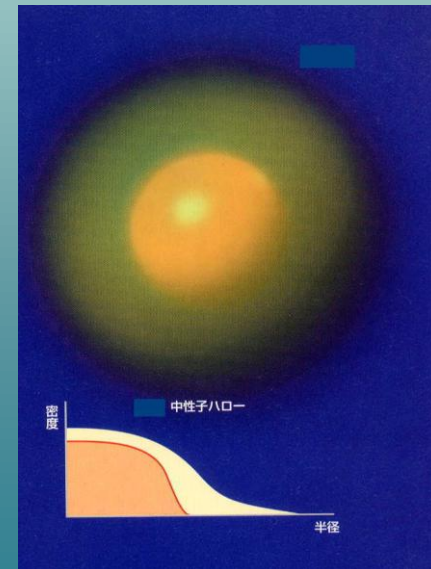
# The islands of inversion (N=8)



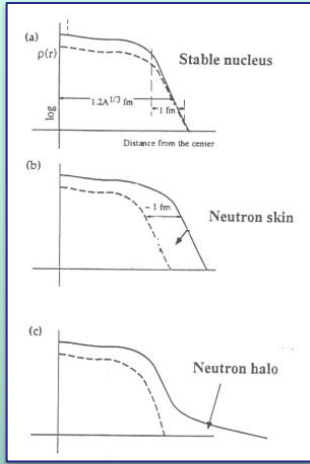
At N=8 the shell gap vanishes for very neutron rich nuclei.

The ground state of  $^{11}\text{Be}$  is the “intruder”  $1/2^+$ , the “normal” negative parity state lies at  $\sim 300$  keV.

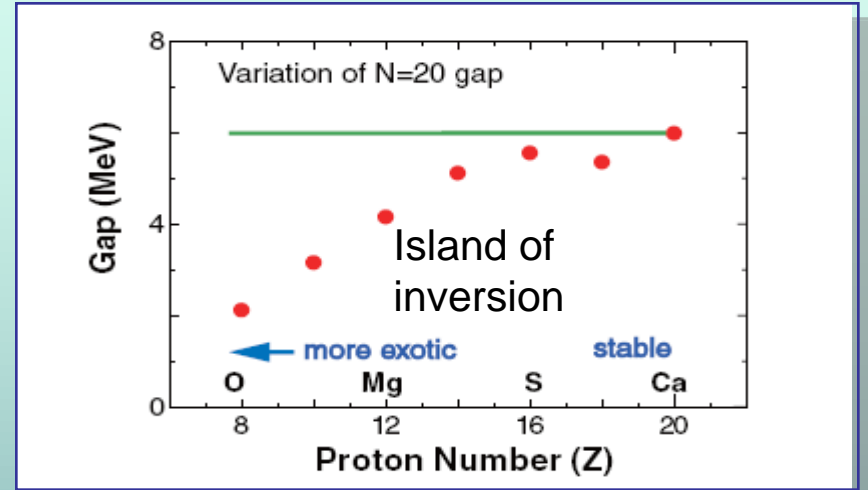
The weakly bound neutron/s occupy a low  $\ell$  orbit, giving rise to the halo



# The islands of inversion (N=20)



RIBF @ RIKEN  
 $^{31}\text{Ne}$  the heaviest  
 neutron halo system



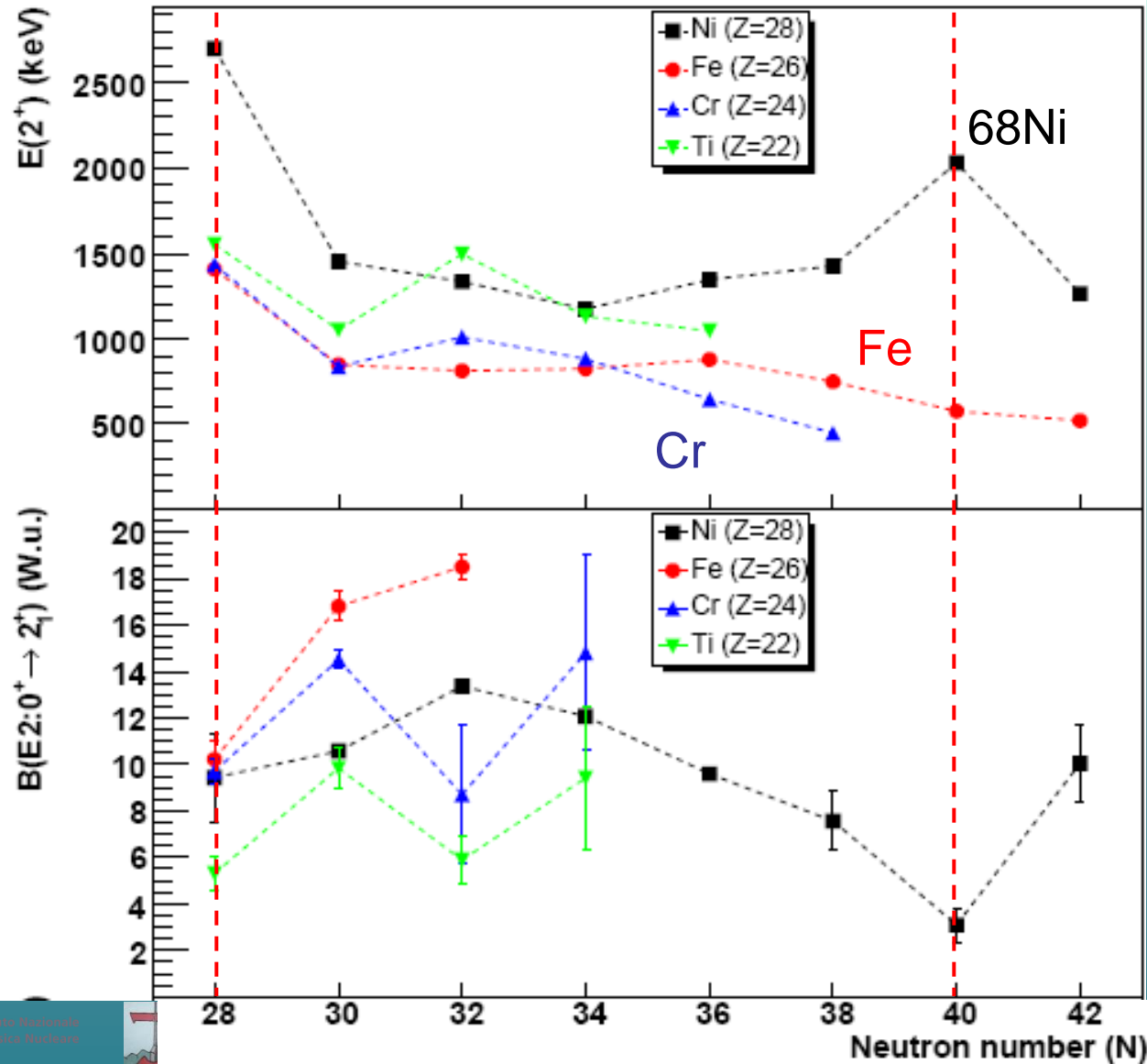
T. Otsuka EPJ S. Top. 156, 169 (2008)

The last neutron occupies probably the  $2p_{3/2}$  ( $S_n \leq 800$  keV)  
 It is suggested to form a halo

T. Nakamura et al., Phys. Rev. Lett. 103, 262501 (2009)



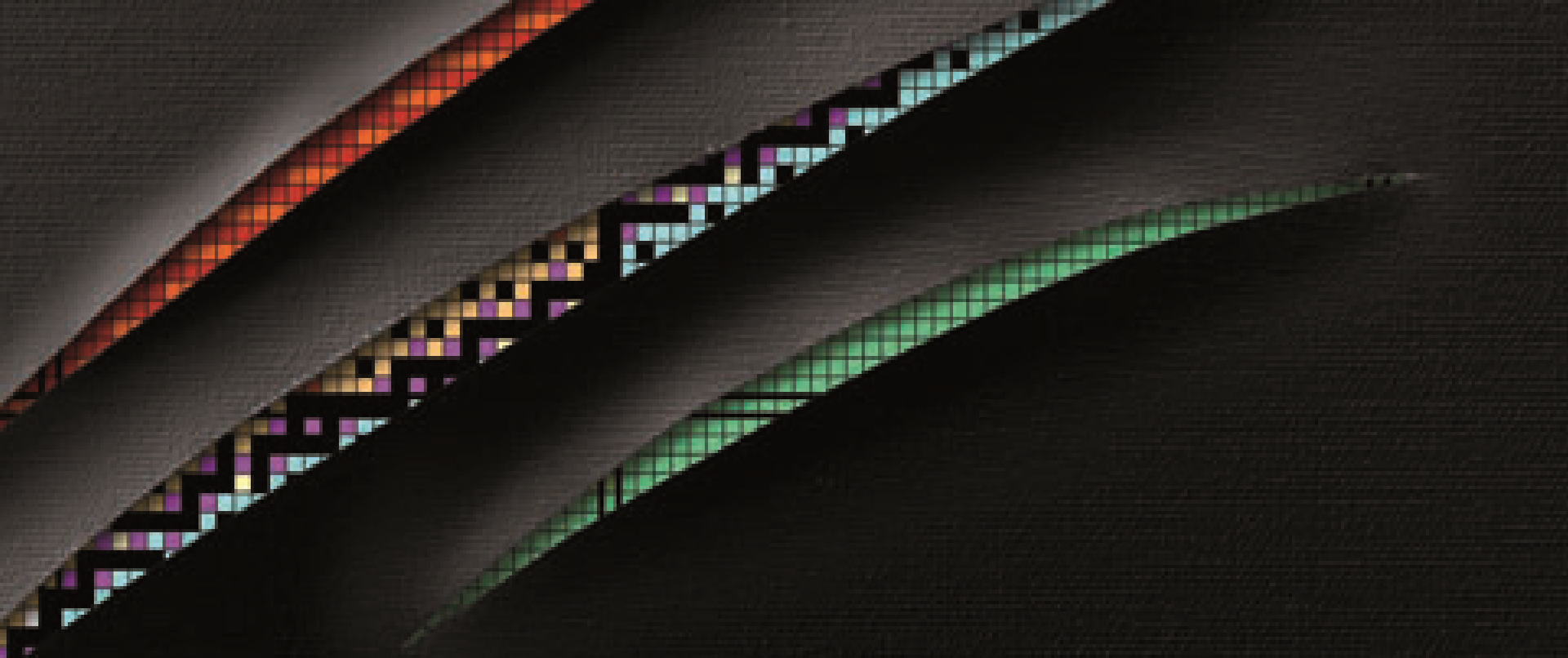
# The islands of inversion (N=40?)



