

Continuum Random Phase Approximation Theory

JAPAN-ITALY EFES Workshop Torino 6-8 Sept. 2010

VIVIANA DE DONNO

University of Salento and INFN Lecce (Italy)

In collaboration with:

G. Co'

University of Salento and INFN Lecce (Italy)

M. Anguiano, A. M. Lallena
University of Granada (Spain)

Aim:

How can we give predictions about ground and excited states of unstable nuclei?

- 1 The problem: how can we study unstable nuclei?
- 2 RPA or MF?
- 3 Self consistent RPA approach
- 4 Continuum in RPA (new technique with Sturmian function basis)
- 5 Results: chain of Oxygen
- 6 Results: chain of Calcium

Facilities:

EUROPE

SPES, LNL - 2015

SPIRAL2, Caen -2015

FAIR, GSI <2020

ISOLDE, CERN - operating

HIE-ISOLDE, CERN <2020

EURISOL - 2020

JAPAN

RIBF, RIKEN - operating

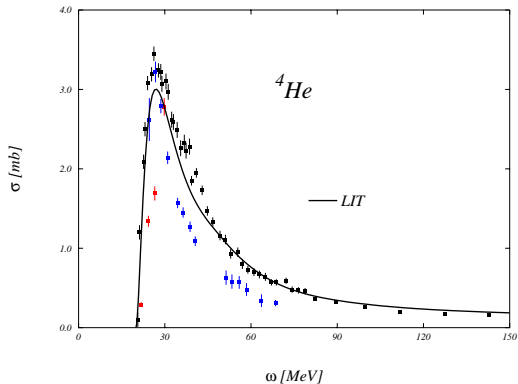
AMERICA

HRIBF, Oak Ridge National Laboratory- operating

FRIB, Michigan State University <2020

RIBRAS, São Paulo Pelletron Laboratory- operating

Microscopic calculation: Helium



Data:

T. Shima et al., *Phys. Rev. C* 72 (2005) 044004

B. Nilsson et al., *Phys. Lett. B* 626 (2005) 65; Yu. M. Arkatov et al. *Yad. Konst.* 4 (1979) 55.

LIT: D. Gazit et al., *Phys. Rev. Lett.* 96 (2006) 112301; G. Orlandini, priv. comm.

$$H|\Psi\rangle = E|\Psi\rangle \quad H^{\text{eff}}|\Psi^{\text{eff}}\rangle = E|\Psi^{\text{eff}}\rangle$$

$$H = H_0 + H_1 \quad H_0 P|\Psi\rangle = \omega P|\Psi\rangle \quad P^2 = P \quad Q = I - P$$

$$\left[H_0 + P \left(H_1 + H_1 Q \frac{1}{E - H_0 - Q H_1 Q} Q H_1 \right) P \right] P|\Psi\rangle = E P|\Psi\rangle$$

$$\left[H_0 + V^{\text{eff}}(E) \right] P|\Psi\rangle = E P|\Psi\rangle$$

Effective hamiltonian depends on the choice of H_0

Effective hamiltonian depends on the energy E

Random Phase Approximation

$$|\nu\rangle = Q_\nu^\dagger |0\rangle \quad Q_\nu |0\rangle = 0$$

$$Q_\nu^\dagger = \sum_{ph} X_{ph} a_p^\dagger a_h - \sum_{ph} Y_{ph} a_h^\dagger a_p$$

$$(\epsilon_p - \epsilon_h - \omega) X_{ph} + \sum_{p'h'} [v_{ph,p'h'} X_{p'h'} + u_{ph,p'h'} Y_{p'h'}] = 0$$

