



Skyrme energy-density functional approach to collective excitations in medium-mass to heavy nuclei



Kenichi Yoshida

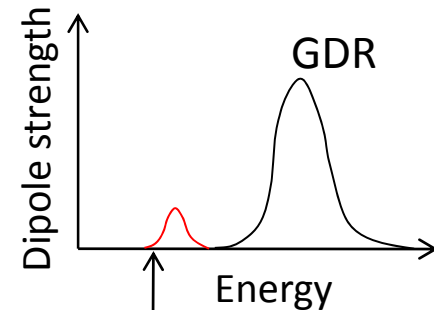
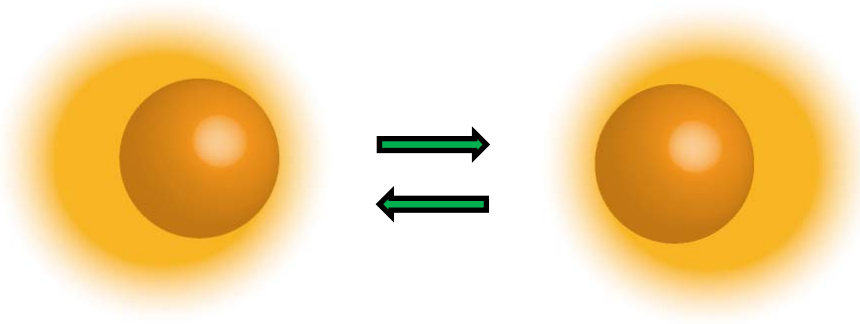
Collective modes unique to neutron-rich nuclei

DEFORMATION

- ✓ Coupling among excitation modes with different angular momenta

NEUTRON EXCESS

- ✓ IS and IV mixing modes
- ✓ Neutron-excitation dominant modes
- ✓ Neutron-skin excitation modes
- ✓ Soft dipole mode, Pygmy resonance



Skyrme-HFB-QRPA for axially-symmetric nuclei

Minimizing the energy density $\delta\mathcal{E} = 0$ $\mathcal{E} = \mathcal{E}_{\text{kin}} + \mathcal{E}_{\text{Sky}} + \mathcal{E}_{\text{Coul}} + \mathcal{E}_{\text{pair}} + \mathcal{E}_{\text{corr}}$



The coordinate-space Hartree-Fock-Bogoliubov eq. (Kohn-Sham-Bogoliubov eq.)

$$\begin{pmatrix} h^q(\mathbf{r}, \sigma) - \lambda^q & \tilde{h}^q(\mathbf{r}, \sigma) \\ \tilde{h}^q(\mathbf{r}, \sigma) & -(h^q(\mathbf{r}, \sigma) - \lambda^q) \end{pmatrix} \begin{pmatrix} \varphi_{1,i}^q(\mathbf{r}, \sigma) \\ \varphi_{2,i}^q(\mathbf{r}, \sigma) \end{pmatrix} = E_i \begin{pmatrix} \varphi_{1,i}^q(\mathbf{r}, \sigma) \\ \varphi_{2,i}^q(\mathbf{r}, \sigma) \end{pmatrix}$$

J.Dobaczewski, H.Flocard and J.Treiner, NPA422(1984)103

A.Bulgac, FT-194-1980 (Institute of Atomic Physics, Bucharest)

□ Mean-field Hamiltonian

$$h = \frac{\delta\mathcal{E}}{\delta\rho}$$

□ Pairing field

$$\tilde{h} = \frac{\delta\mathcal{E}}{\delta\tilde{\rho}}$$

HFB equations solved directly on the 2D lattice.

➤ 11-point formula for derivative

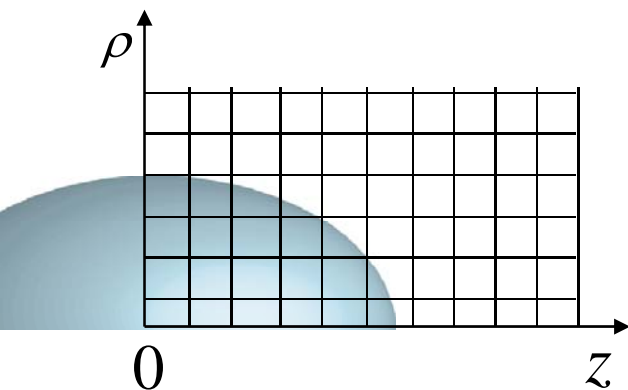


✓ Simple

✓ Appropriate for describing the spatially extended structure of wave functions



H.O. basis



Q(uasiparticle-)RPA

HFB equations \longrightarrow Quasiparticle basis (i,j,k,l)

KY, N.V.Giai, PRC78(2008)064316

The QRPA equation in a matrix form

$$\begin{pmatrix} A_{\alpha\beta\gamma\delta} & B_{\alpha\beta\gamma\delta} \\ B_{\alpha\beta\gamma\delta} & A_{\alpha\beta\gamma\delta} \end{pmatrix} \begin{pmatrix} X_{\gamma\delta}^i \\ Y_{\gamma\delta}^i \end{pmatrix} = \hbar\omega_i \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \begin{pmatrix} X_{\alpha\beta}^i \\ Y_{\alpha\beta}^i \end{pmatrix}$$

Residual interactions

✓ particle-hole channel: $\frac{\delta^2 \mathcal{E}_{\text{Sky}}}{\delta \rho(\mathbf{r}') \delta \rho(\mathbf{r})}$

$$\begin{aligned} v_{ph}(\mathbf{r}, \mathbf{r}') = & [a_0 + a'_0 \boldsymbol{\tau} \cdot \boldsymbol{\tau}' + (b_0 + b'_0 \boldsymbol{\tau} \cdot \boldsymbol{\tau}') \boldsymbol{\sigma} \cdot \boldsymbol{\sigma}'] \delta(\mathbf{r} - \mathbf{r}') \\ & + [a_1 + a'_1 \boldsymbol{\tau} \cdot \boldsymbol{\tau}' + (b_1 + b'_1 \boldsymbol{\tau} \cdot \boldsymbol{\tau}') \boldsymbol{\sigma} \cdot \boldsymbol{\sigma}'] [\mathbf{k}^{\dagger 2} \delta(\mathbf{r} - \mathbf{r}') + \delta(\mathbf{r} - \mathbf{r}') \mathbf{k}^2] \\ & + [a_2 + a'_2 \boldsymbol{\tau} \cdot \boldsymbol{\tau}' + (b_2 + b'_2 \boldsymbol{\tau} \cdot \boldsymbol{\tau}') \boldsymbol{\sigma} \cdot \boldsymbol{\sigma}'] [\mathbf{k}^{\dagger} \cdot \delta(\mathbf{r} - \mathbf{r}') \mathbf{k}] \\ & + (a_4 + a'_4 \boldsymbol{\tau} \cdot \boldsymbol{\tau}') (\boldsymbol{\sigma} + \boldsymbol{\sigma}') \cdot \mathbf{k}^{\dagger} \times \delta(\mathbf{r} - \mathbf{r}') \mathbf{k} \end{aligned}$$

We neglect the two-body **Coulomb** interaction.

✓ particle-particle channel: $\frac{\delta^2 \mathcal{E}_{\text{pair}}}{\delta \tilde{\rho}(\mathbf{r}') \delta \tilde{\rho}(\mathbf{r})}$

Strength distributions

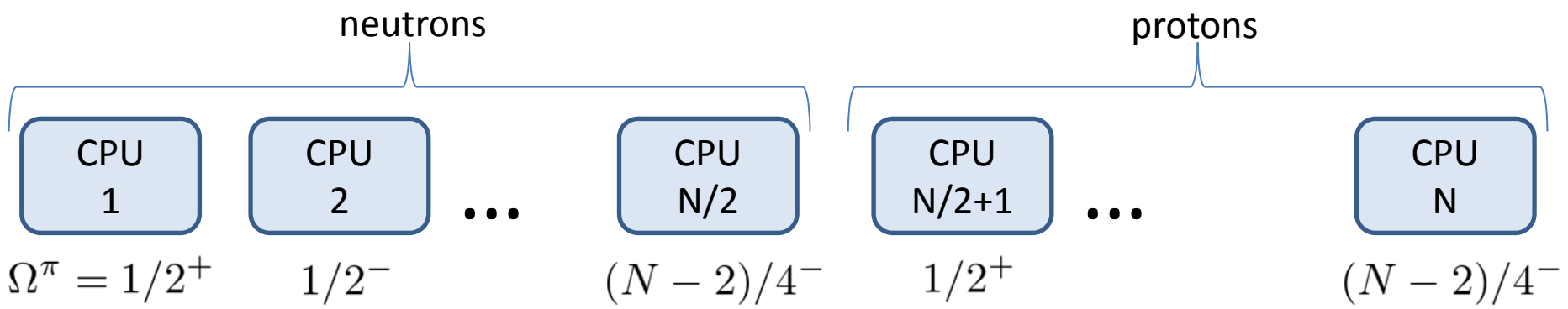
$$S_{\lambda}(E) = \frac{\Gamma/2}{\pi} \sum_i \sum_K \frac{|\langle i | \hat{F}_{\lambda} | 0 \rangle|^2}{(E - \hbar\omega_i)^2 + \Gamma^2/4} \quad \Gamma = 2 \text{ MeV}$$