INF

Institute for Nuclear and Particle Physics

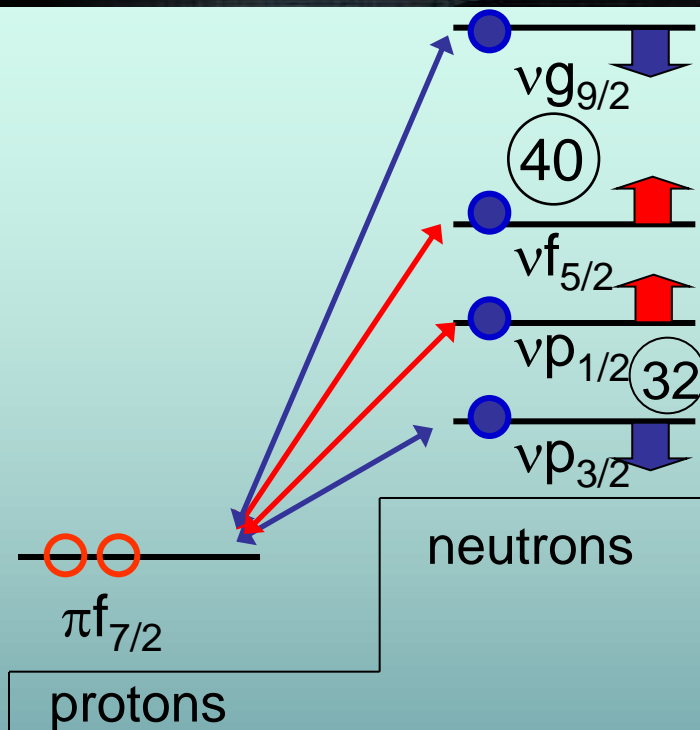
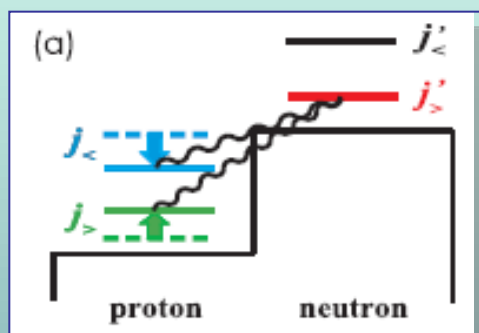




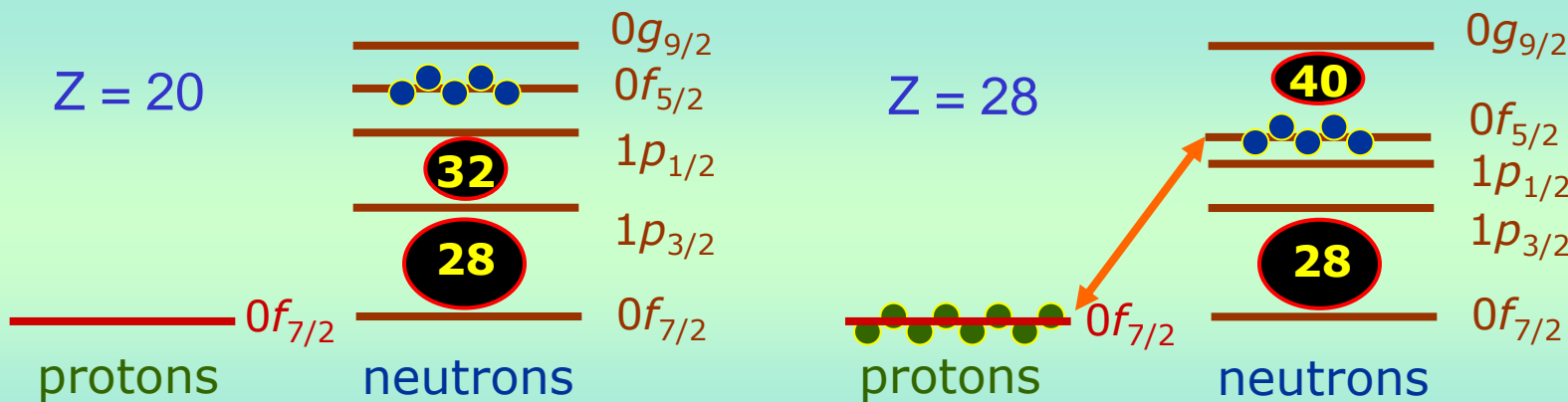
The new region of  
deformation at  $N \sim 40$ :  
Cr, Fe and Co isotopic chains

# Neutron excess and shell migration

$$V_T = \tau \cdot \tau \left( [\sigma \cdot \sigma]^{(2)} \cdot Y^{(2)} \right) f(r)$$

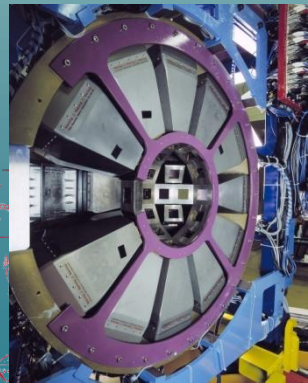
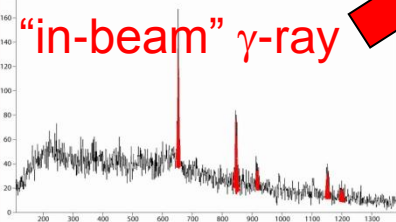
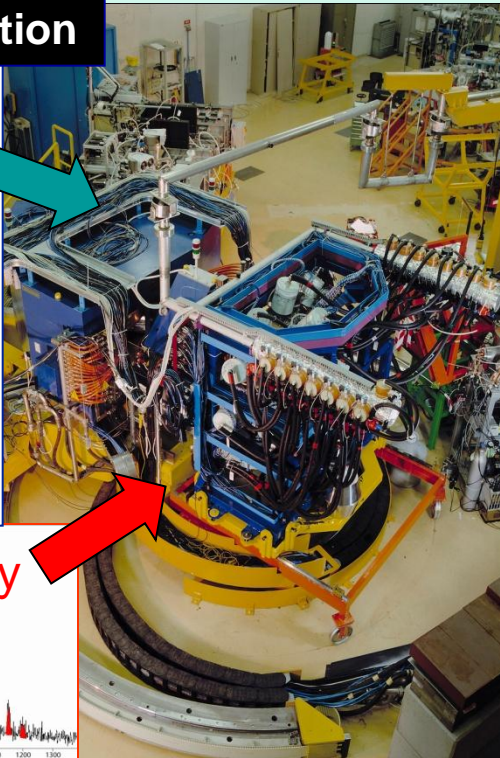
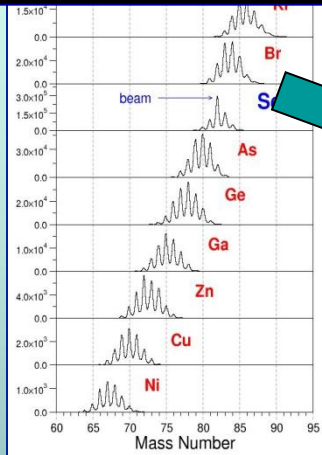


T. Otsuka et al., PRL 95 (2005) 232502



# Studying the shape evolution

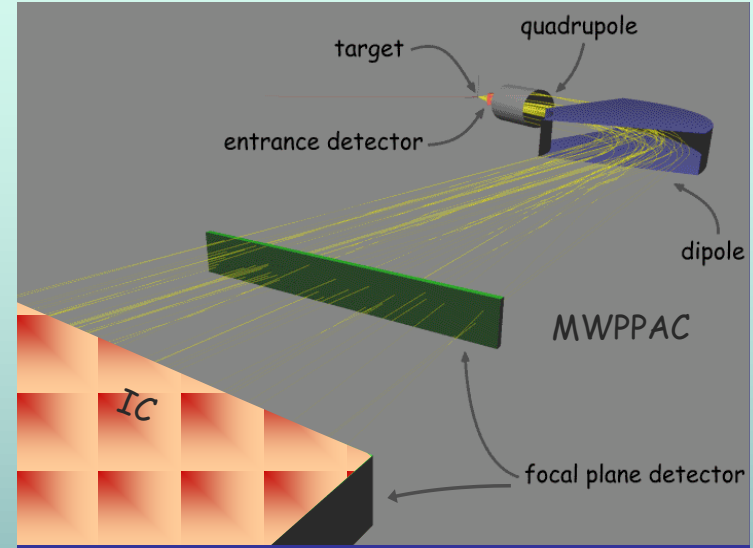
## A & Z identification



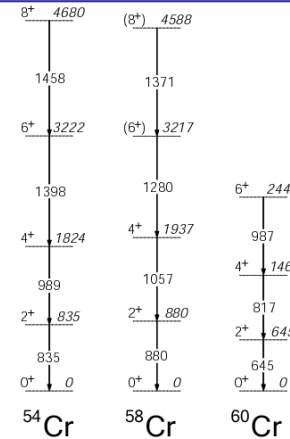
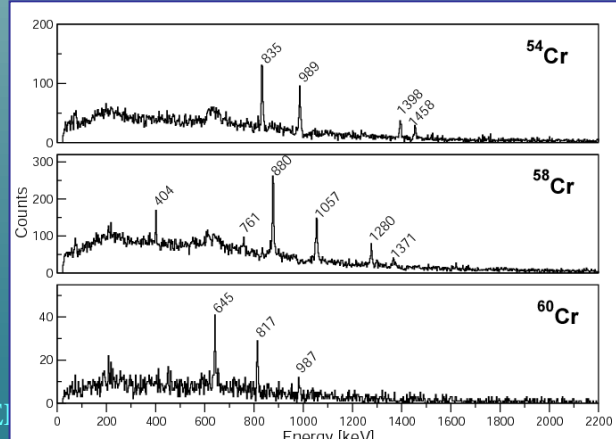
25 Euroball Clover detectors  
for  $E_\gamma = 1.3\text{MeV}$   
Efficiency  $\sim 3\%$   
Peak/Total  $\sim 45\%$   
FWHM  $\sim 10\text{keV}$   
(at  $v/c = 10\%$ )



Silvia Lenzi - JAPAN-ITALY E



## CLARA+PRISMA @ Legnaro



# $^{58}\text{Cr}$ and the shape phase transition critical point

VOLUME 85, NUMBER 17      PHYSICAL REVIEW LETTERS      23 OCTOBER 2000

## Dynamic Symmetries at the Critical Point

F. Iachello

Center for Theoretical Physics, Sloane Laboratory, Yale University, New Haven, Connecticut 06520-8120  
(Received 8 May 2000)

TABLE 1. Excitation energies of the E(5) symmetry.