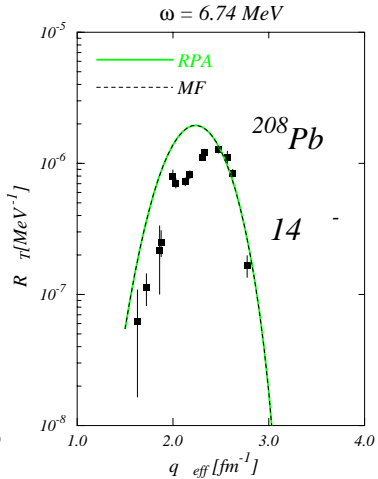
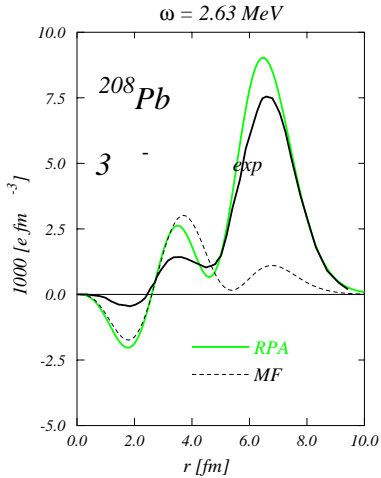
$$(\epsilon_p - \epsilon_h + \omega) Y_{ph} + \sum_{p'h'} [u_{ph,p'h'}^* X_{p'h'} + v_{ph,p'h'}^* Y_{p'h'}] = 0$$

$$v_{ph,p'h'} = \langle ph' | V | hp' \rangle - \langle ph' | V | p'h \rangle$$

$$u_{ph,p'h'} = \langle pp' | V | hh' \rangle - \langle pp' | V | h'h \rangle$$

$$\langle \nu | T | 0 \rangle = \sum_{ph} [X_{ph} \langle p | T | h \rangle - Y_{ph} \langle h | T | p \rangle]$$

MF and RPA



Input

Single particle wavefunctions

Single particle energies

Effective nucleon-nucleon interaction

Input

Single particle wavefunctions from Woods-Saxon potentials

Experimental single particle energies (when available)

Effective nucleon-nucleon interaction chosen to reproduce some empirical quantity.

The input changes for each nucleus.

Input

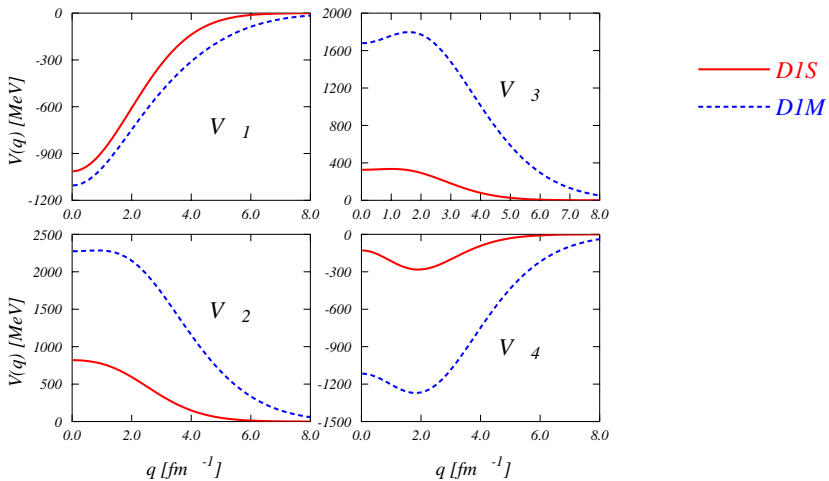
Single particle bases taken from Hartree Fock (HF) calculations
The same interaction is used in HF and RPA

A unique interaction for all the nuclei

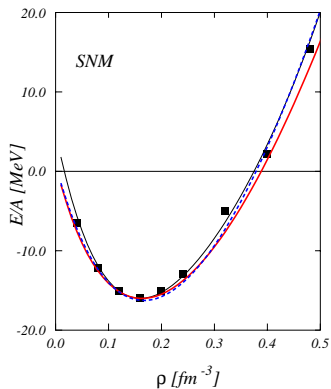
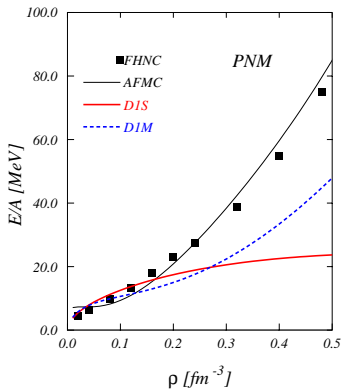
- Gogny-like interaction
- finite range
- zero-range Spin-Orbit term
- zero-range Density dependent term
- 14 parameters chosen with a fit of about 2000 nuclear binding energies and 700 charge radii.