Deformed HFB+QRPA for heavy nuclei

Using N CPUs:

HFB equations for each angular momentum, parity and isospin

$$\begin{pmatrix} h^q(\mathbf{r}, \sigma) - \lambda^q & \tilde{h}^q(\mathbf{r}, \sigma) \\ \tilde{h}^q(\mathbf{r}, \sigma) & -(h^q(\mathbf{r}, \sigma) - \lambda^q) \end{pmatrix} \begin{pmatrix} \varphi_{1,i}^q(\mathbf{r}, \sigma) \\ \varphi_{2,i}^q(\mathbf{r}, \sigma) \end{pmatrix} = E_i \begin{pmatrix} \varphi_{1,i}^q(\mathbf{r}, \sigma) \\ \varphi_{2,i}^q(\mathbf{r}, \sigma) \end{pmatrix}$$



Densities, Hamiltonians



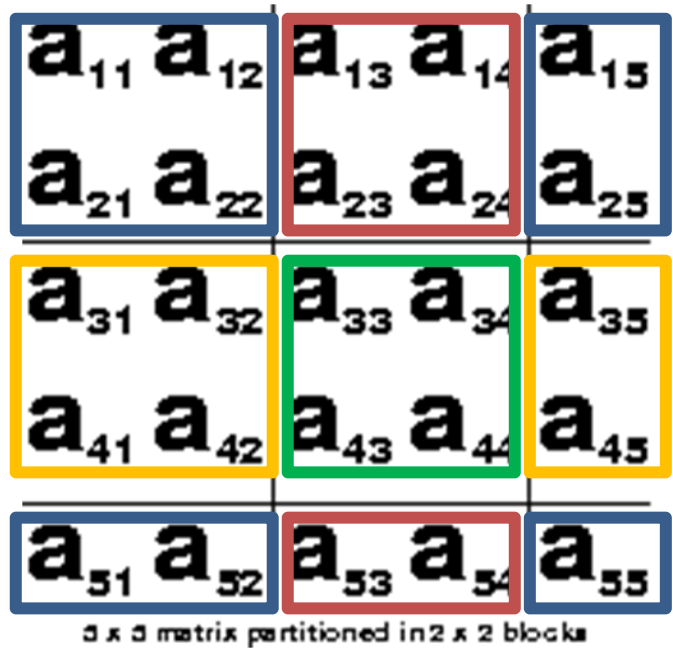
Iteration

Deformed HFB+QRPA for heavy nuclei

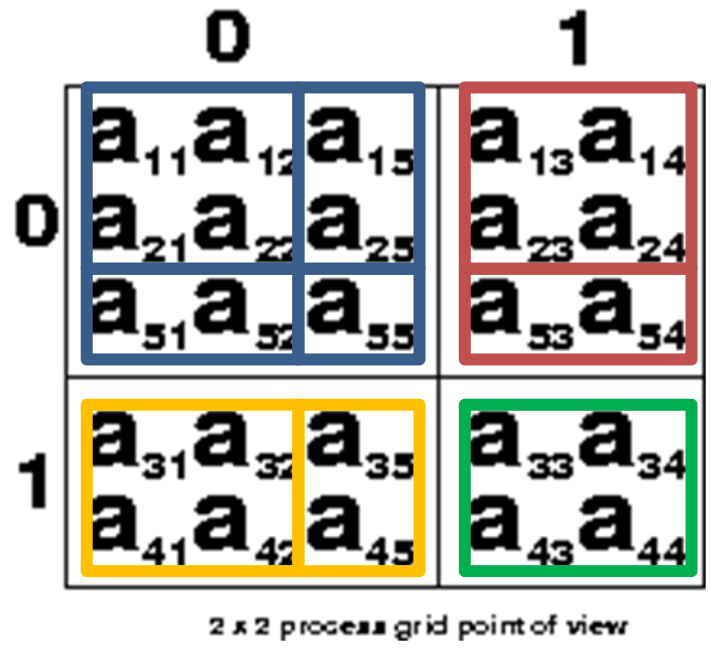
Distribution of the QRPA matrices

Ex. Using 4 CPUs

block matrix



original matrix (global)

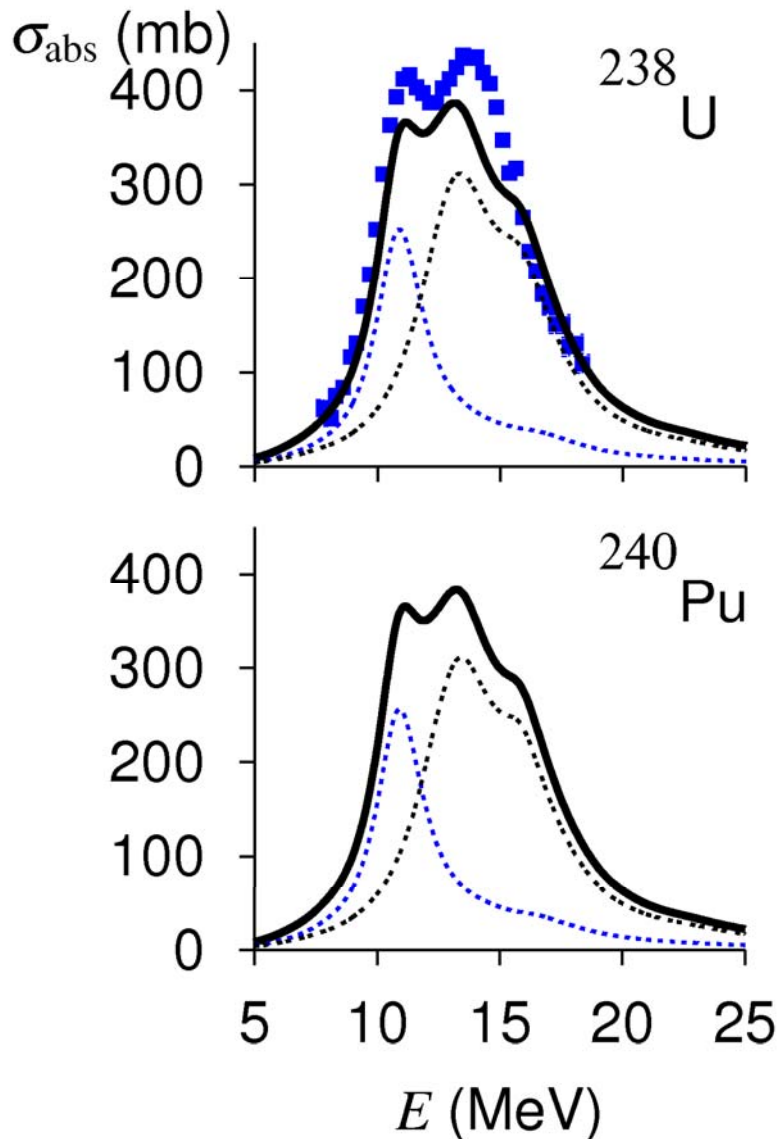


distributed matrix (local)

- ✓ Matrix elements
- ✓ Diagonalization → ScaLAPACK

Dipole responses in actinides

SkM* functional



HFB calc. (using 64 CPUs)

Box: $14.7 \text{ fm} \times 14.4 \text{ fm}$

Cut-off: $\Omega \leq \frac{31}{2}$, $E_{\alpha} \leq 60 \text{ MeV}$

QRPA calc.