	$\xi = 1$	$\xi = 2$	$\xi = 3$	$\xi = 4$
$\tau = 0$	0	2.02	7.58	13.64
$\tau = 1$	1		11	16.93
$\tau = 2$	2.20		86	20.44
$\tau = 3$	3.59		81	24.16
$\tau = 4$	5.17			

$^{58}\text{Cr}$ :

$$E_{4^+}/E_{2^+} = 2.20$$

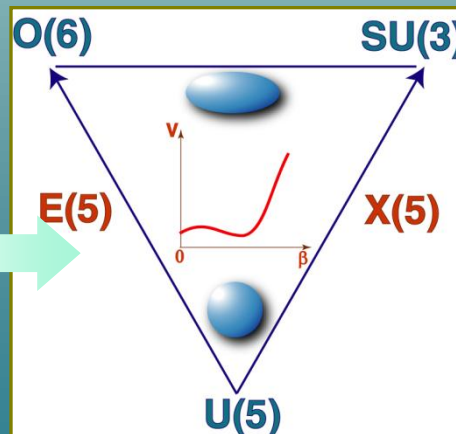
$$E_{6^+}/E_{2^+} = 3.65$$

$$E_{8^+}/E_{2^+} = 5.31$$

8+	4680	4550	4442	4447	4743	4946
6+	3219	3159	3130	2990	3188	3299
4+	1937	1936	1937	1770	1885	2051
2+	880	880	882	880	870	1102
0+	0	0	0	0	0	0
EXP.	E(5)	IBA	KB3G	FPD6	GXPF1	

Marginean et al.  
Phys. Lett. B 633  
(2006)696

$^{58}\text{Cr}$

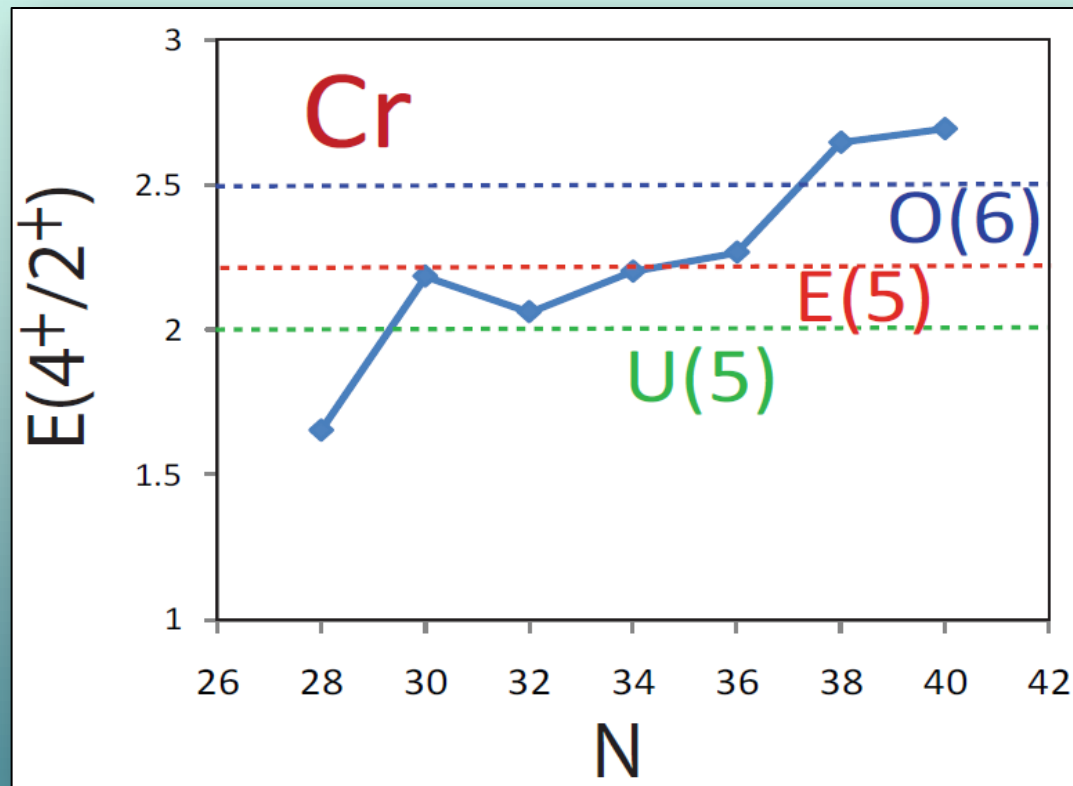


A possible bridge between shell model, algebraic and analytical approaches

Need to measure transition probabilities



# Evolution of Cr isotopes



Istituto Nazionale  
di Fisica Nucleare





# Cr isotopic chain: data

Eur. Phys. J. A **16**, 55–61 (2003)  
DOI 10.1140/epja/i2002-10069-9

THE EUROPEAN  
PHYSICAL JOURNAL A

## beta decay @ GANIL

### New region of deformation in the neutron-rich $^{60}\text{Cr}_{24}$ and $^{62}\text{Cr}_{38}$

O. Sorlin<sup>1,a</sup>, C. Donzau<sup>1</sup>, F. Nowacki<sup>2</sup>, J.C. Angélique<sup>3</sup>, F. Azaiez<sup>1</sup>, C. Bourgeois<sup>1</sup>, V. Chisté<sup>1</sup>, Z. Dlouhy<sup>4</sup>, S. Grévy<sup>5</sup>, D. Guillemaud-Mueller<sup>1</sup>, F. Ibrahim<sup>1</sup>, K.-L. Kratz<sup>6</sup>, M. Lewitowicz<sup>6</sup>, S.M. Lukanov<sup>7</sup>, J. Mrasek<sup>4</sup>, Yu.-E. Penionzhkevich<sup>7</sup>, F. de Oliveira Santos<sup>6</sup>, B. Pfeiffer<sup>3</sup>, F. Pougheon<sup>1</sup>, A. Poves<sup>8</sup>, M.G. Saint-Laurent<sup>9</sup>, and M. Stanoiu<sup>6</sup>

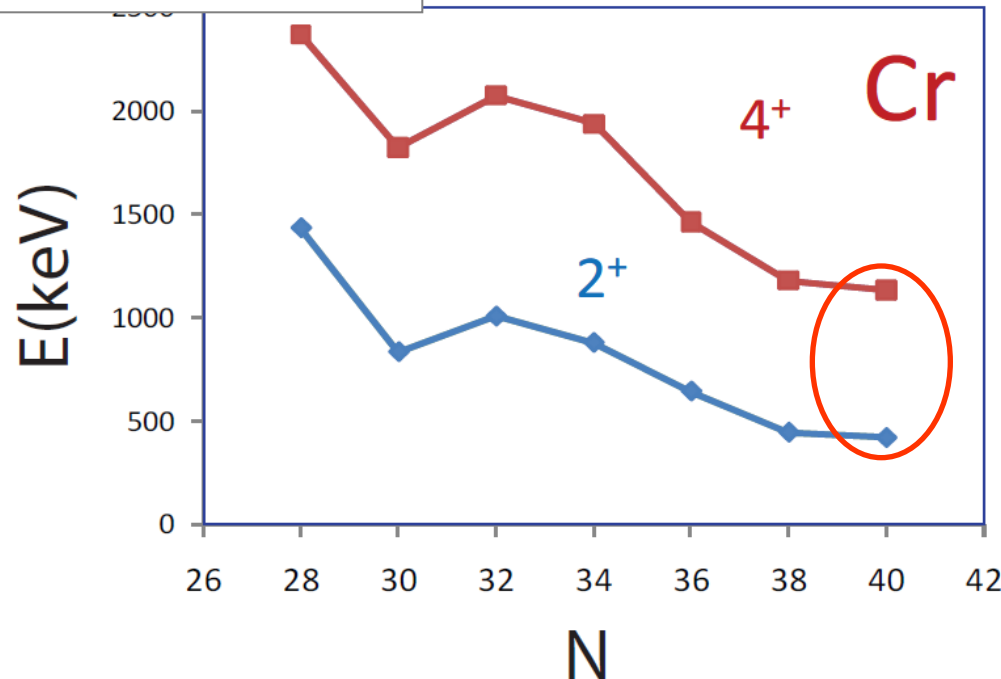
PRL **102**, 012502 (2009)

PHYSICAL REVIEW LETTERS

week ending  
9 JANUARY 2009

### Development of Large Deformation in $^{62}\text{Cr}$

N. Aoi,<sup>1</sup> E. Takeshita,<sup>1,2</sup> H. Suzuki,<sup>3</sup> S. Takeuchi,<sup>1</sup> S. Ota,<sup>4</sup> H. Baba,<sup>1</sup> S. Bishop,<sup>1</sup> T. Fukui,<sup>4</sup> Y. Hashimoto,<sup>5</sup> H. J. Ong,<sup>6</sup> E. Ideguchi,<sup>7</sup> K. Ieki,<sup>8</sup> N. Imai,<sup>8</sup> M. Ishihara,<sup>1</sup> H. Iwasaki,<sup>6</sup> S. Kanno,<sup>2</sup> Y. Kondo,<sup>5</sup> T. Kubo,<sup>1</sup> K. Kurita,<sup>2</sup> K. Kusaka,<sup>1</sup> T. Minemura,<sup>8</sup> T. Motobayashi,<sup>1</sup> T. Nakabayashi,<sup>5</sup> T. Nakamura,<sup>5</sup> T. Nakao,<sup>6</sup> M. Niikura,<sup>7</sup> T. Okumura,<sup>5</sup> T. K. Ohnishi,<sup>6</sup> H. Sakurai,<sup>6</sup> S. Shimoura,<sup>7</sup> R. Sugo,<sup>2</sup> D. Suzuki,<sup>6</sup> M. K. Suzuki,<sup>6</sup> M. Tamaki,<sup>7</sup> K. Tanaka,<sup>1</sup> Y. Togano,<sup>2</sup> and K. Yamada<sup>1</sup>



(p,p') @ RIKEN

### inelastic scattering

@ NSCL (MSU)

PHYSICAL REVIEW C **81**, 051304(R) (2010)