Two parametrizations

- **D1S**: J. F. Berger et al., Comp. Phys. Comm. 63 (1991) 365
- **D1M**: S. Goriely et al., Phys. Rev. Lett. 102 (2009) 252501



Equations of state

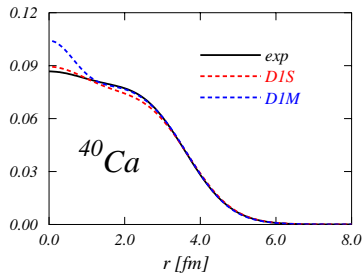
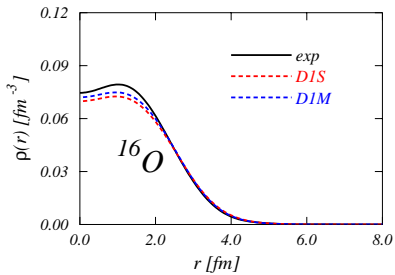


FHNC: A. Akmal et al., Phys Rev C 58 (1998) 1804

AFMC: S. Gandolfi et al., Mon. Not. Roy. Astron. Soc. 404 (2010) L35

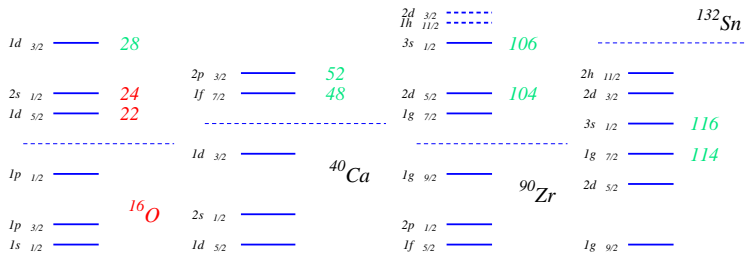
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Continuum RPA

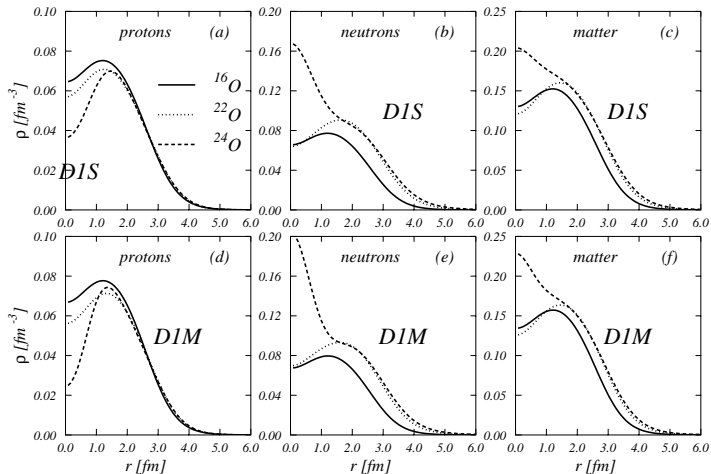


Data: C.W.D.Jager et al., Nucl. Data Tables 36 (1987) 495.