Cut-off: $E_{\alpha} + E_{\beta} \leq 60 \text{ MeV}$

of 2qp excitation: about 50,000

Matrix elements: 590 CPU hours

Diagonalization: 330 CPU hours

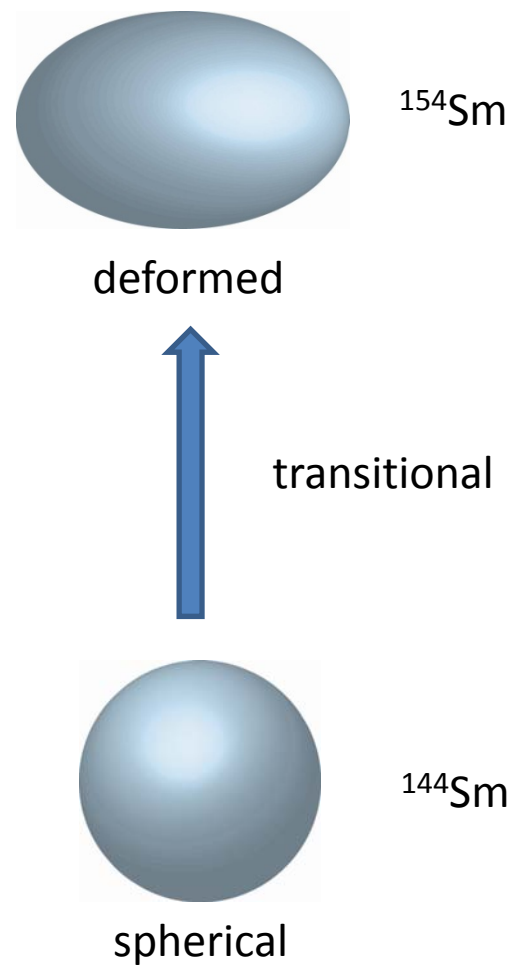
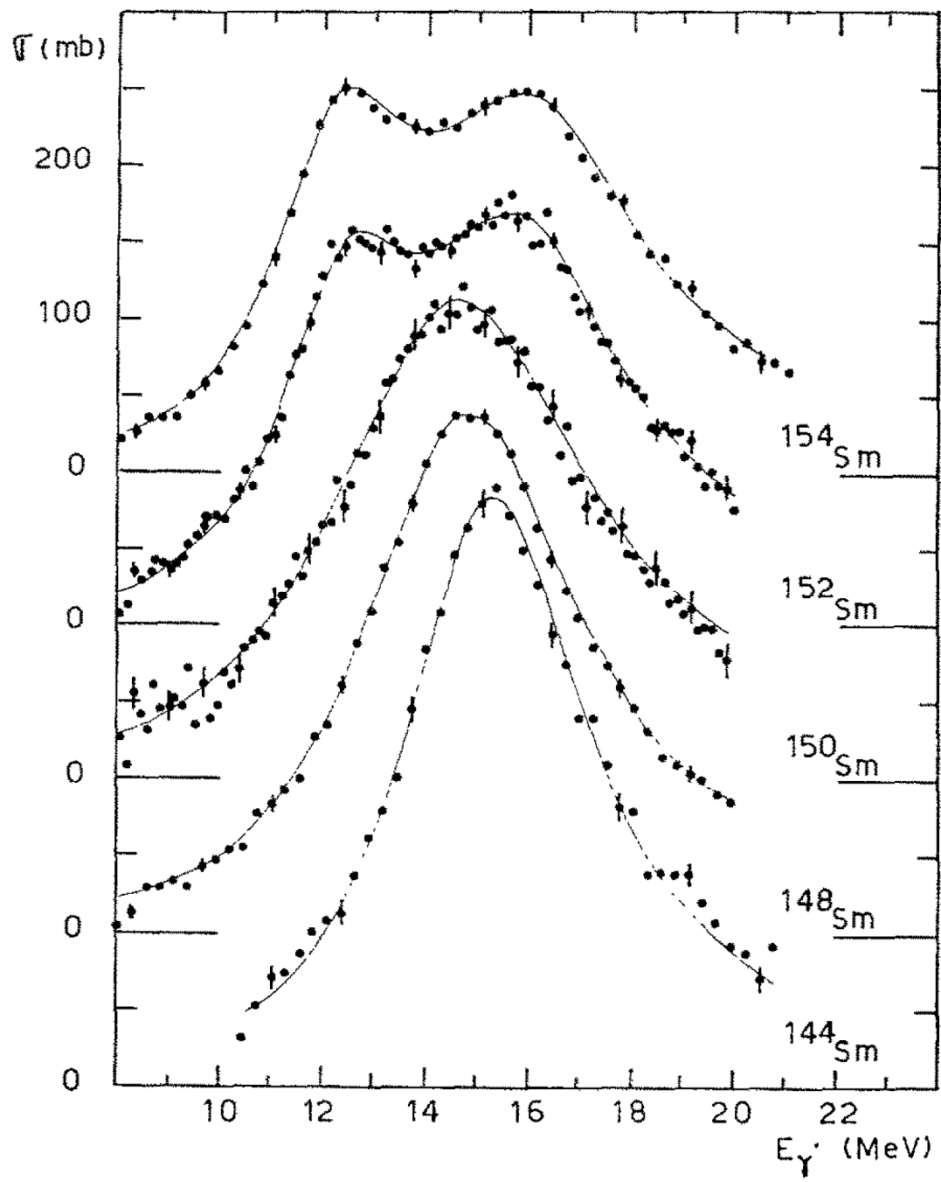


512 CPUs@RICC

Matrix elements: 69 minutes

Diagonalization: 38 minutes

Evolution of nuclear deformation in GDR

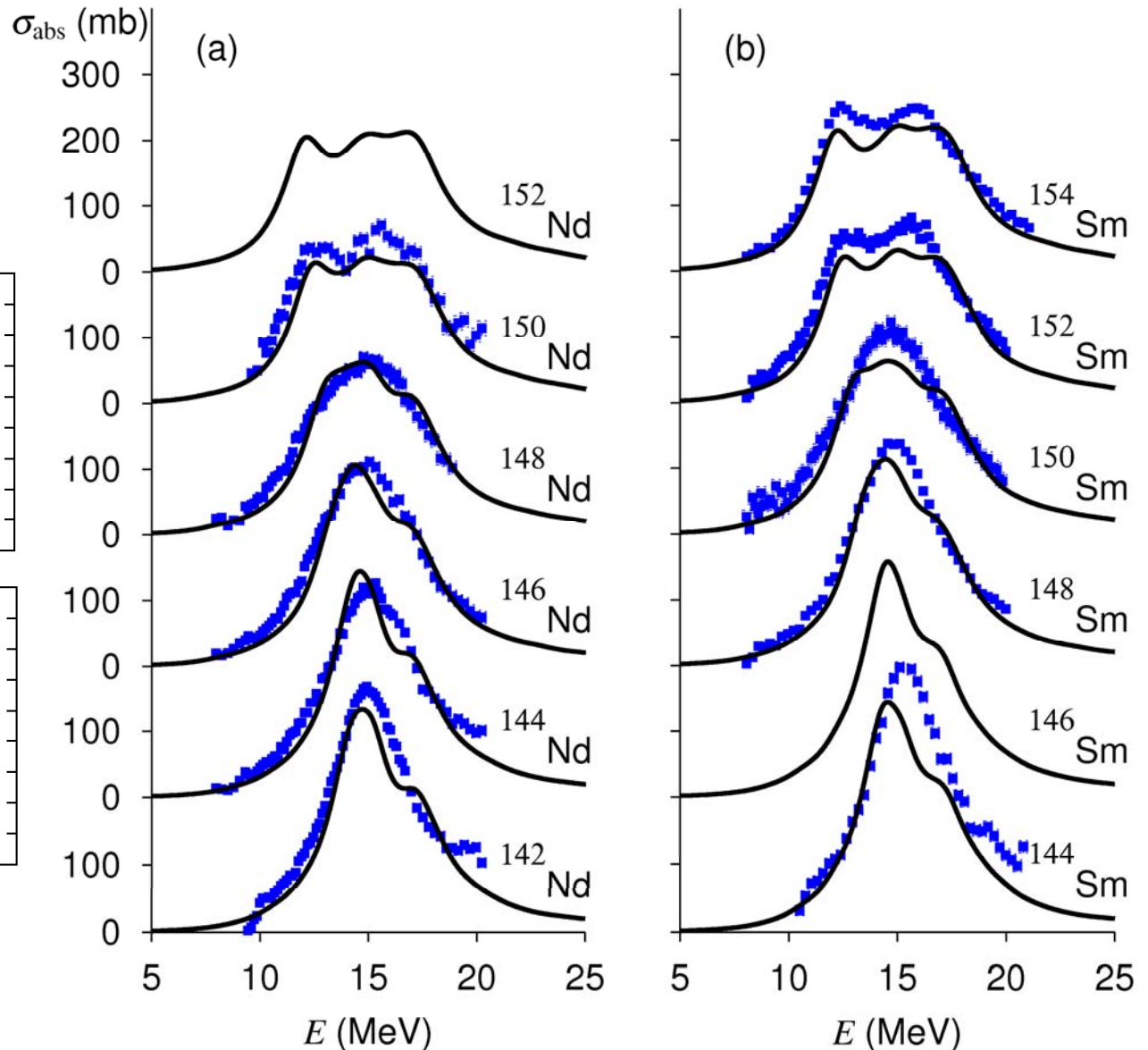
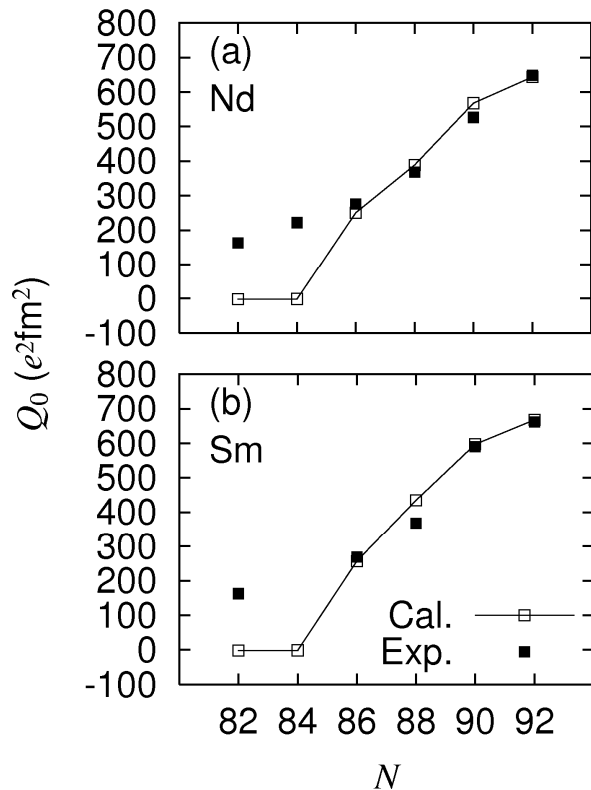


