

The many facets of breakup reactions with exotic beams

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cf. Y. Suzuki & Co., H. Sagawa & Co., T. Nakamura & Co.



Introduction

Breakup reactions are a versatile mean of studying both projectile and target nuclear properties

In exotic nuclei they are used to study projectile structure via inverse kinematics experiments

Also transfer to the continuum from target sometime or projectile fragmentation to study resonance states in unbound nuclei

High energy scattering and the eikonal approximation. Optical potentials.

Elastic scattering of halo nuclei and the optical potential including breakup.

Transfer to the continuum, projectile fragmentation.

Coulomb breakup. All orders vs first order approximation. The proton vs neutron case.

Accuracy of reaction theory and experimental data analysis vs structure theory.





(inclusive breakup with final state interaction with the target)



 $k_2 - k_1 = k \epsilon_f - \epsilon_i = mv^2/2$

 $\varepsilon_{f}^{opt} > 0$ for small ε_{i}

diffraction and stripping



(inclusive breakup with final state interaction with the target)





























J.Enders et al.



FIG. 3. Parallel-momentum distributions of the reaction residues

FIG. 4. Measured momentum distribution (full points) co-

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Inclusive spectra of stripping reactions induced by heavy ions

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after



































CAPEL, GOLDSTEIN, AND BAYE

Projectile fragmentation

60

¹¹Be: a **simple** test case



2HYSICAL REVIEW C 70, 064605 (2004)

from bound s-state to d-resonance: inelastic excitation to the continuum?

¹¹Be+¹²C @ 67A.MeV



FIG. 4. Theoretical and experimental breakup cross sections as a function of the energy. The four curves correspond to the calculations performed with various combinations of the potentials of Table III convoluted with energy resolution. Experimental data are from Ref. [39].

Fig. 3. n^{-10} Be relative energy spectrum, including Coulomb and nuclear breakup for the reac ¹¹Be + ¹²C \rightarrow n + ¹⁰Be + X at 67 A MeV. Only the contributions from an s initial state with spectroscopic tor $C^2S = 0.84$ are calculated. The triangles are the total calculated result after convolution with the experime resolution function. The dots are the experimental points from [1].

[39] N. Fukuda et al., Phys. Rev. C 70, 054606 (2004).



Analytical methods for transfer and breakup

$$|S_{ct}|^{2}$$

$$\uparrow$$

$$\sigma = \int d^{2}b_{c}P_{el}(b_{c})P_{tr}(b_{c}); P_{tr} = |A|^{2} \longrightarrow A = \frac{1}{i\hbar}\int dt \langle \psi_{f}(r,t) | V_{2} | \psi_{i}(r-R(t),t) \rangle$$

Seaking a clear physical interpretation of DWBA (<u>Brink</u> et al. and Copenhagen school since 1978). similar to Alder& Winther for Coulomb excitations.



Review of basic knowledge of core-target and nucleon-target interaction potentials and cross sections. This is necessary to ensure accuracy of absolute cross sections in spectroscopic studies.

Heavy-ion high energy scattering and the eikonal approximation of a contraction of a contra



Isao Tanihata

Nuclear Physics A654 (1999) 235e-251e

Nuclear Structure Studies from Reaction Induced by Radioactive Nuclear Beams

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Reactions with Radioactive Ion Beams

Fig. 2 Interaction cross sections of p and sd shell nuclei at the beam energy near 800A MeV. He: ref. 1, Li, Be: ref. 2, B: ref. 3-5, Ne and A=17: ref. 6, A=20: ref. 7, Na: ref. 8, Mg:ref. 9, and others ref. 10.



PHYSICAL REVIEW C

INFN Angela Bonaccorso

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Trends of total reaction cross sections for heavy ion collisions in the intermediate energy range

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$$\sigma_{R} = \pi R_{int}^{2} \left[1 - \frac{B_{C}}{E_{c.m.}} \right], \quad \begin{array}{c} \text{takes into account difference between impact parameter and distance of closest approach} \quad (13) \end{array}$$

where the term B_C is the Coulomb barrier of the projectile-target system. It is given by

$$B_{C} = \frac{Z_{t} Z_{p} e^{2}}{r_{C} (A_{t}^{1/3} + A_{p}^{1/3})} , \qquad (14)$$

$$R_{\rm int} = R_{\rm vol} + R_{\rm surf}$$
.

$$R_{\rm surf} = r_0 \left[a \frac{A_p^{1/3} A_t^{1/3}}{A_p^{1/3} + A_t^{1/3}} - c \right] \, .$$

validity of the strong absorption model for heavy-ion reactions gives a simple way to treat the core-target interaction in halo nuclei scattering



From a fit of many data of σ_R from 30A to 2100A MeV reactions, the parameters r_0 , a, c were determined. It was found that $r_0 = 1.1$ fm and a = 1.85 are independent of the projectile-target combination and the beam energy. Only c was found to depend on the beam energy, as shown in Fig. 2.3.