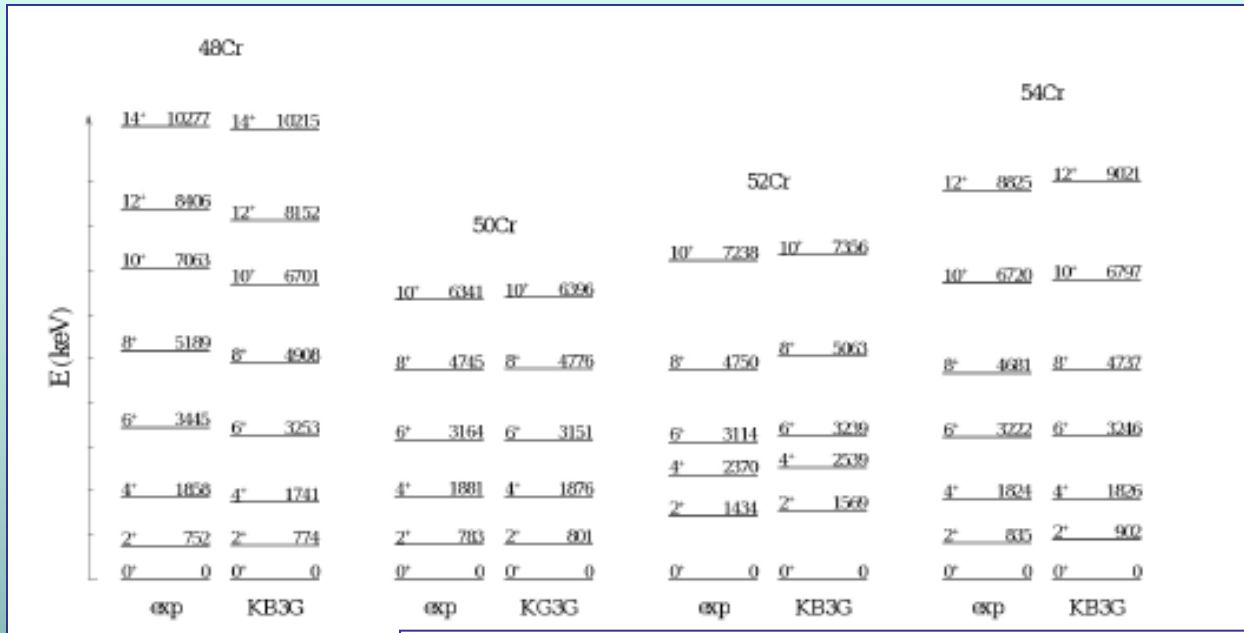
RAPID COMMUNICATIONS

### Collectivity at $N = 40$ in neutron-rich $^{64}\text{Cr}$

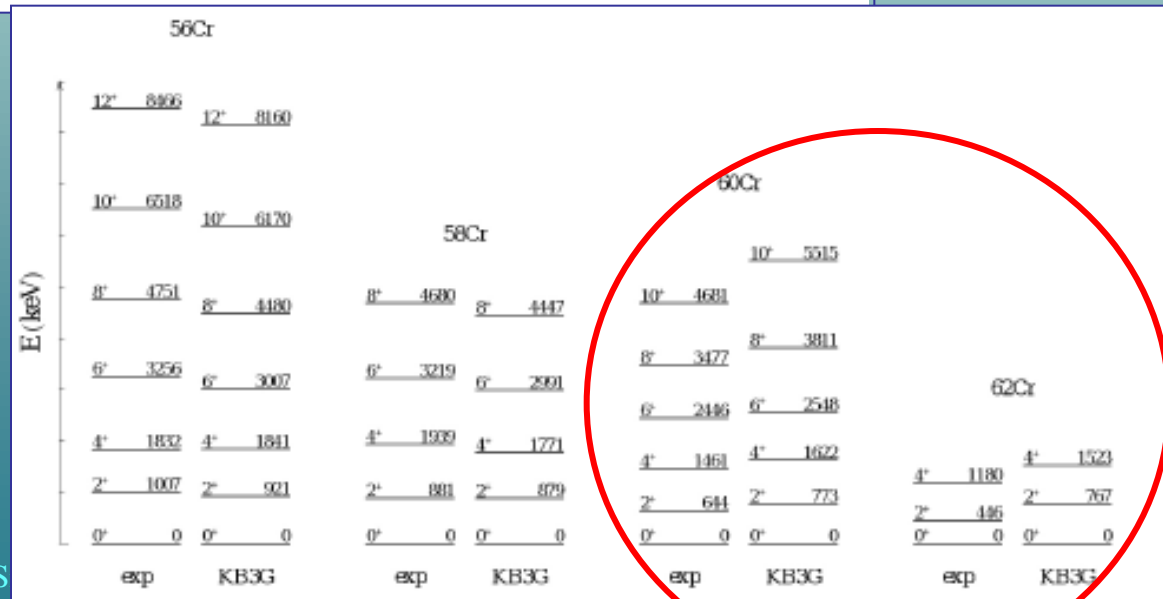
A. Gade,<sup>1,2</sup> R. V. F. Janssens,<sup>3</sup> T. Baugher,<sup>1,2</sup> D. Bazin,<sup>1</sup> B. A. Brown,<sup>1,2</sup> M. P. Carpenter,<sup>3</sup> C. J. Chiara,<sup>3,4</sup> A. N. Deacon,<sup>5</sup> S. J. Freeman,<sup>5</sup> G. F. Grinyer,<sup>1</sup> C. R. Hoffman,<sup>3</sup> B. P. Kay,<sup>3</sup> F. G. Kondev,<sup>6</sup> T. Lauritsen,<sup>3</sup> S. McDaniel,<sup>1,2</sup> K. Meierbachtol,<sup>1,7</sup> A. Ratkiewicz,<sup>1,2</sup> S. R. Stroberg,<sup>1,2</sup> K. A. Walsh,<sup>1,2</sup> D. Weisshaar,<sup>1</sup> R. Winkler,<sup>1</sup> and S. Zhu<sup>3</sup>



# The Chromium Isotopic chain



Calculations in the fp shell only



# Shell model for heavier Cr isotopes

## Proton inelastic scattering in inverse kinematics

PRL 102, 012502 (2009)

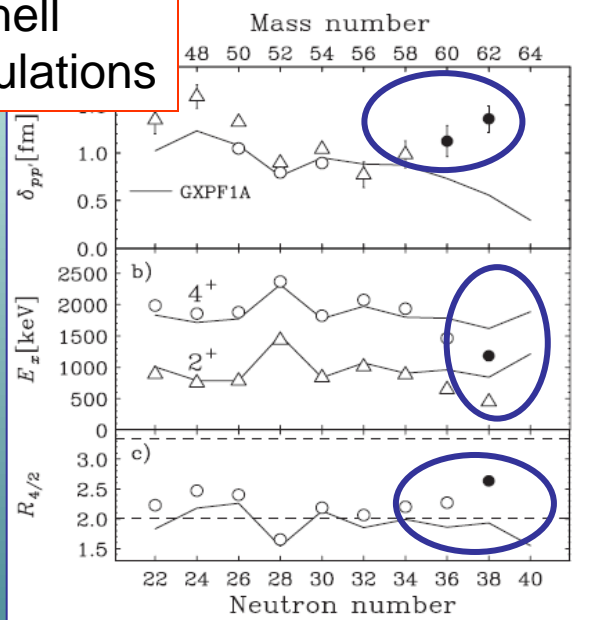
PHYSICAL REVIEW LETTERS

week ending  
9 JANUARY 2009

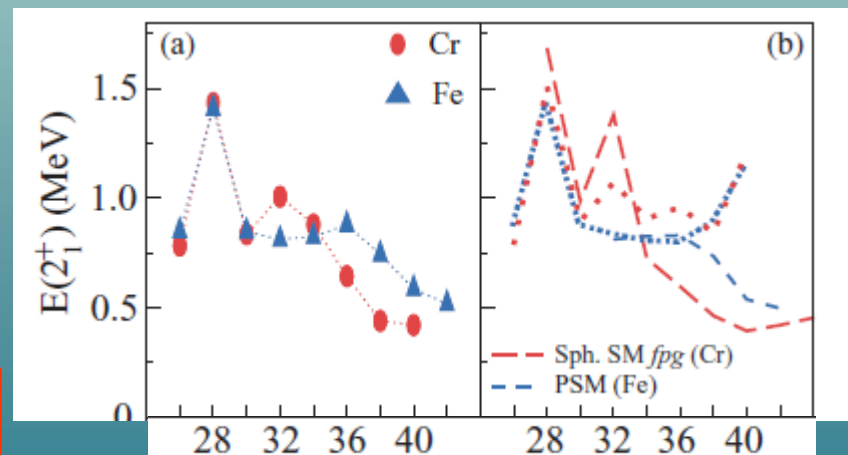
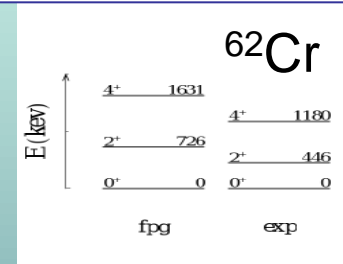
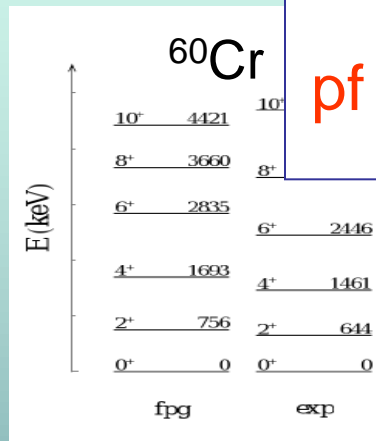
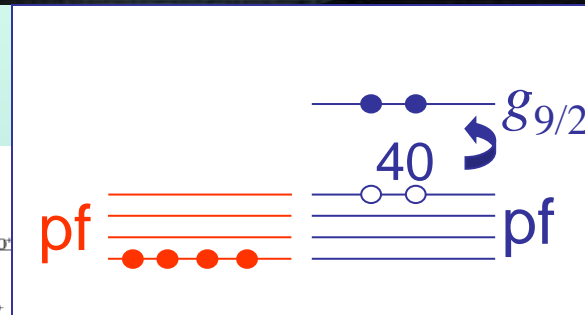
### Development of Large Deformation in $^{62}\text{Cr}$

N. Aoi,<sup>1</sup> E. Takeshita,<sup>1,2</sup> H. Suzuki,<sup>3</sup> S. Takeuchi,<sup>1</sup> S. Ota,<sup>4</sup> H. Baba,<sup>1</sup> S. Bishop,<sup>1</sup> T. Fukui,<sup>4</sup> Y. Hashimoto,<sup>5</sup> H. J. Ong,<sup>6</sup> E. Ideguchi,<sup>7</sup> K. Ieki,<sup>2</sup> N. Imai,<sup>8</sup> M. Ishihara,<sup>1</sup> H. Iwasaki,<sup>6</sup> S. Kanno,<sup>2</sup> Y. Kondo,<sup>5</sup> T. Kubo,<sup>1</sup> K. Kurita,<sup>2</sup> K. Kusaka,<sup>1</sup> T. Minemura,<sup>8</sup> T. Motobayashi,<sup>1</sup> T. Nakabayashi,<sup>5</sup> T. Nakamura,<sup>5</sup> T. Nakao,<sup>6</sup> M. Niikura,<sup>7</sup> T. Okumura,<sup>5</sup> T. K. Ohnishi,<sup>6</sup> H. Sakurai,<sup>6</sup> S. Shimoura,<sup>7</sup> R. Sugo,<sup>2</sup> D. Suzuki,<sup>6</sup> M. K. Suzuki,<sup>6</sup> M. Tamaki,<sup>7</sup> K. Tanaka,<sup>1</sup> Y. Togano,<sup>2</sup> and K. Yamada<sup>1</sup>

pf-shell  
calculations

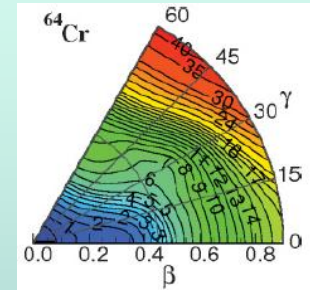
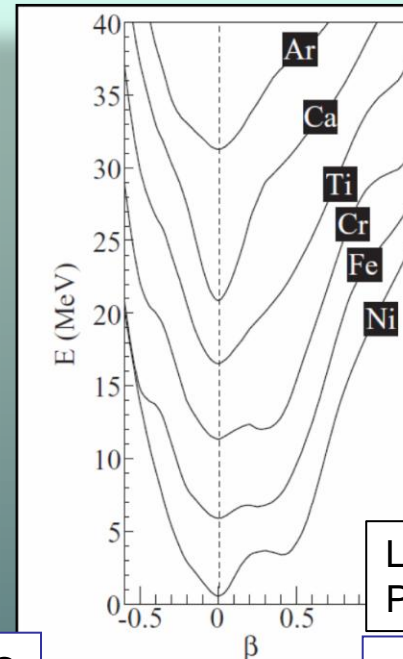
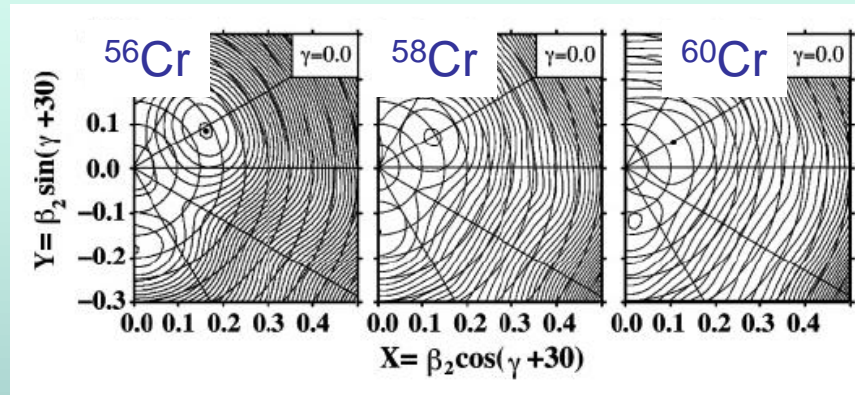