Skyme-QRPA photoabsorption cross sections

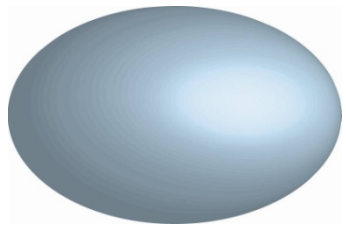
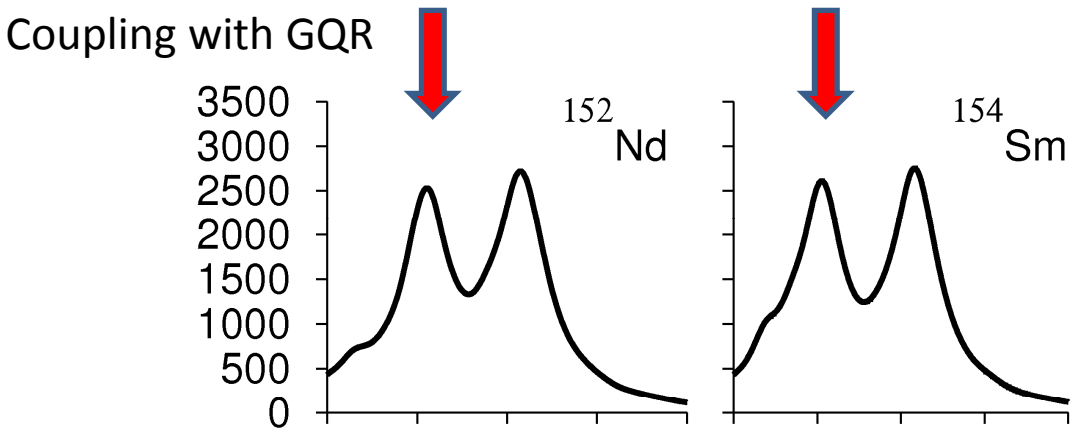
SkM* functional