These equations provide a simple way to compare the reaction cross sections at different energies. However, since they are purely empirical formula, one should be careful when applying them to an exotic nucleus because of a possible difference in the surface diffuseness as well as any proton-neutron density difference. When one measures σ_R using a β -unstable nucleus, only ro is expected to change. Although r_0 includes size information of both the projectile and the targets, it provides a simple mean to study the deviation of the radius







Nucleon-target potential

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FINAL STATE INTERACTION EFFECTS IN BREAKUP ... PHYSICAL REVIEW C 61 034605



FIG. 1. Neutron-target cross sections as a function of the neutron incident energy. Top figure: ⁹Be target. Dotted and dot-dashed curves are the elastic and reaction cross sections, respectively. Full curve is their sum. Data points from Ref. [18]. Center and bottom figure: ²⁸Si target with JLM potential and optical potential from Table I, respectively. Same notation as above. Data points from Ref. [18].



PHYSICAL REVIEW C

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Neutron total cross sections at intermediate energies

R. W. Finlay, W. P. Abfalterer, G. Fink, E. Montei, and T. Adami Department of Physics and Astronomy, Ohio University, Athens, Ohio 45701

P. W. Lisowski, G. L. Morgan, and R. C. Haight P-Division, Los Alamos National Laboratory, Los Alamos, New Mexico 87545 (Received 30 September 1992)

http://www.nea.fr/html/dbdata/x4.



PHYSICAL REVIEW C, VOLUME 62, 064612

Global analysis of proton nucleus reaction cross sections

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Elastic scattering and the optical potential including breakup channel (cf. talks on FUSION)

Relevant papers in the past

- [25] R. A. Broglia, and A. Winther, *Heavy Ion Reactions*, Benjamin, Reading, Mass, 1981.
- [26] R. A. Broglia, G. Pollarolo and A. Winther, Nucl. Phys. A361, 307 (1981).
- [27] A. Bonaccorso, G. Piccolo, D. M. Brink, Nucl. Phys. A441 (1985) 555.
- [28] Fl. Stancu and D. M. Brink, Phys. Rev. C 32, 1937 (1985).



Elastic scattering and reaction mechanisms of the halo nucleus ¹¹Be around the Coulomb barrier

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TABLE I: W-S Optical potentials obtained from the fit of the experimental data. The real potential radius parameter is $r_0=1.1$ fm and the imaginary one is $r_i=1.2$ fm, where $R_{0,i,si}=r_{0,i,si}(A_p^{1/3}+A_t^{1/3})$. The Coulomb radius parameter is $r_c=1.25$ fm.

Reaction	V(MeV)	a(fm)	$V_i(MeV)$	$a_i(fm)$	$V_{\rm si}({\rm MeV})$	$r_{\rm si}({\rm fm})$	$a_{\rm si}({\rm fm})$	J_V (MeV fm ³)	J_W (MeV fm ³)
⁹ Be+ ⁶⁴ Zn	126	0.6	17.3	0.75				295	53
¹⁰ Be+ ⁶⁴ Zn	86.2	0.7	43.4	0.7				193	124
¹¹ Be+ ⁶⁴ Zn	86.2	0.7	43.4	0.7	0.151	1.3	3.5	193	129



$$|S_{NN}(b)|^2 = e^{-4\delta_I(b)}$$
$$\delta_I(b) = -\frac{1}{2\hbar} \int_{-\infty}^{+\infty} (W_V(\mathbf{r}(t)) + W_S(\mathbf{r}(t))) dt$$

$$\int_{-\infty}^{+\infty} W_S(\mathbf{r}(t)) dt = -\frac{\hbar}{2} P_{b_{up}} \quad \text{or } P_{transf}$$

 $\mathbf{r}(t) = \mathbf{b}_{\mathbf{c}} + vt$

$$|S_{NN}|^{2} = |S_{CT}|^{2} e^{-P_{bup}}$$
$$W_{S}^{N}(r) = -\frac{\hbar v}{2} p_{b_{up}}^{N}(r) \frac{1}{\sqrt{2\pi ar}}$$



Appendix A. Connection to low energy approaches

In our formalism the imaginary part of the optical potential due to Coulomb breakup i given by

$$\int_{-\infty}^{+\infty} W_S(\mathbf{r}(t)) dt = -\frac{\hbar}{2} p_{b-up}^C, \qquad (A.1)$$

while Eq. (12) of Andrés et al. [14] reads

$$\int_{-\infty}^{+\infty} W_S(\mathbf{r}(t)) dt = h\alpha.$$
(A.2)

Where both p_{b-un}^C and α depend on the incident energy and on the classical trajectory of relative motion. In our case such a trajectory is a straight line since our approach applies to incident energies well above the Coulomb barrier.