The energy levels at  $N=40$  cannot be described within the *pf* or *fpg* space



A.Gade et al., PRC 81, 051304(R) (2010)

# Collectivity at $N \sim 40, Z < 28$

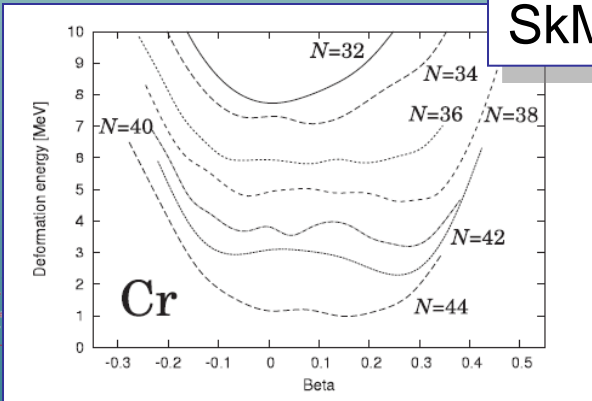


N=40 isotones  
HFB+GCM  
Gogny force

L. Gauthier et al.,  
PRC 80 064313(2009)

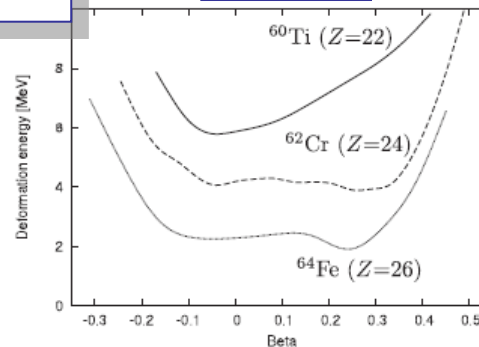
Ground-state potential energy surfaces (TRS). Cr isotopes seem to exhibit  $\gamma$  softness for large N values

S. Zhu et al., PRC 74, 064315 (2006)

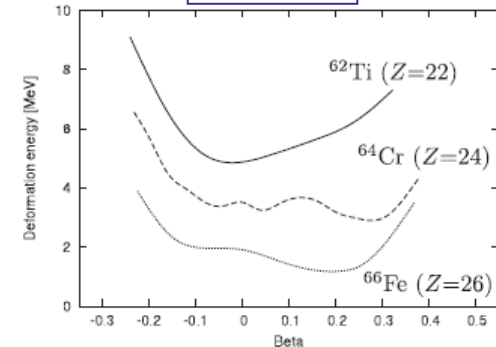


SkM\*-HFB

N=38

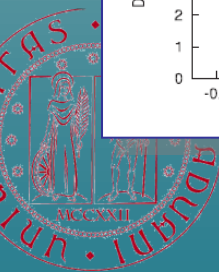


N=40



H. Oba and M. Matsuo, Prog. Theo. Phys. 120, 143 (2008)

Silvia Lenzi - JAPAN-ITALY EFES Workshop, Torino, 6-8 September 2010



INFN  
Istituto Nazionale  
di Fisica Nucleare



# Fe isotopes and the shell model

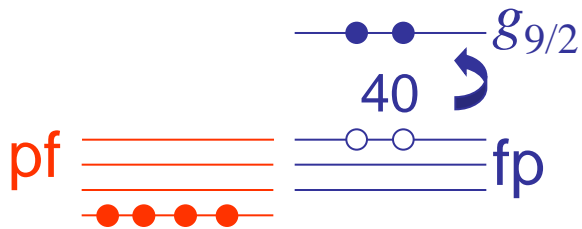
S. Lunardi *et al.*,  
Phys. Rev. C **76**, 034303 (2007)

## Shell model calculations

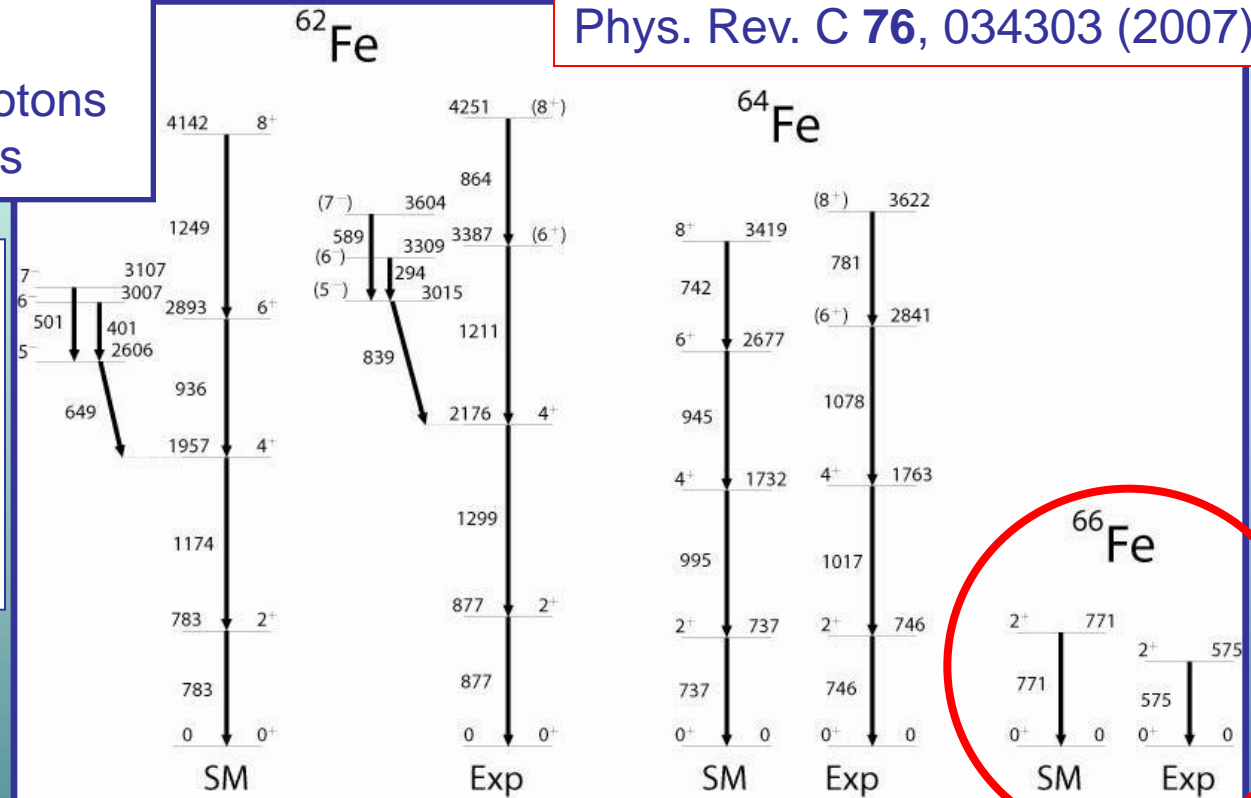
Core  $^{48}\text{Ca}$

valence space: full  $fp$  for protons

$p_{3/2}, f_{5/2}, p_{1/2}, g_{9/2}$  for neutrons



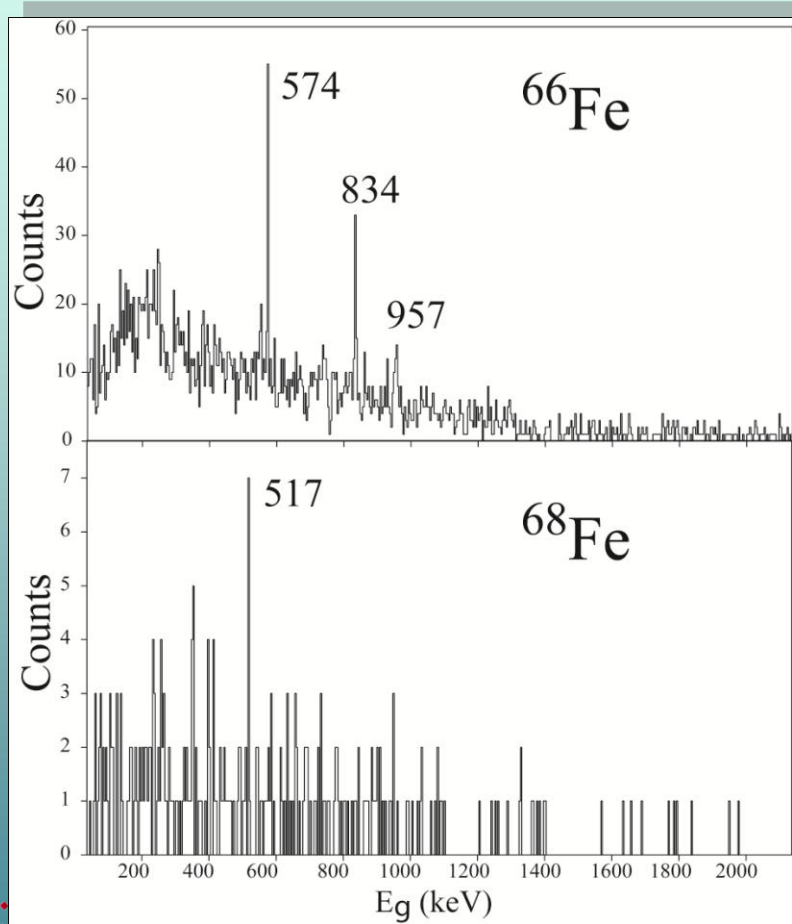
$fp$  Interaction described in  
O. Sorlin *et al.*, PRL **88**,  
092501 (2002).



These calculations fail to describe the  
collectivity in the  $N=40$   $^{66}\text{Fe}$  isotope