KY, T.Nakatsukasa, arXiv:1008.1520

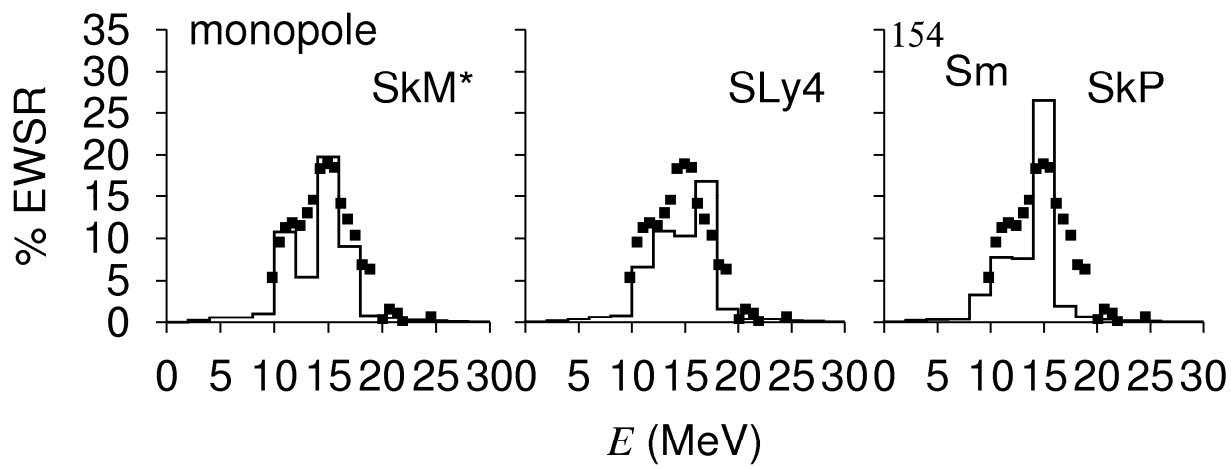
Intrinsic Q moment



Deformation effect on ISGMR



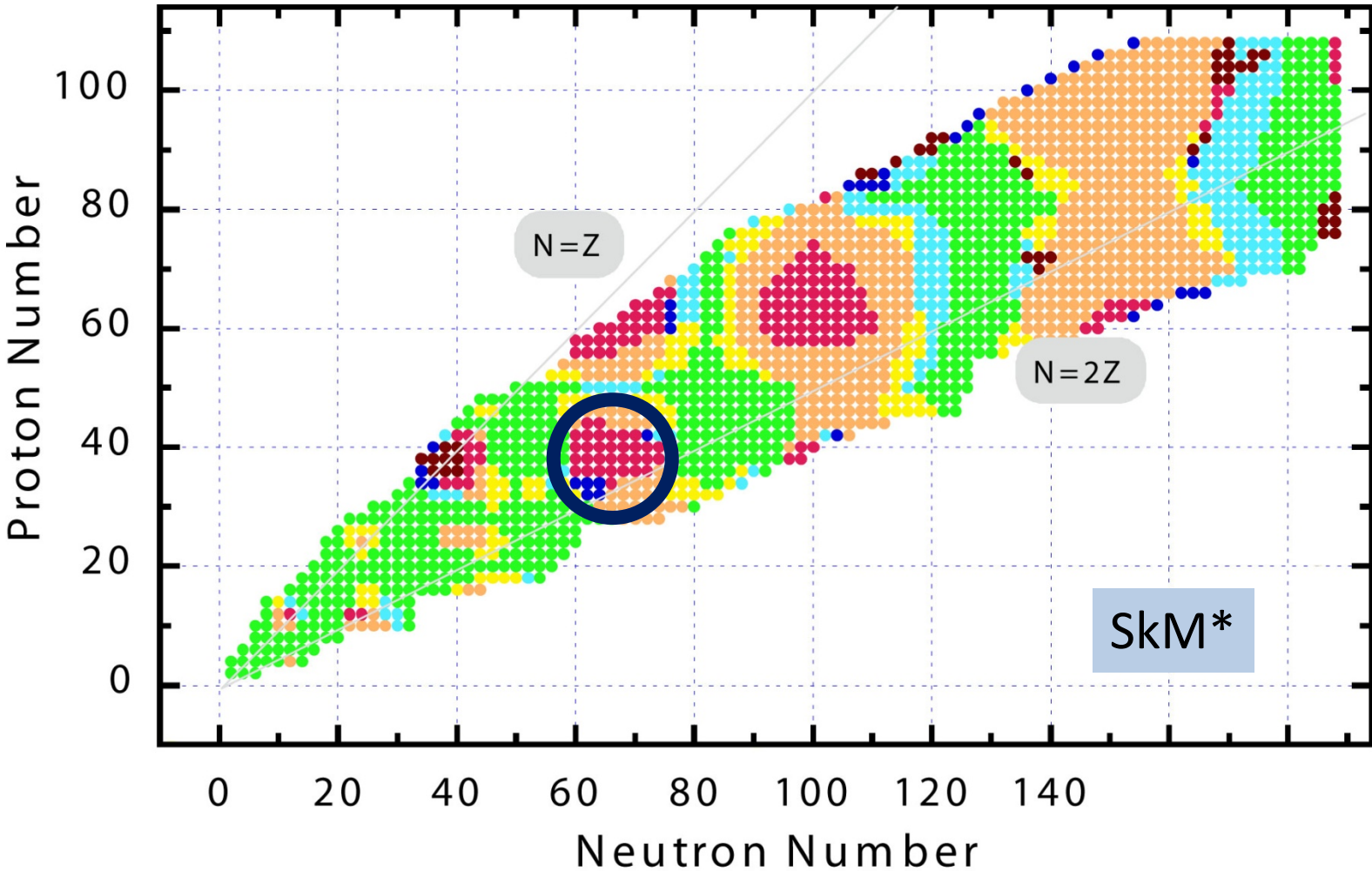
deformed



spherical

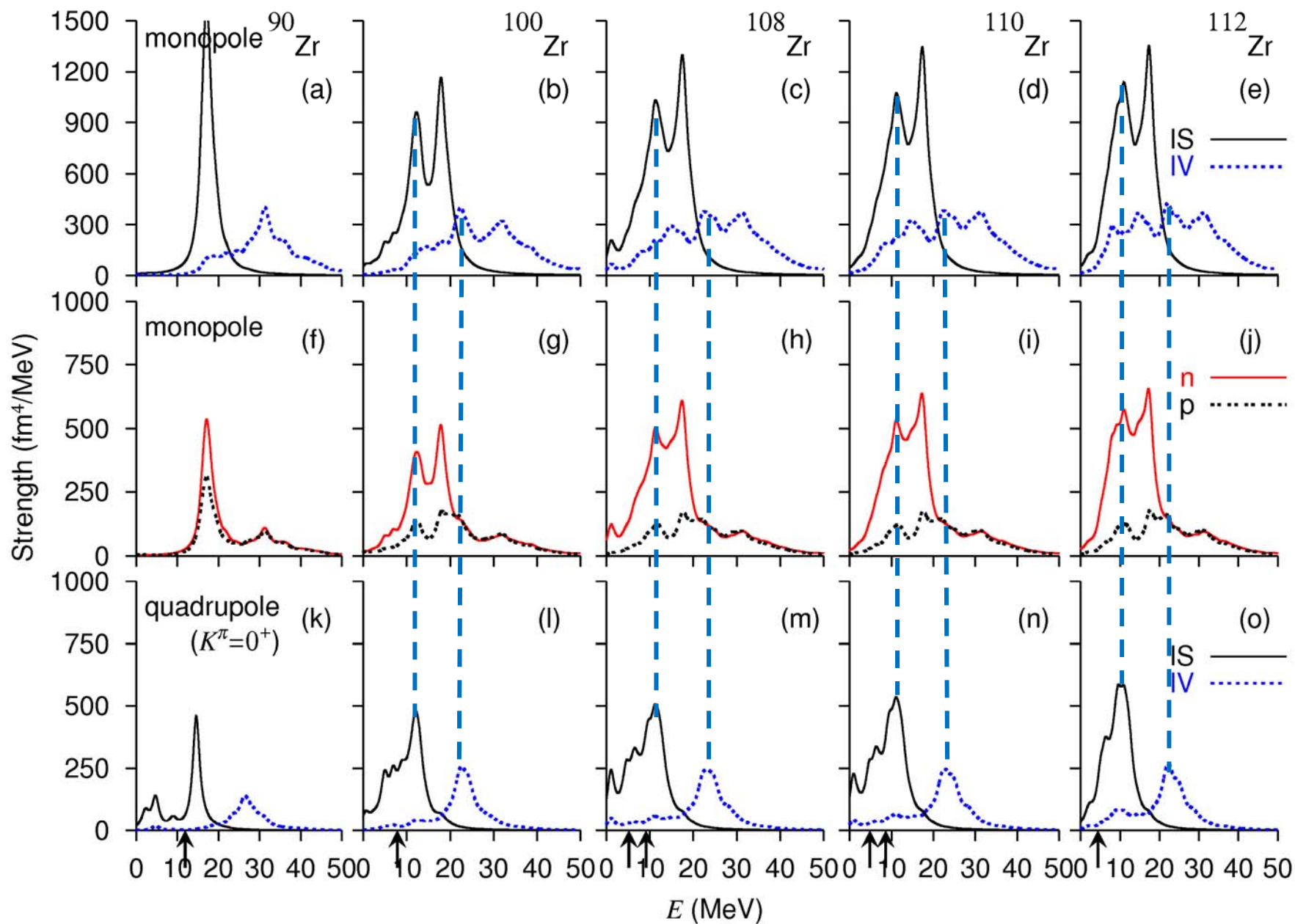
Exp.: D.H.Youngblood *et al.*, PRC69(2004)034315

Deformation in Zr isotopes



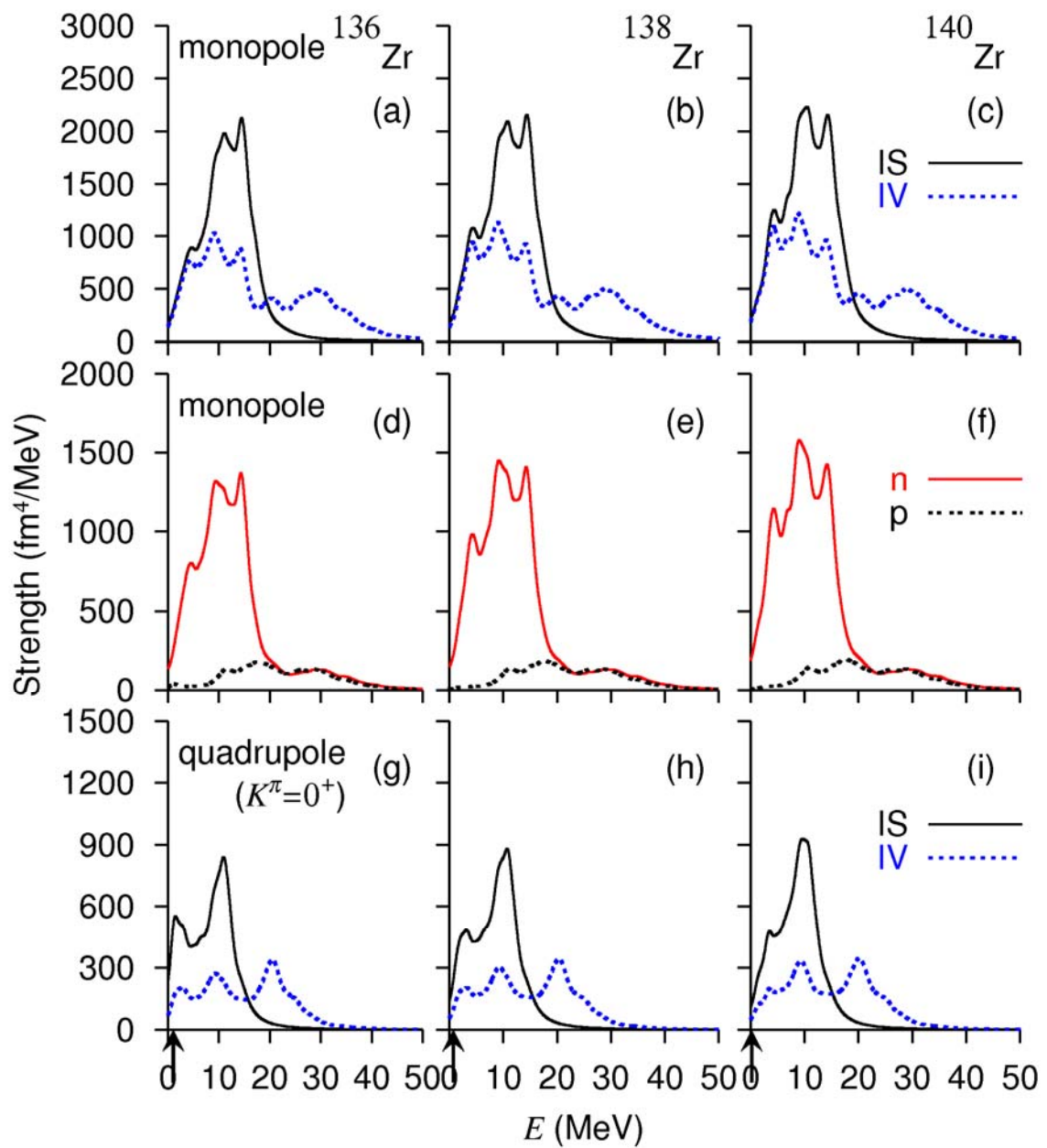
Strong deformation in Zr isotopes around $N=70$