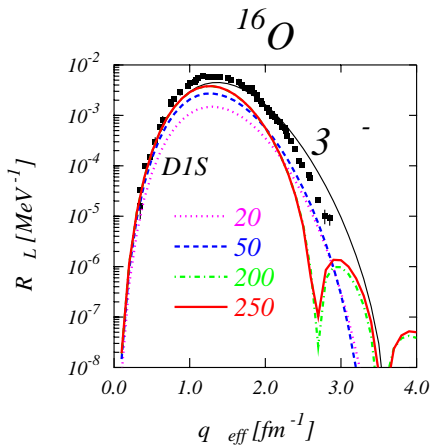
Isotope Chains



Distributions of Oxygen



Sensitivity to configuration space in the continuum



$\epsilon_{ph}^{\text{max}}$ [MeV]	ω [MeV]
20.0	9.11
50.0	8.55
200.0	7.87
250.0	7.85
exp	6.13

Data: R. Buti et al., Phys. Rev. C 33 (1986) 755

(A pedagogical and simplified presentation)

$$(\epsilon_p - \epsilon_h - \omega)X_{ph}(\epsilon_p) + \sum_{p'h'} \int d\epsilon_{p'} v_{ph,p'h'}(\epsilon_p, \epsilon_{p'})X_{ph}(\epsilon_{p}') = 0$$

Definition of a new unknown

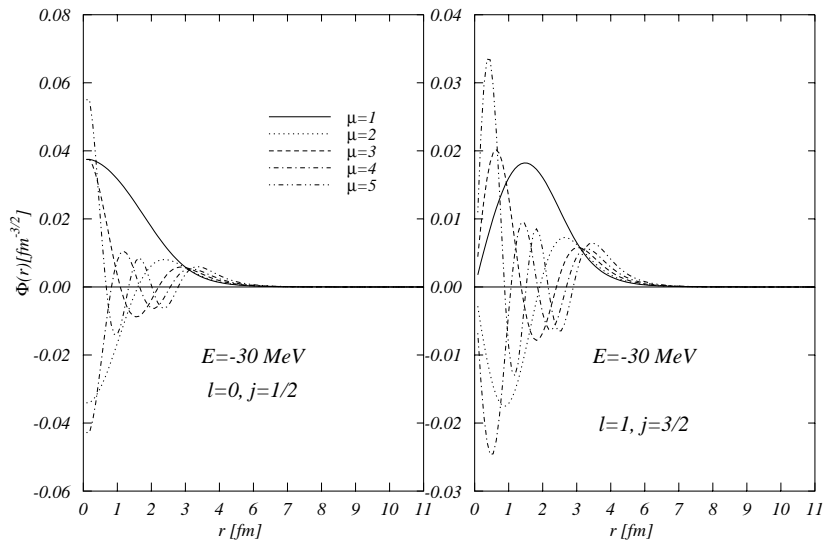
$$f_{ph}(r) = \int d\epsilon_p X_{ph}(\epsilon_p) R_p(r, \epsilon_p)$$

A new equation to be solved

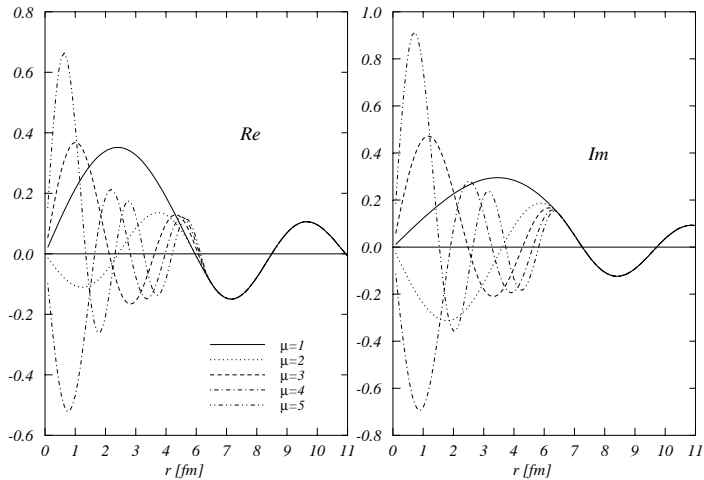
$$0 = -\frac{\hbar^2}{2m} \nabla^2 f_{ph}(r) + U(r)f_{ph}(r) - \int dr' r'^2 W(r, r')f_{ph}(r') - (\epsilon_h + \omega)f_{ph}(r) \\ - \sum_{p'h'} \int dr' r'^2 \left[R_{h'}^*(r') v^{\text{dir}}(r, r') R_h^*(r) f_{p'h'}(r') - R_{h'}^*(r') v^{\text{exc}}(r, r') R_h^*(r') f_{p'h'}(r) \right]$$