The two approaches are consistent if $\alpha \rightarrow -p_{b-un}^C/2$ in the high energy limit. To show that this is true we write explicitly the expression in Ref. [14]

$$\alpha = -\frac{\pi}{9} \left(\frac{Z_T e}{\hbar v a_c} \right)^2 \int d\varepsilon_k \left(I_{11}^2(\varpi) + I_{1-1}^2(\varpi) \right) \frac{dB(E1, \varepsilon_k)}{d\varepsilon_k}, \quad (A.3)$$

where I1±1 are the well known Coulomb integrals [46] which can be expressed in terms of Bessel functions of imaginary order. However, according to Eq. (28) of Ref. [50] in the high energy limit

$$I(E1, \pm 1) = I_{1\pm 1} = \frac{2a_c}{b_c} \varpi K_1(\varpi),$$
 (A.4)

where a_c is the Coulomb length parameter and now K_1 is an ordinary Bessel function of real index.

On the other hand, considering Eq. (15) for p_{b-up}^C we remark that it is well known and shown, for example, in Fig. 1 of Ref. [51] that $\varpi^2 K_0^2(\varpi)$ is much smaller than $\varpi^2 K_1^2(\varpi)$ for values of $\varpi \approx 0.1$, which happens for heavy ions at high energies. We can then write Eq. (15) as

$$p_{b-up}^{C}(b_{c}) \approx \frac{2\pi}{9} \left(\frac{Z_{T}e}{\hbar v b_{c}}\right)^{2} \int d\varepsilon_{k} 2(2\varpi K_{1}(\varpi))^{2} \frac{dB(E1, \varepsilon_{k})}{d\varepsilon_{k}},$$
 (A.5)

A.A. Ibraheem, A. Bonaccorso / Nuclear Physics A 748 (2005) 414-432

$$p_{b-up}^{C}(b_{c}) \approx \frac{32}{3\pi} C^{2} S\left(\frac{C_{0}C_{i}}{b_{c}}\right)^{2} \int d\varepsilon_{k} \frac{m_{n}}{\hbar^{2}k} \left(\varpi^{2} K_{1}^{2}(\varpi) + \varpi^{2} K_{0}^{2}(\varpi)\right) \frac{k^{4}}{(k^{2} + \gamma^{2})^{4}}$$

ce for the case studied in this paper the explicit form of B(E1) is

$$\frac{dB(E1, \epsilon_k)}{d\epsilon_k} = C^2 S \frac{m_n}{\hbar^2 k} (C_i \beta_1 Z_P e)^2 \frac{6}{\pi^2} \frac{k^4}{(k^2 + \gamma^2)^4},$$
(A.6)

ich is the consistent with Eq. (6.5) of Ref. [51] or Eq. (7.24) of [28] and it is the explicit m of the B(E1) obtained for an s-initial state using the asymptotic form of the wave sction.

Finally, using Eq. (A.4) in Eq. (A.3) and comparing with Eq. (A.5) we obtain that $\alpha =$ score/2 in the high energy, straight line trajectory limit. However, we remark that our shability Eq. (13) is more accurate than the high energy limit of a of Eq. (A.3) since it contains also the term representing longitudinal excitations, proportional to K₀ and to k₂, the parallel component of neutron momentum.



A. Bonaccorso and F. Carstoiu Optical potentials of halo and weakly bound nuclei Nucl. Phys. A706 (2002) 322.



A.A. Ibraheem and A. Bonaccorso, Recoil effects on the optical potentials of weakly bound nuclei Nucl. Phys. A748 (2005) 414.









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Nuclear and Coulomb breakup potentials can be compared by using the parameterization :

$$W_S^N(r) = -\frac{\hbar v}{2} P_0 \sum_n A_n \exp\left(-r/\alpha_n\right) \frac{1}{\sqrt{2\pi\alpha_n r}}.$$
$$W_S^C(r) = -\frac{\hbar v}{2} P_0 \sum_n B_n \exp\left(-r/\beta_n\right) \frac{1}{\sqrt{2\pi\beta_n r}}.$$

The core survival probability has been parameterized as

$$P_0(b_c) = |S_{CT}|^2 = \exp(-\ln 2e^{[(R_s - b_c)/a_0]}),$$

$$\alpha_2 \approx 1/2\gamma$$
, $\gamma = \sqrt{2\mu\epsilon_i}/\hbar$ $\beta_3 \approx (\epsilon_f - \epsilon_i)/\hbar v$

the most relevant parameter is the diffusness whose physical interpretation is

decay length of initial state wave function

adiabaticity parameter of Coulomb



$$1 - |S_{NN}(b_c)|^2 \approx 1 - |S_{CT}(b_c)|^2 e^{-P_{bup}(b_c)}$$

= 1 - |S_{CT}(b_c)|^2 +
+|S_{CT}(b_c)|^2 (p_{bup}^N(b_c) + p_{bup}^C(b_c))

$$\sigma_{NN} = 2\pi \int b_c db_c \left(1 - |S_{NN}(b_c)|^2\right)$$
$$\approx \sigma_{CT} + \sigma_{b_{up}}^N + \sigma_{b_{up}}^C.$$



Projectile fragmentation and resonances (near threshold).

- During scattering at low energy a quasi-stationary system is formed (compound nucleus). Link the properties of the unperturbed "target" nucleus (wave functions of stationary states, underlying potential) to the experimentally measured scattering quantity.
- This is usually s-state (sometime p-state) scattering. Higher angular momentum resonances need an energy dependent optical potential (channel coupling).