Effects deformation and neutron excess on GMR



GMR in deformed drip-line nuclei

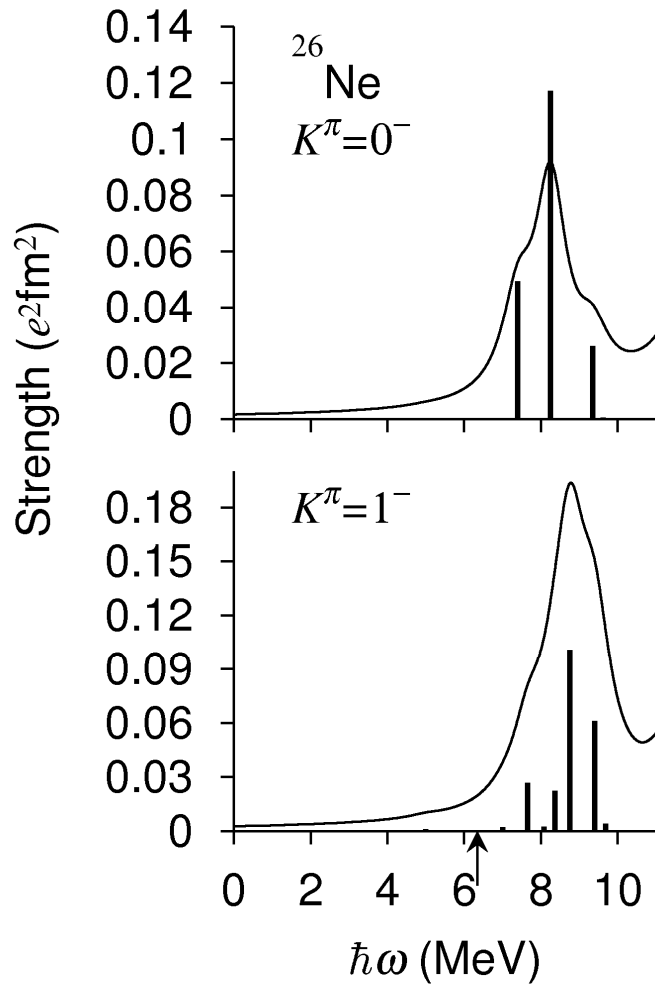
KY, arXiv:1008.1522



- ✓ Excitation of neutrons
- ✓ Threshold strength

Pygmy resonance in ^{26}Ne

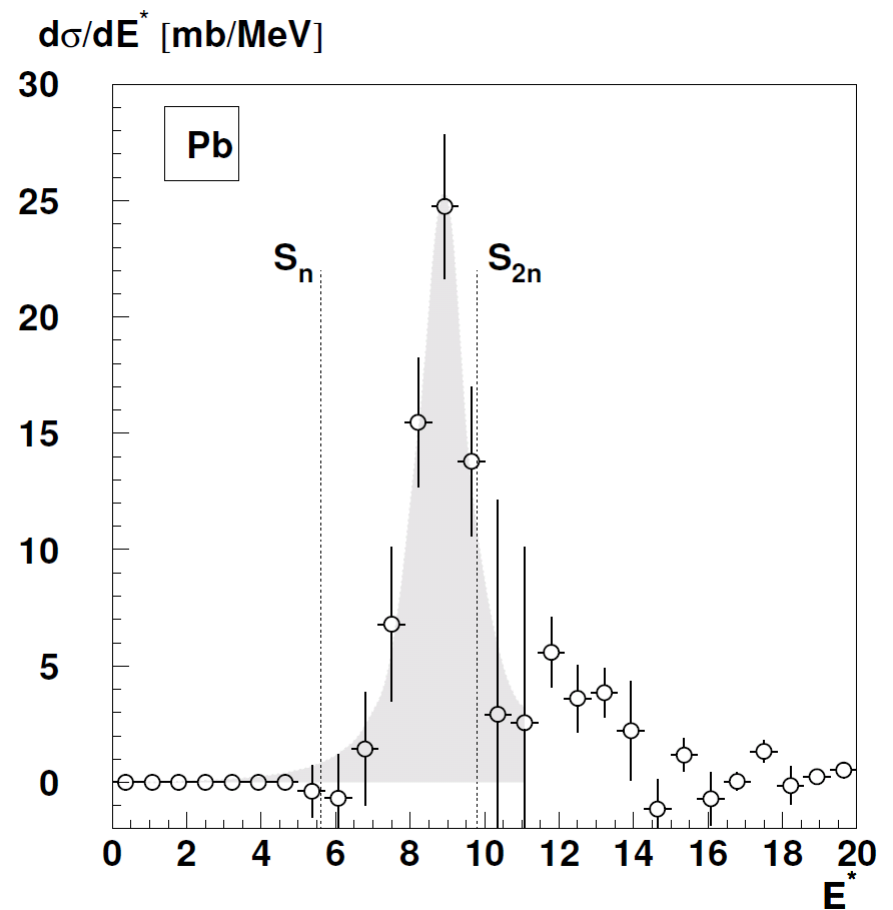
KY, N.V.Giai, PRC78(2008)014305



6% of the TRK sum rule (up to 10MeV)

Single-particle excitation is dominant: $\nu(2s_{1/2}^{-1}1p_{3/2})$

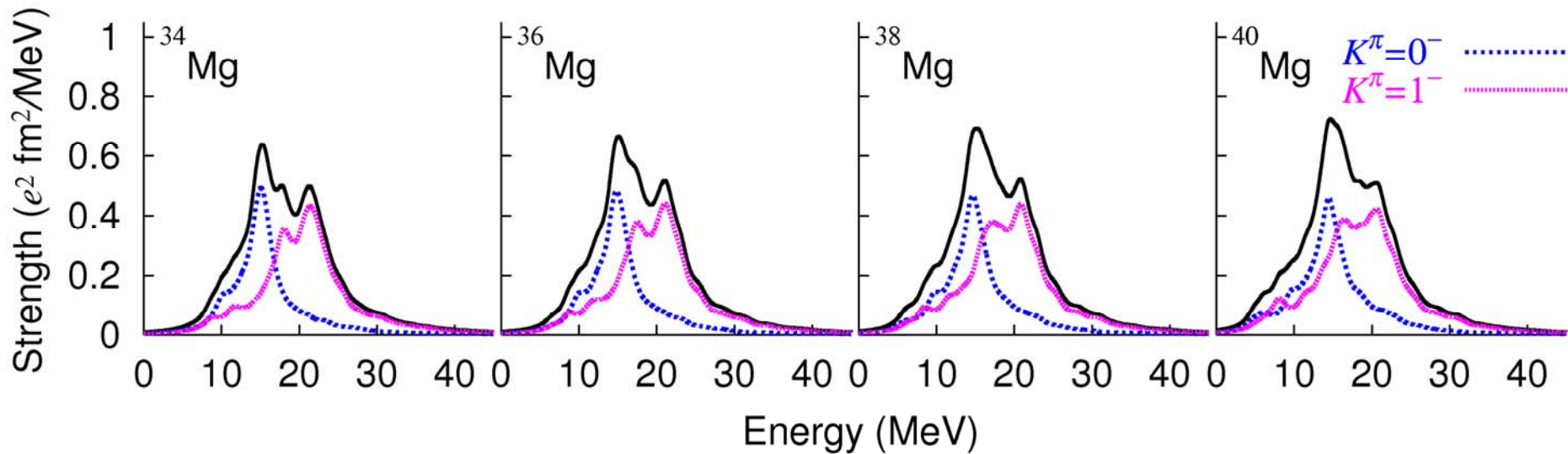
J.Gibelin *et al.*, PRL101(2008)212503



IV dipole excitations in neutron-rich Mg isotopes

KY, PRC80(2009)044324

| | ^{34}Mg | ^{36}Mg | ^{38}Mg | ^{40}Mg |
|---------------|------------------|------------------|------------------|------------------|
| $\beta_{2,n}$ | 0.35 | 0.31 | 0.29 | 0.28 |
| $\beta_{2,p}$ | 0.41 | 0.39 | 0.38 | 0.36 |