Expansion of $f_{ph}(r)$ on a Sturm-Bessel functions basis

Sturmian functions

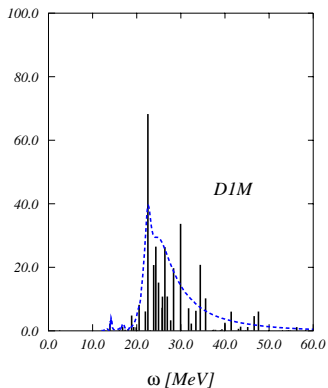
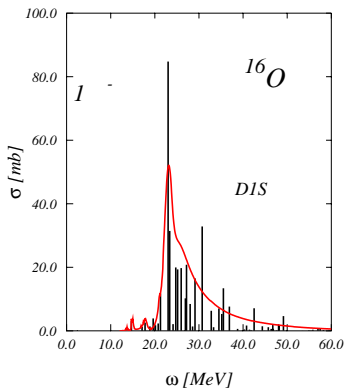


Sturmian functions



$\epsilon = 30$ MeV, $l = 1$, $j = 3/2$, ^{16}O

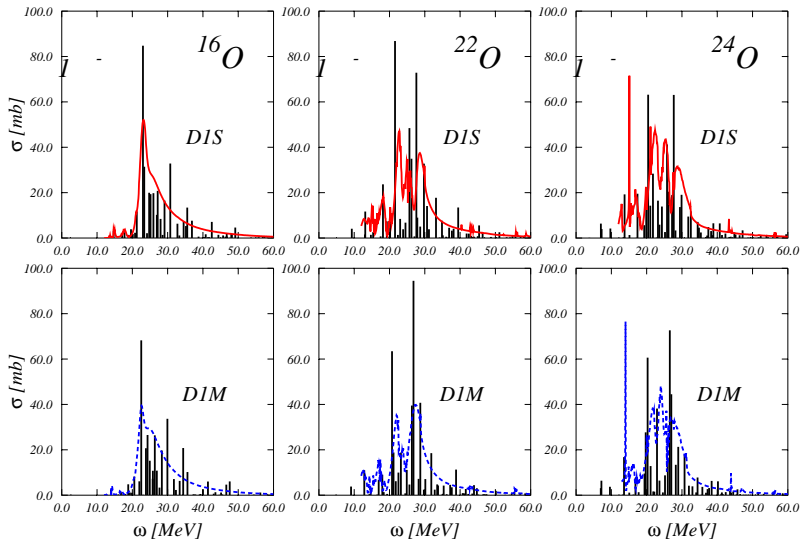
Continuum versus Discrete RPA



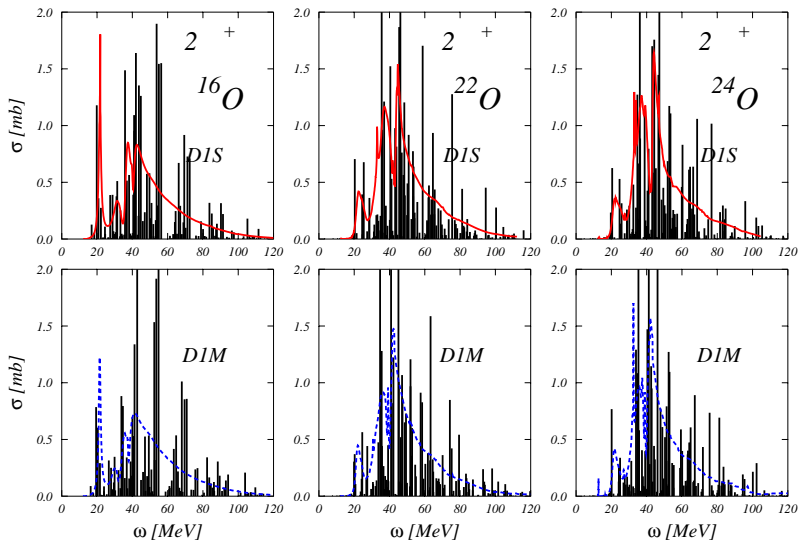
Centroid energies in MeV

ϵ_{ph}^{\max}	20	50	200	250	cont.
D1S	24.06	27.80	28.27	28.25	28.58
D1M	24.74	27.82	28.25	28.23	28.57