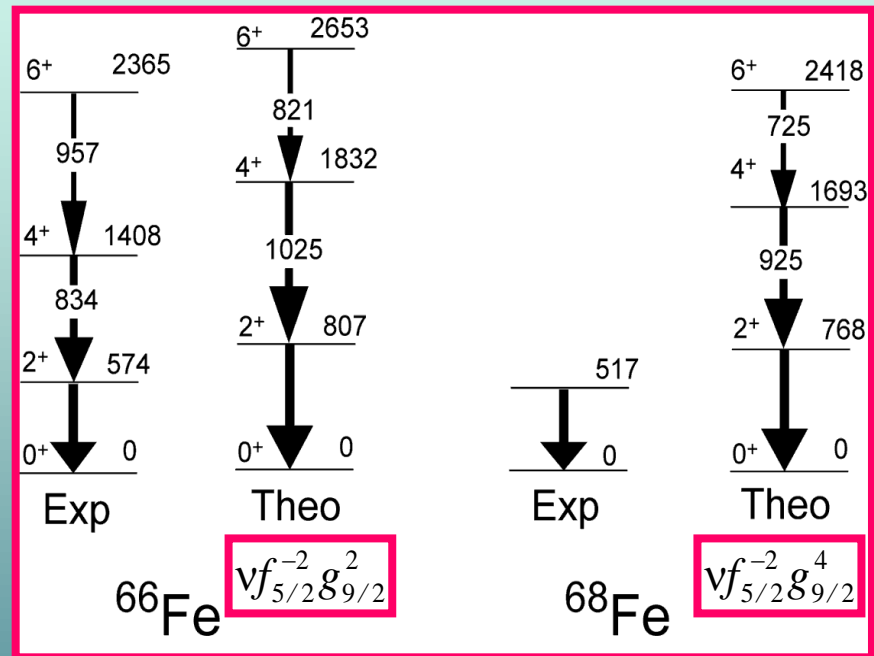
# Beyond N=40



SML et al.,  
LNL Ann. Rep. 2008

N=40

N=42



**Shell model calculations**

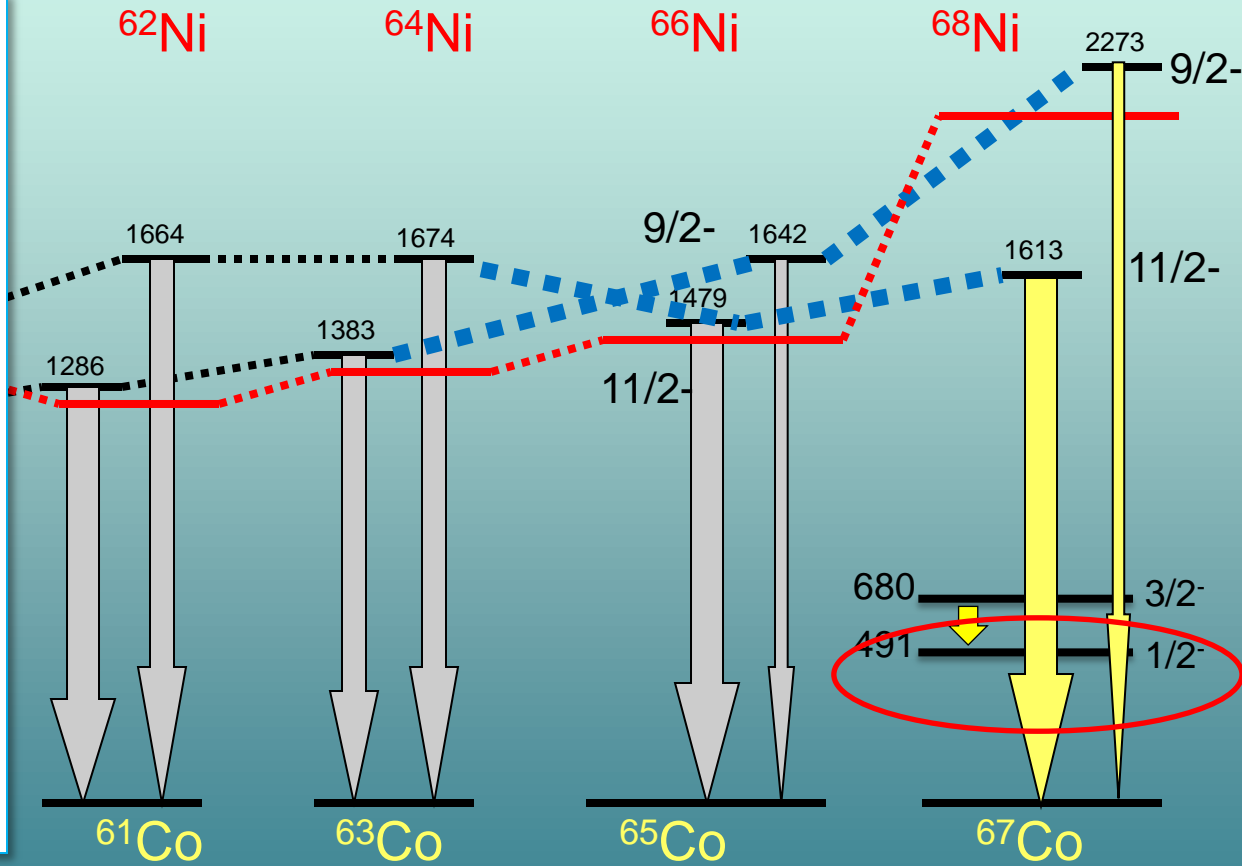
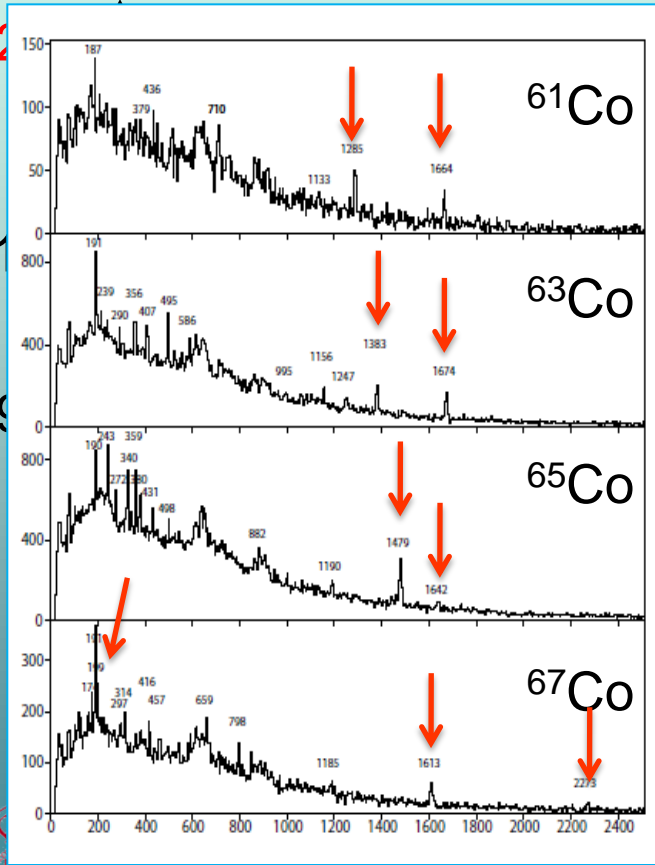
Core  $^{48}\text{Ca}$

valence space: full  $fp$  for protons

$p_{3/2}, f_{5/2}, p_{1/2}, g_{9/2}$  for neutrons



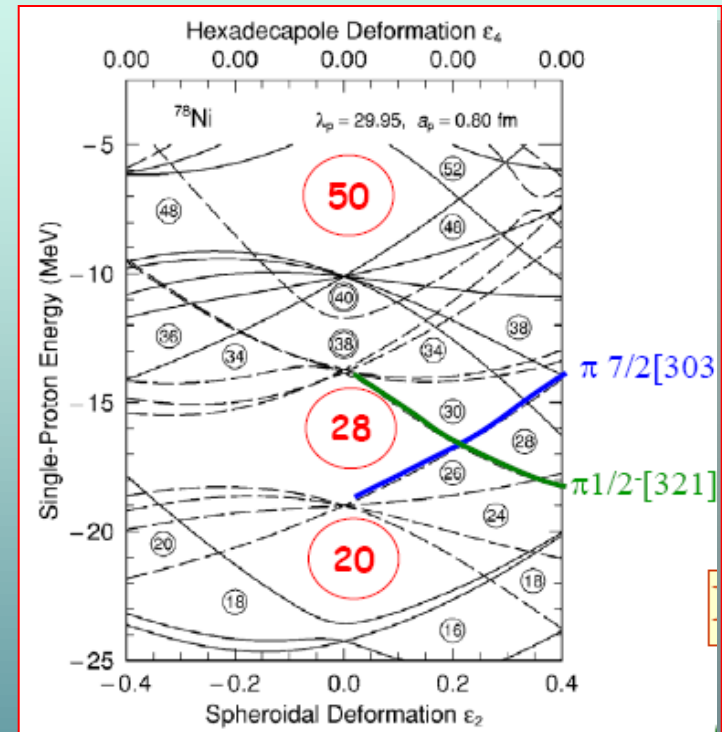
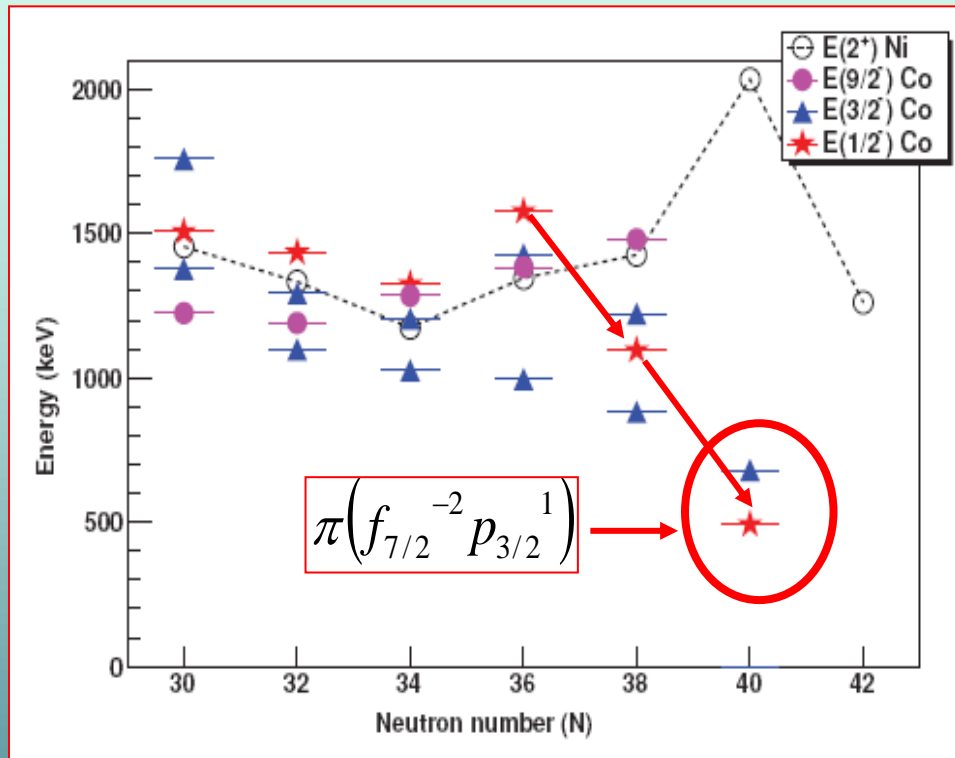
# Evolution of yrast levels in Co isotopes



65Co: D.Pawels et al.,  
Phys. Rev. C 79, 044309 (2009)