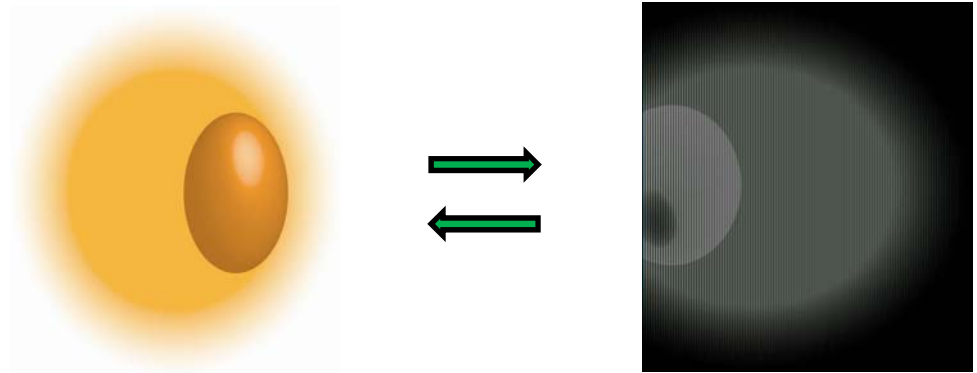
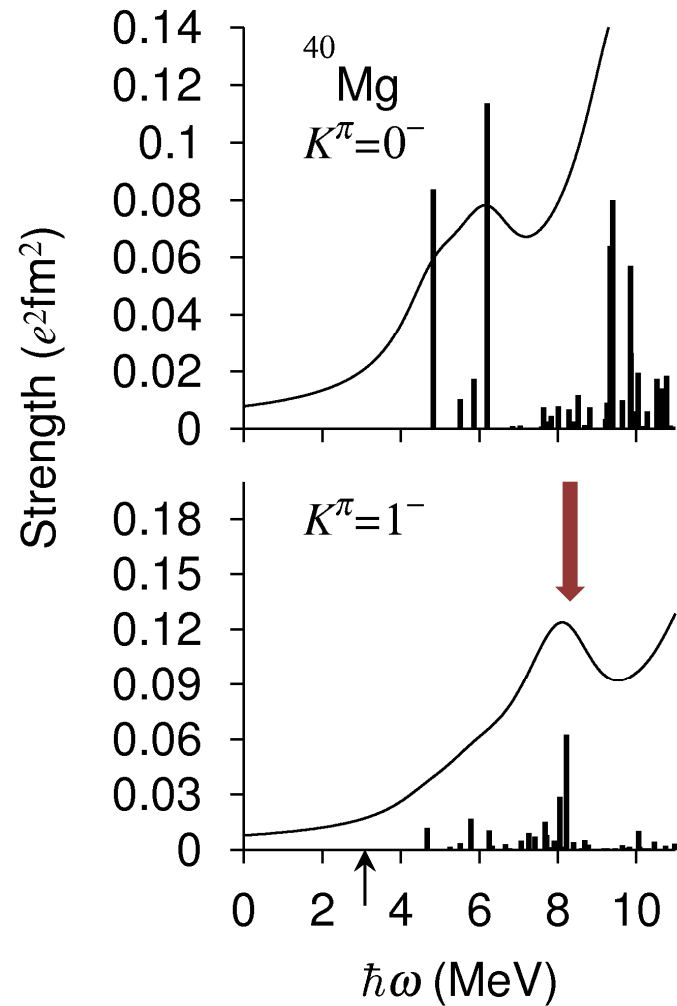
GDR: “K splitting”

→ good indicator of deformation 😊

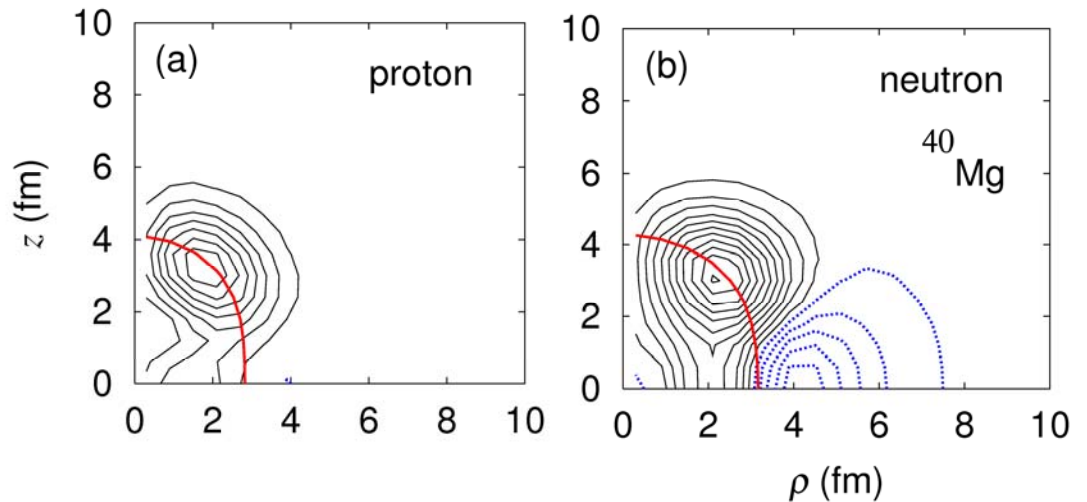
➤ Unique feature in neutron drip-line nuclei

✓ As approaching the drip line, the bump structure below 10MeV develops.

Pygmy mode in ^{40}Mg

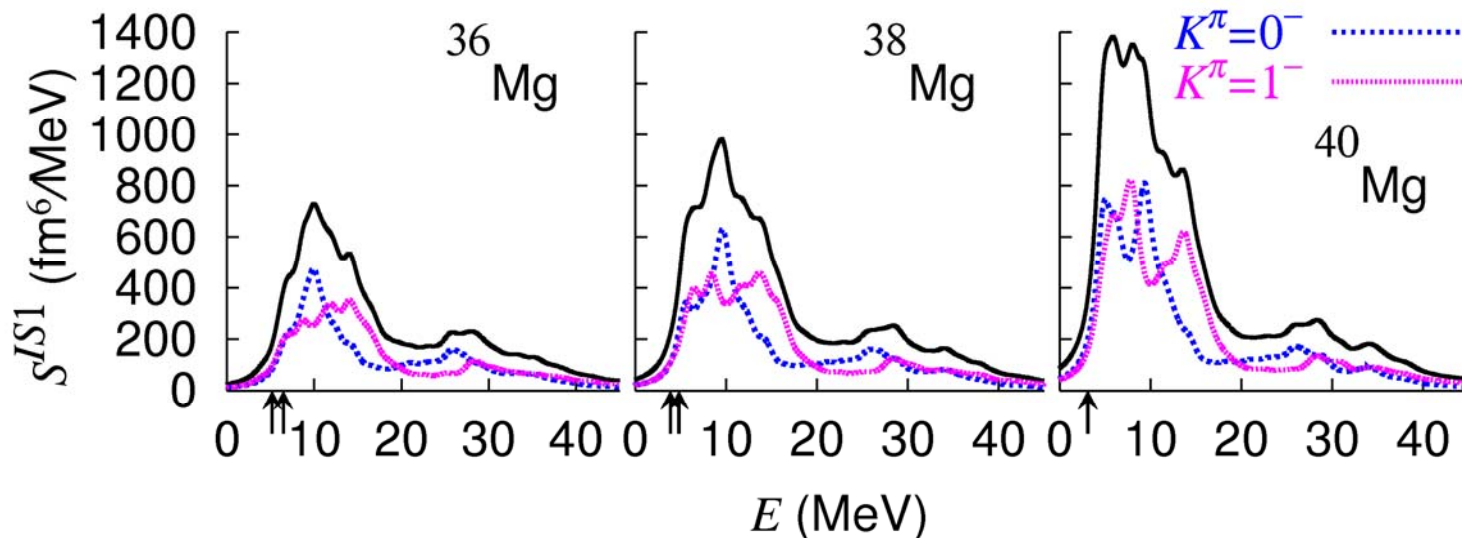


Transition density (8.2 MeV)