Transfer to the continuum vs. Projectile fragmentation: a model

for diffractive breakup in which the observable studied is the n-

core relative energy spectrum and its resonances

$$A_{fi} = \frac{1}{i\hbar} \int_{-\infty}^{\infty} dt \langle \psi_f(\mathbf{r}, t) | V_2(\mathbf{r} - \mathbf{R}(t)) | \psi_i(\mathbf{r}, t) \rangle,$$

$$\begin{aligned} \frac{dP_t(b_c)}{d\varepsilon_f} &= \frac{1}{8\pi^3} \frac{mk_f}{\hbar^2} \frac{1}{2l_i + 1} \Sigma_{m_i} |A_{fi}|^2 \\ &\approx \frac{4\pi}{2k_f^2} \Sigma_{j_f} (|1 - S_{j_f}|^2 + 1 - |S_{j_f}|^2) (2j_f + 1) (1 + F_{l_f, l_i, j_f, j_i}) B_{l_f, l_i} \\ &= \sigma_{nN}(\varepsilon_f) \mathcal{F}, \quad \text{diffraction + stripping} \quad \text{inclusive breakup} \quad ($$

$$\begin{split} \frac{dP_{in}}{d\varepsilon_f} &= \frac{2}{\pi} \frac{v_2^2}{\hbar^2 v^2} C_i^2 \frac{m}{\hbar^2 k} \frac{1}{2l_i + 1} \Sigma_{m_i, m_f} |1 - \bar{S}_{m_i, m_f}|^2 |I_{m_i, m_f}|^2, \longrightarrow \text{ exclusive breakup} \\ \hline \delta f = Se^{2i\nu} = e^{2i(\delta + \nu)} \quad \overline{S} \text{ off-shell} \\ S \text{ on shell} \qquad \qquad I_{l_f, l_i} \approx \frac{e^{-2\eta b_c}}{b_c^3} \text{ Fragmentation} \end{split}$$







Comparison to R-matrix theory

AB, DM Brink, PRC38, 1776(1988)

$$|\sin\delta_{l_f}|^2 = \frac{\Gamma}{2} \frac{\Gamma/2}{(\epsilon - \epsilon_{\rm res})^2 + \Gamma^2/4} \simeq \frac{\Gamma}{2} \pi \delta(\epsilon - \epsilon_{\rm res})$$
 (3.1)

and

Ρ

$$\begin{aligned} (l_f, l_i) &= \int \frac{dP}{d\varepsilon} (l_f, l_i) d\varepsilon \\ &\simeq \frac{\Gamma}{2} \pi \int d\varepsilon \, \delta(\varepsilon - \varepsilon_{\rm res}) 4B(l_{\rm res}, l_i) \\ &= \frac{\pi}{2} \left[\frac{\hbar}{mv} \right]^2 \frac{m\Gamma}{\hbar^2 k_{\rm res}} |C_i|^2 (2l_f + 1) \\ &\qquad \times P_{l_i} \left[1 + 2\frac{k_1^2}{\gamma^2} \right] P_{l_f} \left[2\frac{k_2^2}{k_{\rm res}^2} - 1 \right] \frac{e^{-2\eta R}}{\eta R} , \end{aligned}$$

$$(3.2)$$

where $B(l_{res}, l_i)$ is given by Eq. (2.29).

In the case of transfer between bound states [cf. Eq. (3.15) of Ref. 4] the equivalent of Eq. (3.2) was

$$P(l_2, l_1) = \frac{\pi}{2} \left[\frac{\hbar}{mv} \right]^2 |C_1 C_2|^2 (2l_2 + 1) P_{l_1} \left[1 + 2\frac{k_1^2}{\gamma_1^2} \right] \\ \times P_{l_2} \left[2\frac{k_2^2}{\gamma_2^2} + 1 \right] \frac{e^{-2\eta R}}{\eta R} .$$
(3.3)

The place of the asymptotic normalization constant of the final state C_2 is then taken by the term $m \Gamma / \hbar^2 k_{res}$.

To understand this we use the definition of Γ given in *R*-matrix theory¹⁴

$$\Gamma = \frac{\hbar^2 k_{\rm res}}{m} \frac{u_l^2(R)}{[k_{\rm res}O_l(k_{\rm res}R)]^2} , \qquad (3.4)$$

where u_l is the neutron radial wave function calculated in the potential of the target at the resonance energy and $O_l(k_{res}R) = h_l^{(+)}(k_{res}R)$ is its asymptotic form outside a radius R beyond which the nuclear potential vanishes. Then we have

$$\frac{m\Gamma}{\hbar^2 k_{\rm res}} = \frac{u_l^2(R)}{\left[k_{\rm res}O_l(k_{\rm res}R)\right]^2}$$
(3.5)

. .

$$C_2 \mid^2 = \frac{\psi_{\text{num}}^2(R)}{[\gamma_2 h_l^{(+)}(i\gamma_2 R)]^2} , \qquad (3.6)$$

where ψ_{num} is the numerical solution of the single-particle Schrödinger equation at the experimental binding energy and $h_l^{(+)}(i\gamma_2 R)$ is a Hankel function of complex argument imposed as its asymptotic form. C_2 is independent from the radius R when this is taken well outside the nuclear potential.