Continuum versus Discrete RPA: 1^- Oxygen chain



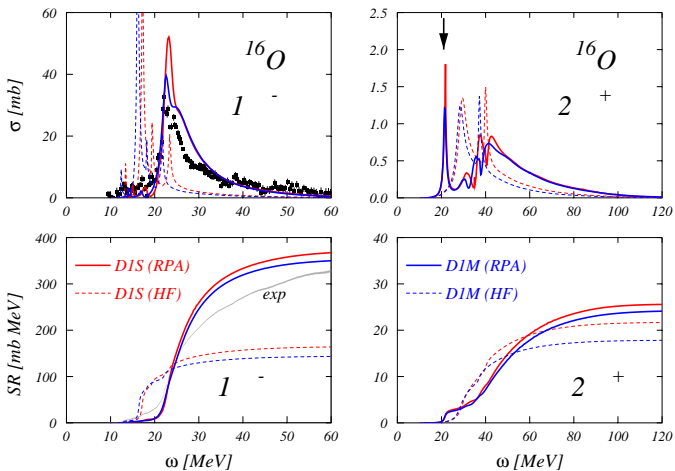
Continuum versus Discrete RPA: 2^+ Oxygen chain



Centroid energies in MeV

	D1S(dis)	D1S(con)	D1M(dis)	D1M(con)
1^-				
^{16}O	28.27	28.58	28.24	28.56
^{22}O	27.34	27.43	27.09	27.50
^{24}O	26.08	26.18	25.99	26.31
2^+				
^{16}O	67.99	45.45	69.04	45.76
^{22}O	68.77	44.87	67.50	45.00
^{24}O	67.54	44.21	60.07	43.74

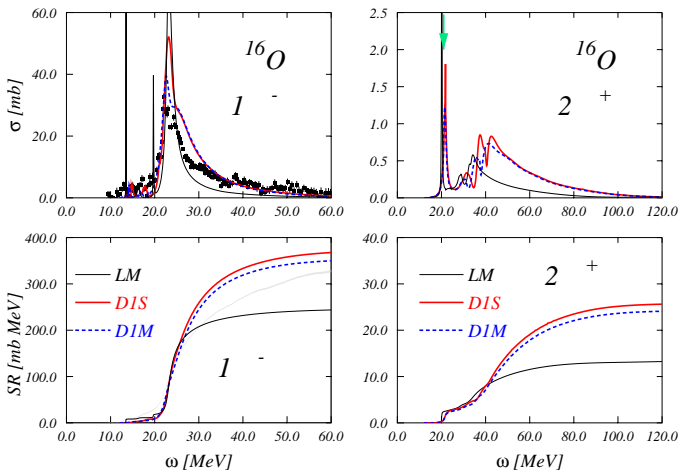
RPA versus MF



1^- data: J. Ahrens et al., Nucl. Phys. A 251 (1975) 479.