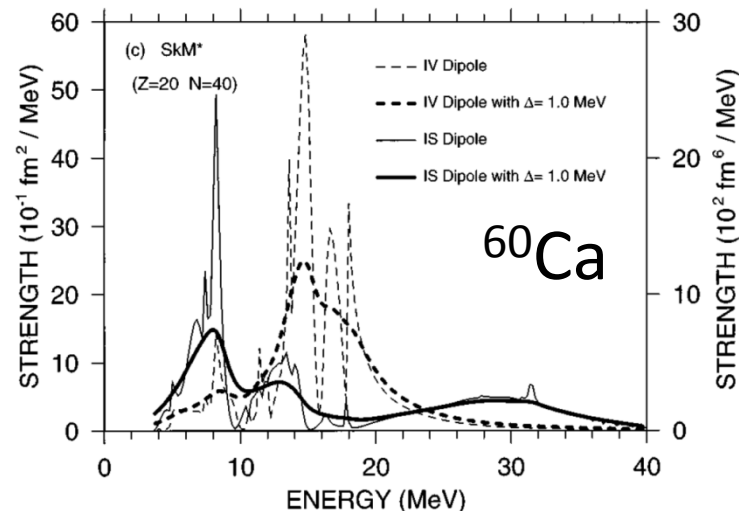
Isoscalar character of the pygmy mode

Responses for the compression dipole operator

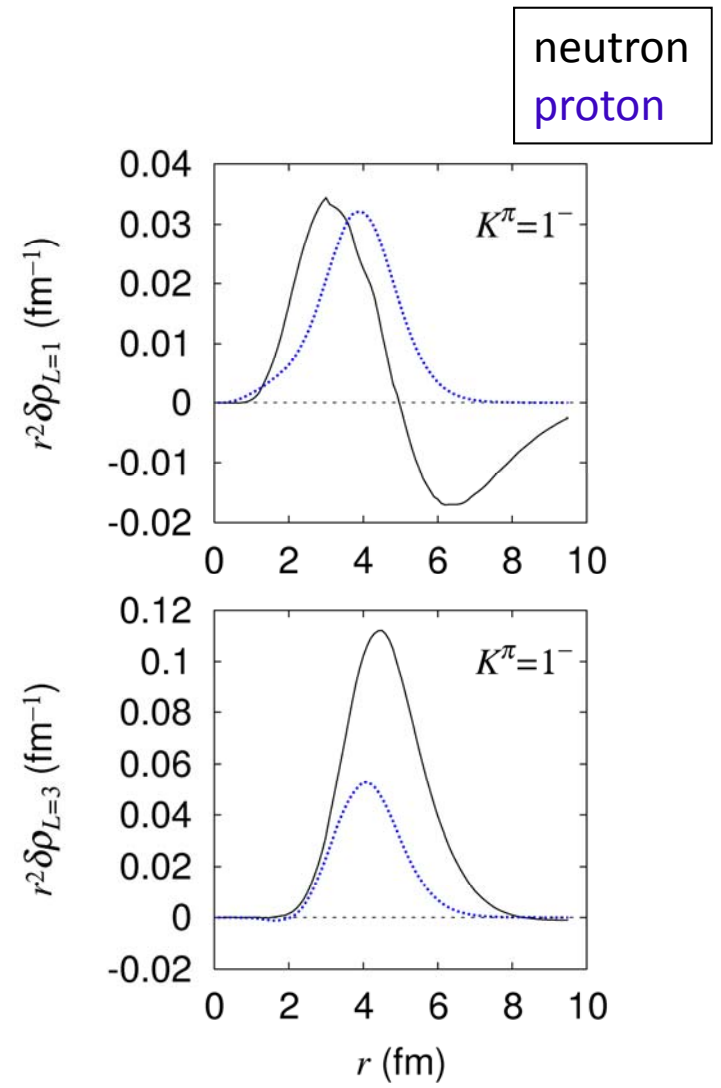
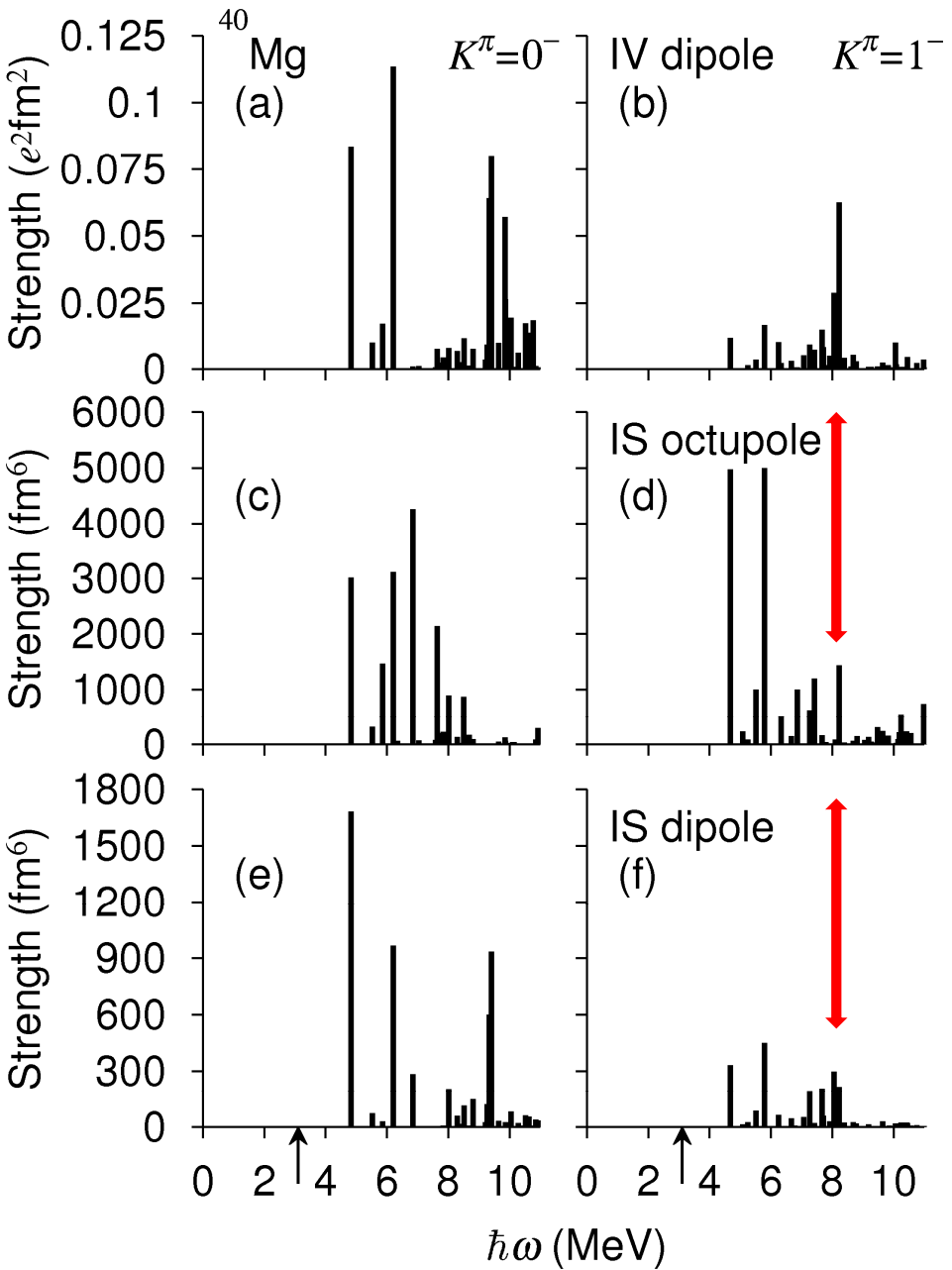


Tremendous enhancement of the transition strengths in the low-energy region

NEUTRON SKIN EFFECT (?)



Mixing of different modes of excitation



$$\delta\rho_L(r) = \int d\cos\theta d\varphi \delta\rho(\rho, z) Y_{LK}^*(\theta, \varphi)$$

Summary

Skyrme-EDF based deformed QRPA ready for the systematic investigation of the collective excitations in nuclei located in a wide mass region from drip line to drip line

High performance computer



✓ Nuclear deformation



Deformation splitting

Coupling among excitation modes with different angular momenta

GMR and the $K=0^+$ component of GQR

✓ Neutron excess



Enhancement of the transition strengths in the low energy region

Lower peak of the ISGMR in deformed neutron-rich nuclei

Pygmy mode: IV dipole + IS octupole + IS compression dipole