¹⁴A. M. Lane, R. G. Thomas, and E. P. Wigner, Phys. Rev. 98, 639 (1955). •¹⁴B fragmentation on C



JL Lecouey LPCC 02-03; Few-Body Systems 34 (2004) 21





H.Simon et al, NPA791 (2007)267







Systematic investigation of the drip-line nuclei ¹¹Li and ¹⁴Be and their unbound subsystems ¹⁰Li and ¹³Be.

Nucl. Phys. A791 (2007) 267.

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¹⁴Be T_{1/2}=4.35ms±0.17







Fig. 10. Differential cross section as a function of the relative energy between 12 Be and a neutron. The data points are the same as those in Fig. 4, panel 3. The thin-solid line corresponds to the $1/2^+$ virtual state, the dotted line is the contribution from the $5/2^+$ state. Dashed lines display the $1/2^-$ state and its satellite at low energy. The thick-solid line is the sum of the reaction branches.

Systematic investigation of the drip-line nuclei ¹¹Li and ¹⁴Be and their unbound subsystems ¹⁰Li and ¹³Be.

Nucl. Phys. A791 (2007) 267.

- H. Simon ^{a,b}, M. Meister ^{a,c}, T. Aumann ^{b,d}, M.J.G. Borge^e,
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Figure 3.5: Formation of ¹³Be with one neutron (crosses) added to an open shell ¹²Be. Only one neutron is added in each configuration, but the cross indicates states which can be populated.

M. Labiche, F. M. Marqués, O. Sorlin, and N. Vinh Mau, Phys. Rev. C 60, 027303 (1999).
J. C. Pacheco and N. Vinh Mau, Phys. Rev. C 65, 044004 (2002).



TABLE III: Theoretical and experimental values of S_{2n} (MeV) in ¹²Be and ¹⁴Be (from Ref.[22]), $\langle \mathbf{r}^2 \rangle_{A+2}^{1/2}$ (fm), $\langle \lambda^2 \rangle^{1/2}$ (fm) and $\langle \rho^2 \rangle^{1/2}$ (fm) in ¹⁴Be (from Ref. [23, 37], λ deduced using Eq.10) in the two cases of non-inversion (A) and inversion (B) of the $2s_{1/2}$ and $1p_{1/2}$ shells.

	$S_{2n}(^{12}\text{Be})$	$S_{2n}(^{14}\text{Be})$	$\langle { m r}^2 angle_{A+2}^{1/2}$	$\langle ho^2 angle^{1/2}$	$\langle \lambda^2 angle^{1/2}$
A	2.91	0.51	3.45	8.45	5.45
В	3.71	1.29	2.91	4.56	4.02
Exp.	$3.673 {\pm} 0.015$	1.26 ± 0.01	$3.10{\pm}0.15$	$5.4{\pm}1.0$	$4.2{\pm}1.7$

Particle-particle random phase approximation applied to Beryllium isotopes



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FIG. 2: Low lying spectra of ¹⁴Be obtained with pp-RPA without (A) and with (B) inversion in ¹³Be compared to experiment.

PRC, in press, 1007.2719v1-nucl-th





Fig. 8. Results obtained including the s, p and d states. Each curve corresponds to just one transition as indicated. The solid curve is the sum of all transitions from the s-bound state. To make them visible some curves have been multiplied by a factor of five as indicated in the legend.



Figure 11: Check of the dependence from the initial state angular momentum. Full curve: sum of transitions from s-initial state. Dashed and dotdashed lines: sum of transitions from p and d-initial states respectively.

In projectile fragmentation reactions it is the lowest angular momentum initial state to dominate the transition process



Strengths of the *s*-state δV potential in Eq. (40) and corresponding scattering lengths, effective range parameter and *energy parameter* ϵ . The strength of the central Woods–Saxon part is $V_0 = -39.8$ MeV in all cases (cf. Table 3)

a (MeV)	a_s (fm)	r_e (fm)	€ (MeV)
8.0	-0.8	117.0	
4.0	-3.5	17.9	
2.0	-6.6	11.8	
-1.0	-26.1	7.58	
-5.0	22.4	5.9	0.06
-15.0	7.1	3.8	1.34
-35.0	4.5	2.7	6.49







- A time dependent theory for projectile fragmentation reaction has been established which contains the sudden approximation and R-matrix theories as limiting cases.
- ✤2p correlations and particle-vibration couplings play a fundamental role.
- Importance of coupling to core excited states.
- For the first time the shell ordering of ¹³Be has been established theoretically on a firm basis and parity inversion across threshold has been proved to persist for N=9 isotones
- Much care is needed in analyzing experimental results in order not to draw misleading or unphysical conclusions: sudden approximation vs. time dependent, use of Breit-Wigner resonance form (vs. exact S-matrix or R-matrix),importance of various initial state components.



Coulomb breakup. All orders vs first order approximation. The proton vs neutron case.