65-67Co: F. Recchia et al.,  
In preparation

# Proton intruder states and shape coexistence in $^{67}\text{Co}$



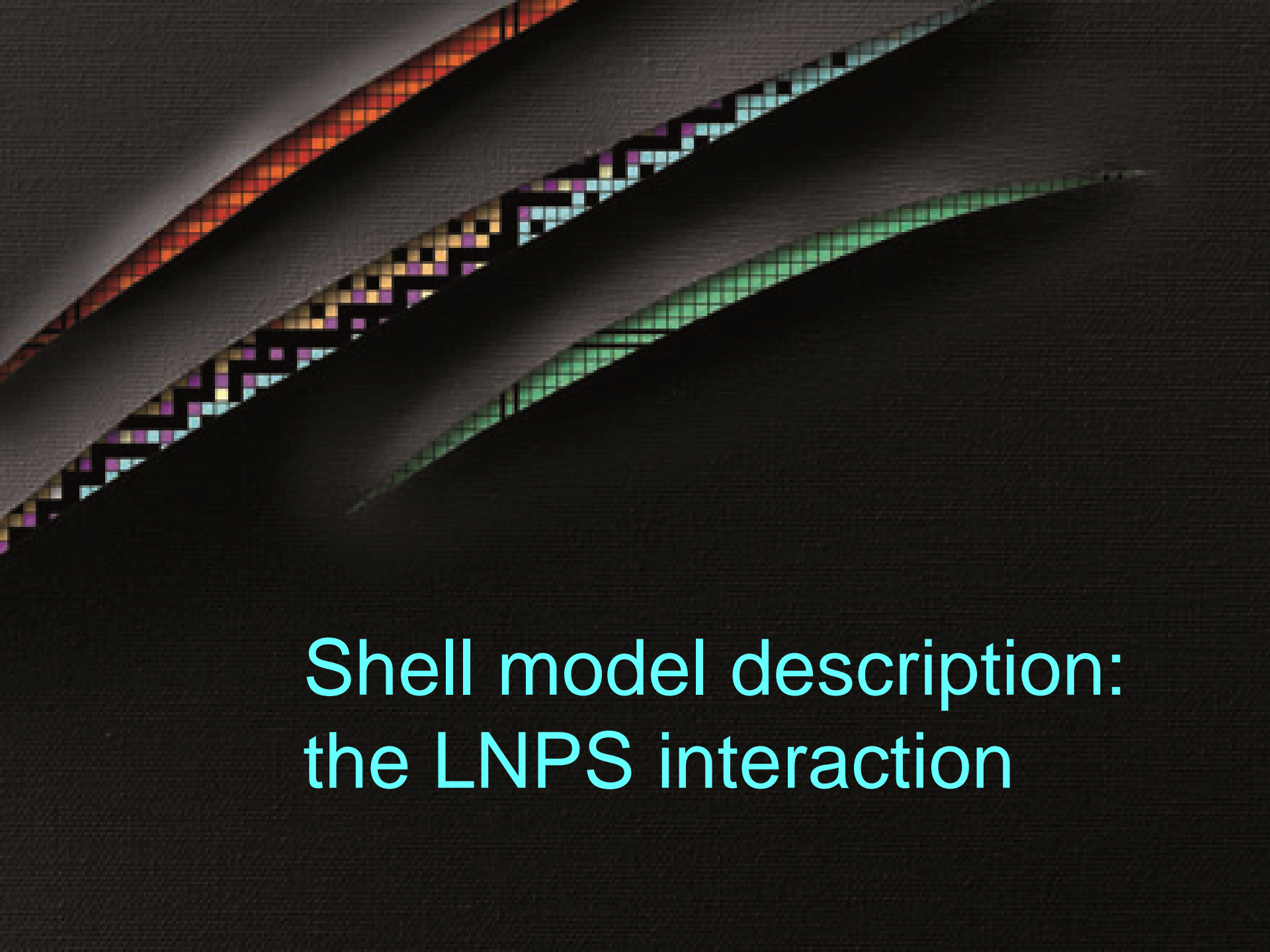
The  $1/2^-$  state lowers due to deformation increase at  $Z < 28$   $N = 40$

D. Pauwels et al., PRC 78, 041307 (2008)  
and PRC 79, 044309 (2009)

Courtesy D. Pauwels  
and P. Van Duppen

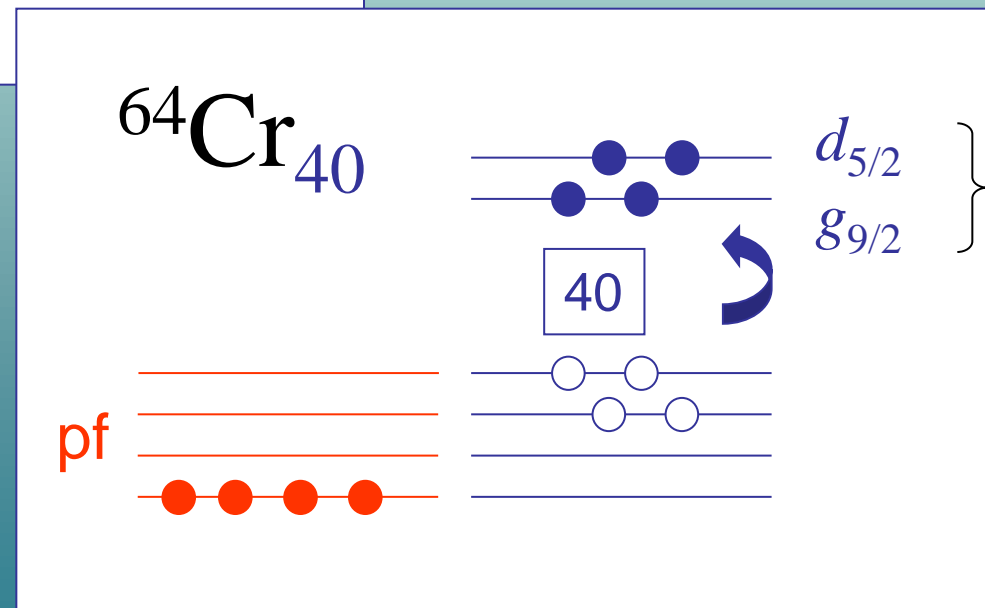
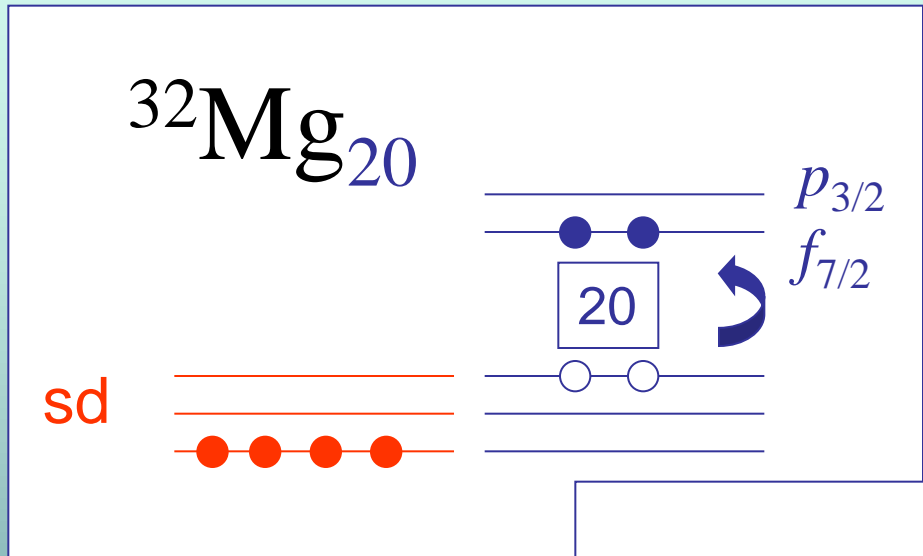




The background features three parallel diagonal bands of small, multi-colored squares (red, orange, yellow, purple, blue, green) set against a dark, textured grey background. The bands are slightly curved and create a sense of depth and movement.

# Shell model description: the LNPS interaction

# Islands of inversion



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# Building quadrupole collectivity

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PHYSICAL REVIEW C

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## Spherical shell model description of rotational motion

A. P. Zuker,<sup>1</sup> J. Retamosa,<sup>2</sup> A. Poves,<sup>2</sup> and E. Caurier<sup>1</sup>

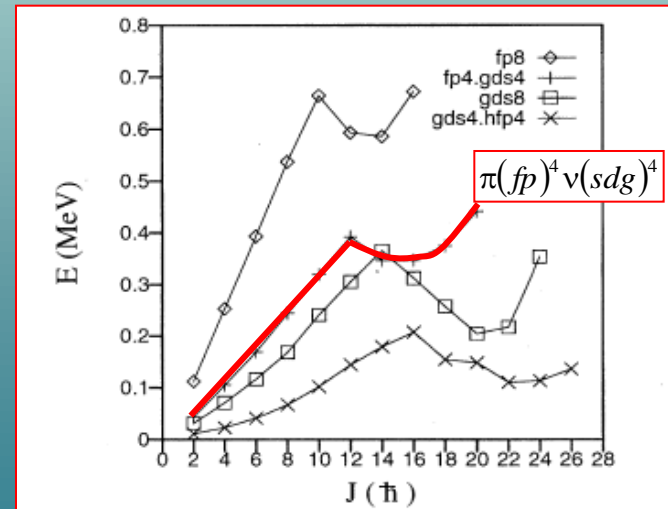
<sup>1</sup>*Physique Théorique, Bâtiment 40/1 CRN, Institut National de Physique Nucléaire et des Particules-CNRS/Université Louis Pasteur, Boîte Postale 28, F-67037 Strasbourg Cedex 2, France*

<sup>2</sup>*Departamento de Física Teórica, Universidad Autónoma de Madrid, E-28049 Madrid, Spain*

(Received 13 July 1994)

Exact diagonalizations with a realistic interaction show that configurations with four neutrons in a major shell and four protons in another—or the same—major shell, behave systematically as backbending rotors. The dominance of the  $q \cdot q$  component of the interaction is related to an approximate “quasi-SU3” symmetry. It is suggested that the onset of rotational motion in the rare earth nuclei is due to the promotion of the eight particle blocks to the major shells above the ones currently filling. Assuming a “pseudo-SU3” coupling for the particles in the lower orbits, it is possible to account remarkably well for the observed  $B(E2)$  rates at the beginning of the region.

Rotational features are determined by the interplay of the quadrupole force with the central field in the subspace spanned by a sequence of  $\Delta j = 2$  orbits that come lowest by the spin-orbit splitting.



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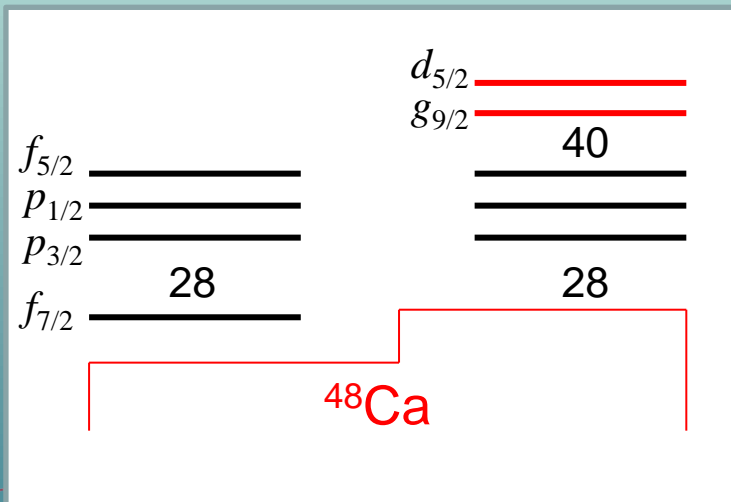
# The new LNPS interaction

LNPS interaction: renormalized realistic interaction  
+ monopole corrections

$^{48}\text{Ca}$  core

protons: full pf shell

neutrons:  $p_{3/2}, f_{5/2}, p_{1/2}, g_{9/2}, d_{5/2}$



- KB3gr for the pf-shell;
- renormalized G-matrix with monopole corrections for the remaining matrix elements involving the  $p_{3/2}$ ,  $p_{1/2}$ ,  $f_{5/2}$  and  $g_{9/2}$  neutron orbits;
- the G-matrix based on the Kahana-Lee-Scott potential for the matrix elements involving the  $d_{5/2}$  orbit;
- monopole corrections to reproduce the  $Z=28$  and  $N=50$  gaps in  $^{78}\text{Ni}$  based on data of neighboring nuclei