2^+ data: K. T. Knöpfke et al., Phys. Rev. Lett. 35 (1975) 779

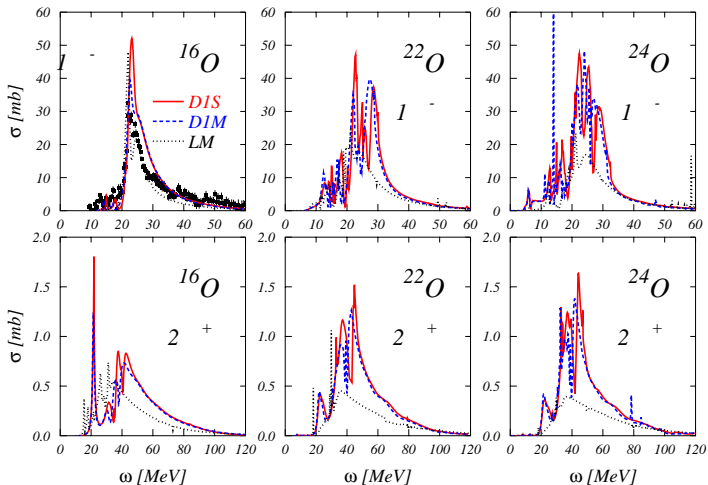
Self consistent versus Phenomenological approach



1^- data: J. Ahrens et al., Nucl. Phys. A 251 (1975) 479.

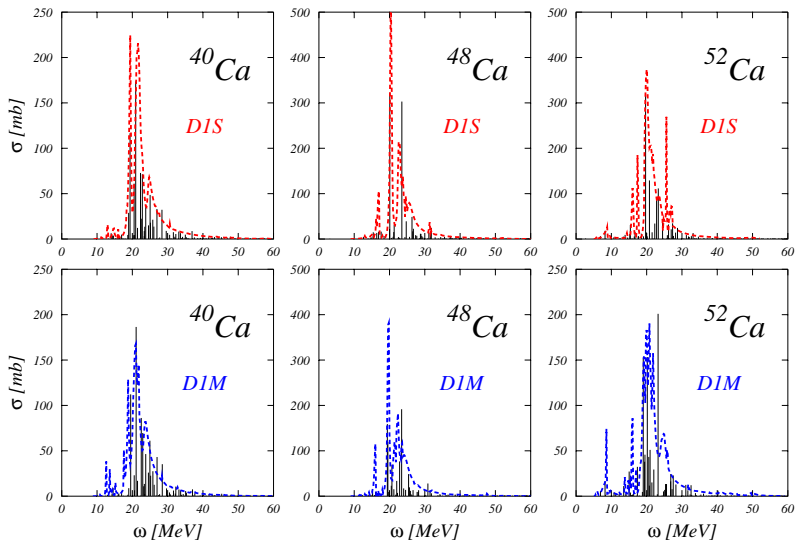
2^+ data: K. T. Knöpfke et al., Phys. Rev. Lett. 35 (1975) 779

Self consistent versus Phenomenological approach: Oxygen chain



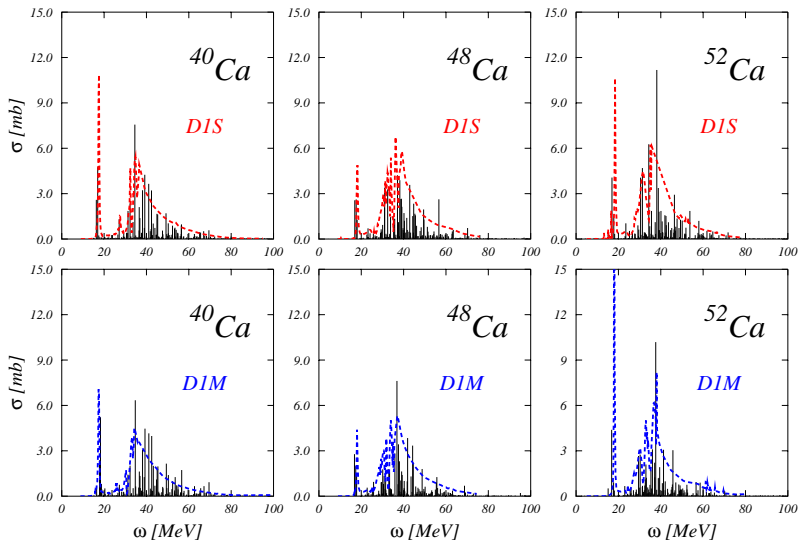
Continuum versus Discretum: 1^- Calcium chain