Angula Benaccorso



$$V_{\rm nt}(\beta_2 \mathbf{r} + \mathbf{R}) \approx V_{\rm nt}(\mathbf{r} + \mathbf{R}),$$

$$V_{\rm ct}(\mathbf{R} - \beta_1 \mathbf{r}) \approx V_{\rm ct}(\mathbf{R}) + \mathbf{V}_{\rm eff}(\mathbf{r}, \mathbf{R})$$

where

1

 $\mathbf{V}_{\text{eff}}(\mathbf{r}, \mathbf{R}) = \beta_1 \mathbf{r} \cdot \mathbf{F}_{\text{ct}}(\mathbf{R}) \text{ and } \mathbf{F}_{\text{ct}}(\mathbf{R}) = -\nabla V_{\text{ct}}(\mathbf{R}).$

$$V_{\text{eff}}(\mathbf{r}, \mathbf{R}(t)) = +\beta_1 Z_P Z_T e^2 \left(\frac{\mathbf{r} \cdot \mathbf{R}(t)}{R(t)^3}\right)$$
$$= +\beta_1 Z_P Z_T e^2 \frac{xd + zvt}{(d^2 + (vt)^2)^{3/2}}.$$

The breakup amplitude becomes

$$g_{lm}(\mathbf{k}, \mathbf{d}) = \frac{1}{i\hbar} \int d^3 \mathbf{r} \int dt \, e^{-i\mathbf{k}\cdot\mathbf{r} + i\omega t} e^{(\frac{1}{i\hbar}\int_t^\infty \overline{V}_2(\mathbf{r}, t')\,dt')} \overline{V}_2(\mathbf{r}, t) \phi_{lm}(\mathbf{r})$$

where $\omega = (\varepsilon_{\mathbf{k}} - \varepsilon_0)/\hbar$.

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$$V(\vec{r}, \vec{R}) = \frac{V_c}{|\vec{R} - \beta_1 \vec{r}|} + \frac{V_v}{|\vec{R} + \beta_2 \vec{r}|} - \frac{V_0}{R}$$
(1)

where $V_c = Z_c Z_t e^2$, $V_v = Z_v Z_t e^2$ and $V_0 = (Z_v + Z_c)Z_t e^2$. β_1 and β_2 are the mass ratios of proton and core, respectively, to that of the projectile. The coordi-

Our expression for the differential cross-section is

$$\frac{d\sigma}{d\vec{k}} = \frac{1}{8\pi^3} \int d\vec{b}_c |S_{ct}(b_c)|^2 |g^{rec} + g^{dir} + g^{nuc}|^2.$$
(6)

where $S_{ct}(b_c)|^2$ is the core-target elastic scattering probability discussed later and the probability amplitude has been written as the sum of three pieces: the recoil term,

$$g^{rec} = \int d\vec{r} e^{-i\vec{k}\cdot\vec{r}} \phi_i(\vec{r}) (e^{i\frac{2V_c}{\hbar v} \log \frac{b_c}{R_{\perp}}} - 1 - i\frac{2V_c}{\hbar v} \log \frac{b_c}{R_{\perp}} + i\chi(\beta_1, V_c)),$$
(7)

where, according to the discussions in [1], 25, 26, 27], the sudden limit has been used in order to include all orders in the interaction. Similarly, the second term in our probability amplitude is the direct proton Coulomb interaction. It has the same form as Eq.(7) but for the substitution $V_c \to V_v$, $b_c \to b_v$ and $\beta_1 \to -\beta_2$.

Finally, the nuclear part is

$$g^{nuc} = \int d\vec{r} e^{-i\vec{k}\cdot\vec{r}} \phi_i(\vec{r}) \left(e^{i\chi_{nt}(b_v)} - 1 \right). \tag{8}$$

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PHYSICAL REVIEW C 76, 014607 (2007)

All orders proton breakup from exotic nuclei

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Figure 2: Calculated inclusive momentum distribution of ⁷Be fragments after proton-removal from ⁸B against Pb at 936 MeV/A. Data are from [46].



Figure 4: For the same reaction of Fig 2, proton momentum distribution in both dipole and full-multipole approximations, for both ground and excited state.

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Dynamic polarization in the Coulomb breakup of loosely bound ¹⁷F

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Fig. 4. Angular distributions of exclusive breakup for (a) 17 F + 58 Ni and (b) 17 F + 208 Pb. The dynamical calculation including the proton-target Coulomb field is shown by the dashed curves and the combined Coulomb and nuclear fields is shown by the solid curves. The dotted curve in (b) is for the perturbation calculation using an effective binding energy of 1.2 MeV (see text).





The proton vs neutron case.

BONACCORSO, BRINK, AND BERTULANI



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FIG. 3. Proton (dashed) and neutron (solid) wave functions for 8B , ${}^{17}F$ as indicated. Neutron wave functions obtained for effective energies as in Table II, in the case of the ${}^{58}Ni$ target.

TABLE II. Effective parameters.