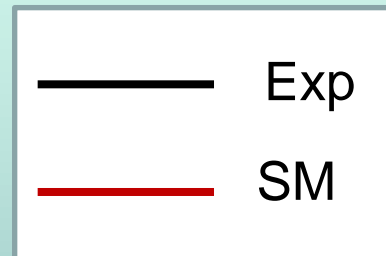
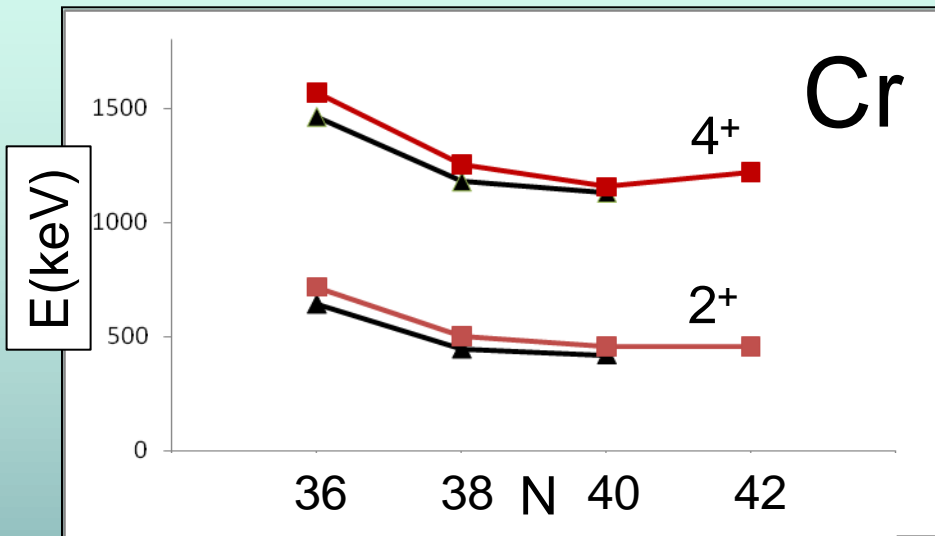
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SML, F. Nowacki, A. Poves and K. Sieja, 2010, in preparation

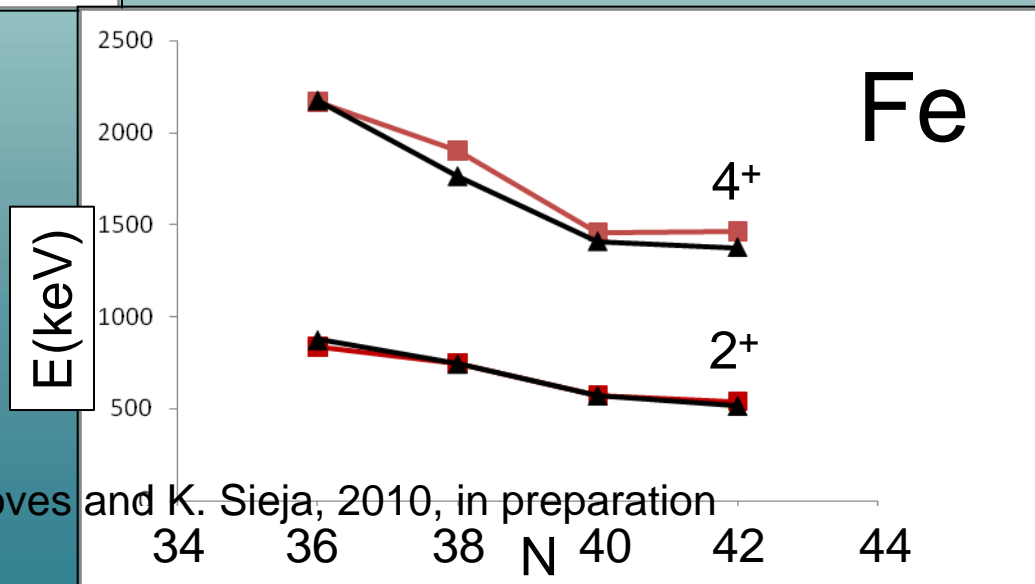
Silvia Lenzi - JAPAN-ITALY EFES Workshop, Torino, 6-8 September 2010

# Description of Cr and Fe around N=40



Calculations with the LNPS interaction and the code Antoine:

- up to 14p-14h excitations.
- matrix dimensions up to  $10^{10}$

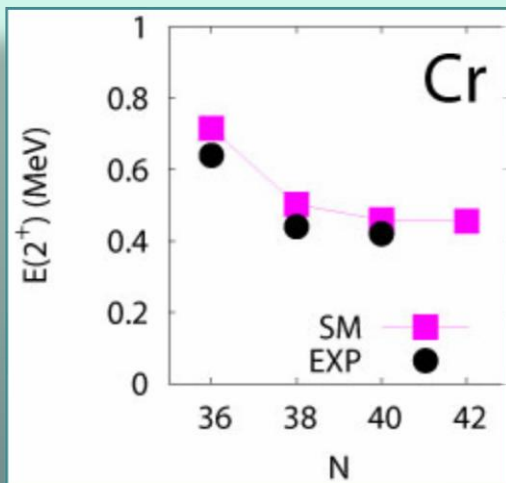


SML, F. Nowacki, A. Poves and K. Sieja, 2010, in preparation

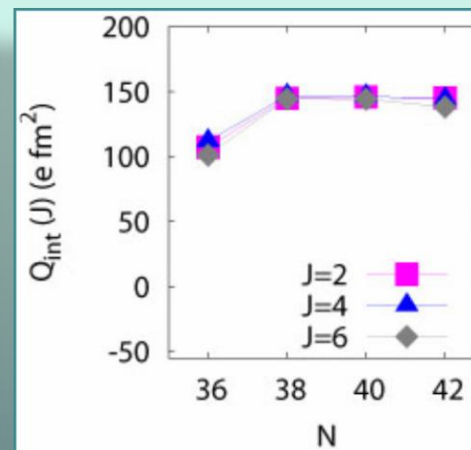


# Cr isotopes

$E(2^+)$

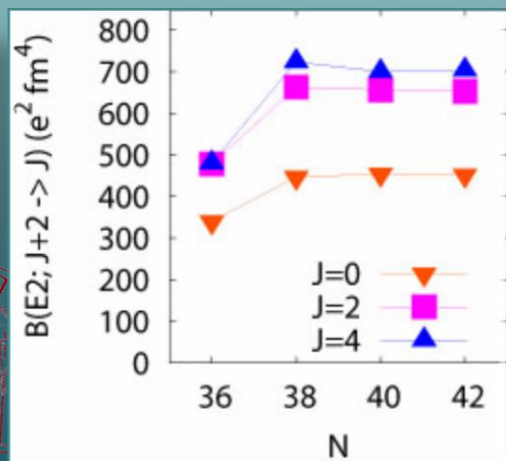


$Q_{int}(J)$



$\beta \sim 0.35$

$B(E2; 2^+ \rightarrow 0^+)$



Relation between Laboratory and Intrinsic frames

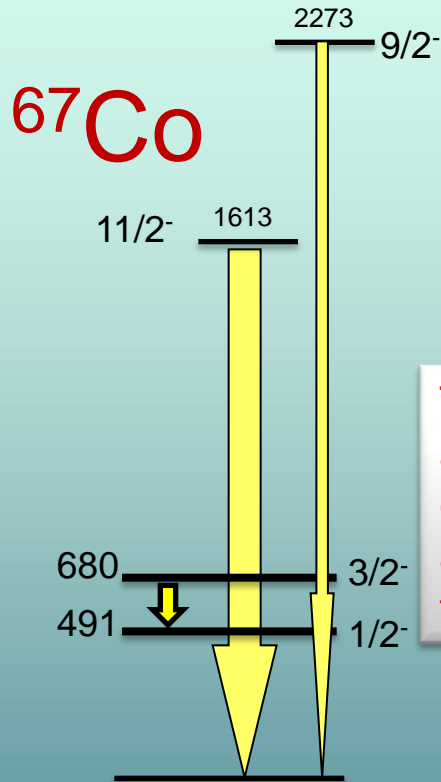
$$Q_{int} = \frac{(J+1)(2J+3)}{3K^2 - J(J+1)} Q_{spec}(J), \quad K \neq 1,$$

$$B(E2, J \rightarrow J-2) = \frac{5}{16} e^2 |\langle JK20 | J-2, K \rangle|^2 Q_{int}^2 \quad K \neq \frac{1}{2}, 1.$$

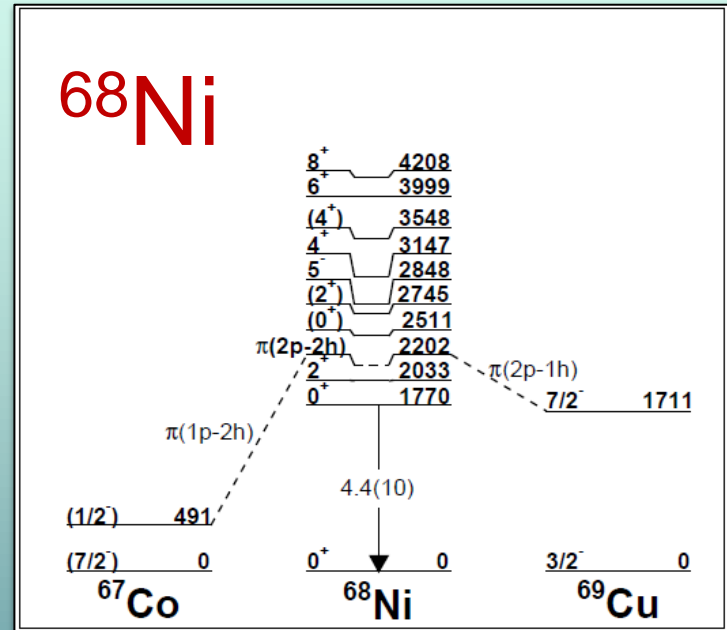
SML, F. Nowacki, A. Poves and K. Sieja, 2010, in preparation



# Shape coexistence in $^{67}\text{Co}$ and $^{68}\text{Ni}$



The  $1/2^-$  state gains a total of  $\sim 8$  MeV of correlation energy and  $\sim 5$  MeV relative to the ground state



D. Pauwels et al., arXiv:1005.4602v1 [nucl-ex] 25 May 2010

$^{67}\text{Co}$ : F. Recchia et al., to be published

The LNPS interaction reproduces the shape coexistence in  $^{67}\text{Co}$  and  $^{68}\text{Ni}$



# Conclusions

The mass region studied shows a development of collectivity (deformation) towards  $N=40$  with rapid changes of shape along the isotopic chains.

The LNPS effective interaction: built up using sets of realistic TBME and monopole corrections. Large scale shell model calculations for Ca, Ti, Cr, Fe, Co and Ni near  $N=40$  (dim  $\sim 10^{10}$ ) have been presented.

The maximum of collectivity is found in Cr isotopes, where stable deformation starts at  $N=38$ . Iron isotopes become well deformed at  $N=40$ .

The LNPS effective interaction in the fp-gd space is able to describe shape coexistence in this third island of inversion.



# Collaboration

Theory:

F. Nowacki, A. Poves, K. Sieja

Experiments:

F. Recchia, S. Lunardi, E. Farnea, A. Gadea,  
J.J. Valiente-Dobon, D.R. Napoli, N. Marginean,  
D. Bazzacco, M. Ionescu-Bujor,  
A. Iordachescu, S. J. Freeman, R. Chapman,  
D. Mengoni, R. Orlandi, A. Bracco, G. Benzoni,  
S. Leoni, B. Million, O. Wieland, R. Broda, B. Fornal,  
J. Wrzesinski *et al.*



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