1^-

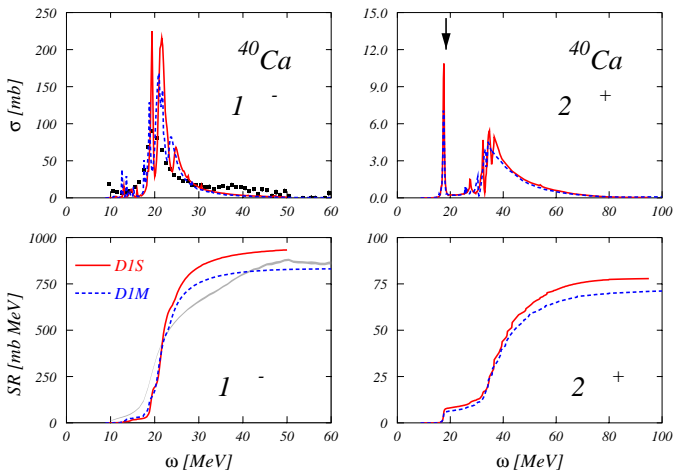


Continuum versus Discretum: 2^+ Calcium chain

2^+



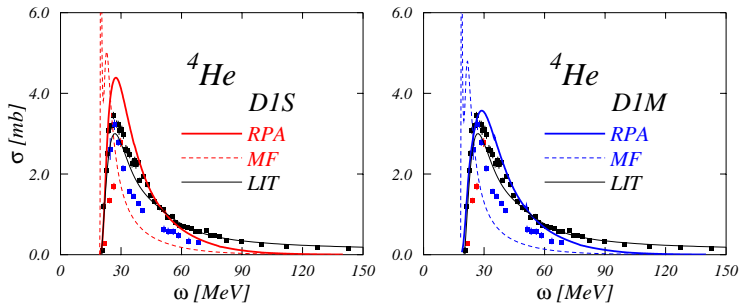
versus experimental data



1^- data: J. Ahrens et al., Nucl. Phys. A 251 (1975) 479.

2^+ data: empirical expression $63.0 A^{-1/3}$

Self-consistent Continuum RPA versus Microscopic Calculations



Data:

T. Shima et al., Phys. Rev. C 72 (2005) 044004

B. Nilsson et al., Phys. Lett. B 626 (2005) 65

Yu. M. Arkatov et al. Yad. Konst. 4 (1979) 55.

LIT:

D. Gazit et al., Phys. Rev. Lett. 96 (2006) 112301

G. Orlandini, priv. comm.

- 1 Our continuum RPA technique allows us to do calculations with interactions with **finite range and tensor channel**.
- 2 The **D1S** and **D1M** forces produce very similar results.
- 3 **Comparison with MF calculations**: MF does not predict the presence of giant resonances.
- 4 **Comparison with discrete RPA**: need of a correct treatment of the continuum in self-consistent calculations.
- 5 **Comparison with phenomenological CRPA**: inadequacy of the phenomenological approach in the study of nuclei lying in experimentally unexplored parts of the nuclear isotope chart.

- 1 **Self-consistent CRPA** calculations describe rather well the experimental positions of the giant resonances peaks, both for the 1^- and 2^+ excitations.
- 2 On the other hand, the strengths distributions are incorrect, and the problem could be solved by considering the excitation of **two particles-two holes pairs**. This is confirmed by the results obtained in ^4He . In this case, the description of the ground state is much worse than that of heavier nuclei. However, the description of the total photoabsorption cross section is much better because in this system the contribution of more complex excitation modes is very small.