	⁸ B+ ⁵⁸ Ni	⁸ B+ ²⁰⁸ Pb	¹⁷ F+ ⁵⁸ Ni	$^{17}F + ^{208}Pb$
Δ_i (MeV)	-1.85	-2.29	-2.7	-3.2
$\widetilde{\epsilon}_i$ (MeV)	-1.99	-2.43	-3.3	-3.8
$\widetilde{\gamma}_i ~({\rm fm}^{-1})$	0.29	0.34	0.39	0.42
\tilde{C}_i (fm ^{-1/2})	0.69	0.79	0.75	0.89
$\tilde{\varepsilon}_{i}^{*}$ (MeV)			-2.8	-3.3
$\widetilde{\gamma}_i^* ~({\rm fm}^{-1})$			0.36	0.39
\tilde{C}_i^* (fm ^{-1/2})			3.06	3.5

	^{8}B	J^{π}	17 F	J^{π}
$R_i(fm)$	6.0		6.5	
$\varepsilon_i(MeV)$	-0.14	$1p_{3/2}$	-0.6	$1d_{5/2}$
$\varepsilon_i^*(MeV)$	-0.57	$1p_{1/2}$	-0.1	$2s_{1/2}$

MINEN Angela Bonaccorso 8B+208Pb (gs p_{3/2}) at 72 Mev/n multipole Vs dipole



First order pert. results

INFN Angela Bonaccorso





8B+208Pb (ground state) at 72 MeV/n Proton Vs Neutron





Accuracy of reaction theory and experimental data analysis vs structure theory.

$$\sigma_{\text{el.bup}} = \int \langle \phi_0 | \widehat{S}_v^* \widehat{S}_c^* | \phi_k \rangle \langle \phi_k | \widehat{S}_v \widehat{S}_c | \phi_0 \rangle \, \mathrm{d}k$$

$$= \langle \phi_0 | | \widehat{S}_v |^2 | \widehat{S}_c |^2 | \phi_0 \rangle - | \langle \phi_0 | \widehat{S}_v \widehat{S}_c | \phi_0 \rangle |^2.$$

$$\sigma_{\text{in.bup}} = \frac{\pi}{k^2} \sum \langle \phi_0 | (1 - \widehat{T}_c) \widehat{T}_v | \phi_0 \rangle.$$

$$T_v \text{ with } 1 - | \widehat{S}_v |^2$$

$$\sigma_{\text{exp}} = R_s \left(\frac{A}{A - 1} \right)^2 C^2 S_j \sigma_{\text{sp}}.$$

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Reduction of spectroscopic strength: Weakly-bound and strongly-bound single-particle states studied using one-nucleon knockout reactions

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reaction theory. The reduction of the experimentally deduced spectroscopic strengths, relative to the predictions of shell-model calculations, is of order 0.8–0.9 in the removal of weakly bound protons and 0.3–0.4 in the knockout of the strongly bound neutrons. These results support previous studies at the extremes of nuclear binding and provide further evidence that in asymmetric nuclear systems the nucleons of the deficient species, at the more-bound Fermi surface are more strongly correlated than those of the more weakly bound excess species.

TABLE I. Summary of the results for the one-proton and one-neutron knockout from ²⁴Si and ²⁸S projectiles. Given are the excitation energy of the final states in the projectile-like knockout residues, the spin and parity, the experimental branching ratios, the measured cross sections, the shell-model single-particle orbitals, the single-particle cross sections from the eikonal theory and their composition into stripping and diffractive contributions, the shell-model spectroscopic factors (USDB effective interaction), the resulting theoretical cross sections from Eq. (1), the theoretical branching ratios, and the deduced reduction factors.

Res.	Ex	J ^x	BRexp	a	Conf.	(mp)	or str	or dif	C ² S	at the second se	BRth	R _s
<u></u>	(KCV)	(//)	(%)	(mb)	SM	(mb)	(mb)	(mb)	SM	(mb)	(%)	10
						Projectile 24Si						
²³ Al	0	5/2+	100	67.3(35)	d5/2	22.74	17.56	5.18	3.42	84.68	100	0.79(4)
23Si	0	5/2+	100	9.8(10)	d5/2	13.43	10.96	2.47	1.71	25.01	100	0.39(4)
						Projectile 28S						
27 P	0	1/2+	82(7)	31(3)	\$1/2	28.57	20.73	7.84	0.832	25.56	60.4	
	1100	3/2+	18(3)	6.8(11)	d3/2	19.01	14.61	4.40	0.82	16.76	39.6	
Inc.				38(3)						42.32		0.90(7)
27S	0	5/2+			d5/2	11.09	8.99	2.10	3.136	37.40	96.5	
	≤100	3/2+			d3/2	10.75	8.72	2.03	0.119	1.37	3.5	
Inc.				11.9(12)						38.77	48	0.31(3)

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The ${}^{9}Be({}^{32}Ar, {}^{31}Ar)X$ reaction, leading to the ${}^{5+}_{2}$ ground state of a nucleus at the proton drip line, has a cross section of 10.4(13) mb at a beam energy of 65.1 MeV/nucleon. This translates into a spectroscopic factor that is only 24(3)% of that predicted by the many-body shell-model theory. We introduce refinements to the eikonal reaction theory used to extract the spectroscopic factor to clarify that this very strong reduction represents an effect of nuclear structure. We suggest that it reflects correlation effects linked to the high neutron separation energy (22.0 MeV) for this state.



FIG. 3. Measured reduction factors R_s as a function of nucleon separation energy. The points, taken from the left, use data from ⁸B, ⁹C, ¹⁵C, ⁵⁷Ni, ¹²C, and ¹⁶O [4,5,26]. The labeled N = 14 nuclei are discussed in the present Letter.

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(6)

2. Effect of particle-vibration coupling on individual energies

Let us start with the Hartree–Fock(HF) potential for a neutron in the mean field of the core nucleus and calculate the correction to this HF potential due to the coupling of single particle states to the RPA collective one-phonon states of the core. Neglecting the antisymmetrisation between the single particle and the particles of the core, one can write this correction δV as [26,28]:

$$\delta V(\mathbf{r}, \mathbf{r}'; E) = \lim_{\eta \to +0} \sum_{N,\lambda} \left[\frac{1 - n_{\lambda}}{E - \epsilon_{\lambda} - E_{N} + i\eta} + \frac{n_{\lambda}}{E - \epsilon_{\lambda} + E_{N} - i\eta} \right] \\ \times V_{0N}^{*}(\mathbf{r}) V_{0N}(\mathbf{r}') \phi_{\lambda}^{*}(\mathbf{r}') \phi_{\lambda}(\mathbf{r}), \qquad (1)$$

 λ and N characterise respectively the HF single particle state of energy ϵ_{λ} and wave function ϕ_{λ} and the RPA collective state of the core of excitation energy E_N ; n_{λ} is the occupation number of the state λ in the HF ground state of the core and V_{0N} the transition amplitude between the ground state and the excited state N. V_{0N} can be written as:

$$\begin{aligned} b_{N}(\mathbf{r}) &= \sum_{i,j} [n_{i}(1-n_{j}) + n_{j}(1-n_{i})] x_{ij}^{(N)} \rho_{ij}(\mathbf{r}) \\ &= \langle \Psi_{N} | v | \Psi_{0} \rangle, \end{aligned}$$
(2)

where $x_{ij}^{(N)}$ are the RPA amplitudes, $\rho_{ij}(\mathbf{r})$ the transition density for the unperturbed particle-hole state (ij), v the two body interaction and Ψ_N and Ψ_0 the RPA wave functions of the excited state and the ground state respectively. In the summation over N we keep only natural parity states with multipolarity L and define amplitudes $f_{NL}(\mathbf{r})$ such that:

$$V_{0N}(\mathbf{r}) = \frac{1}{\sqrt{2L+1}} f_{NL}(\mathbf{r}) Y_L^{M*}(\hat{\mathbf{r}}). \qquad (3)$$

The correction of Eq. (1) to the HF potential induces a modification of the single particle energies which, in first approximation, can be calculated as the average of δV over the HF state of interest, replacing in Eq. (1) the energy E by the corresponding HF energy. For an HF state n of energy ϵ_n we get the modified energy ϵ_n as:

$$\epsilon_s = \epsilon_s + \delta \epsilon_s$$
, (4)

$$\delta \epsilon_{s} = \sum_{N,\lambda} F_{N\lambda} \frac{2j_{\lambda} + 1}{4\pi} \left(\frac{j_{s}}{-1/2} \frac{L}{0} \frac{j_{\lambda}}{1/2} \right)^{2} \left| \int_{0}^{\infty} r^{2} dr \mathcal{R}_{\lambda}(r) \mathcal{R}_{n}(r) f_{NL}(r) \right|^{2}$$
(5)

with

v

$$F_{N\lambda} = \frac{1 - n_{\lambda}}{\epsilon_{\sigma} - \epsilon_{\lambda} - E_{N}} + \frac{n_{\lambda}}{\epsilon_{\sigma} - \epsilon_{\lambda} + E_{N}},$$

 \mathcal{R}_{λ} and \mathcal{R}_{*} are the radial wave functions.

$$f_{NL}(r) = \beta_{NL} R_0 \frac{\mathrm{d} U(r)}{\mathrm{d} r},$$

Pacheco & N. Vinh Mau, PRC 65 (2002) 044004 Labiche et al. PRC 60 027303 (1999)

TABLE IV: Main pp-RPA amplitudes for ¹⁴Be ground state without (A) and with (B) inversion of $2s_{1/2}$ - $1p_{1/2}$ shells.

	X_{ab}			$X_{\alpha\beta}$	
	$(2s_{1/2})^2$	$(1d_{5/2})^2$		$(1p_{3/2})^2$	$(1p_{1/2})^2$
A	-0.93	-0.49		0.32	0.36
	$(1d_{5/2})^2$	$(1p_{1/2})^2$	$(1p_{1/2} \ 2p_{1/2})$	$(1p_{3/2})^2$	$(2s_{1/2})^2$
В	0.69	-0.73	0.52	-0.61	0.45